

CP Violation in Charmless 3-body B decays

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$B^\pm \rightarrow h^+ h^- h^\pm$ LHCb Brazilian Group



Outline

- Theory and Techniques
- The LHCb Detector
- $B^\pm \rightarrow h^+ h^- h^\pm$ decays. ($h = K, \pi$)
- $B^\pm \rightarrow p \bar{p} h^\pm$ decays.

Theory and Techniques

Introduction

- **CP Violation** (**Sakharov**, Baryogenesis)
- Discovered 1964 (**neutral kaons**)
- **Standard Model CPV** (**CKM matrix**)
- **SM CPV** (**insufficient**, **Universe**)
- **CKM matrix**: **D** (small or null), **B** (measurable)
- **3-body decays** are interesting (**signatures in Dalitz Plot**)

Conditions for Direct CP Violation

- In charged B decays, we have multiple amplitudes :

$$\mathcal{A}(B \rightarrow f) = |A_1|e^{i(\delta_1+\phi_1)} + |A_2|e^{i(\delta_2+\phi_2)} + |A_3|e^{i(\delta_3+\phi_3)} + \dots$$

- Strong phases** (δ_i) are invariant under CP Transformation: $\delta_i \rightarrow \delta_i$
- Weak phases** (ϕ_i) change sign under CP Transformation: $\phi_i \rightarrow -\phi_i$

$$\bar{\mathcal{A}}(\bar{B} \rightarrow \bar{f}) = |\bar{A}_1|e^{i(\delta_1-\phi_1)} + |\bar{A}_2|e^{i(\delta_2-\phi_2)} + |\bar{A}_3|e^{i(\delta_3-\phi_3)} + \dots$$

- The Asymmetry can be calculated as:

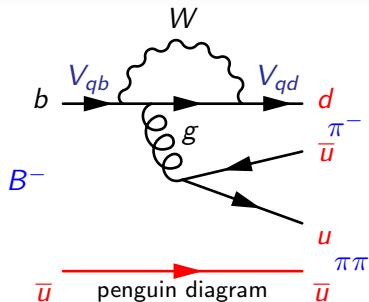
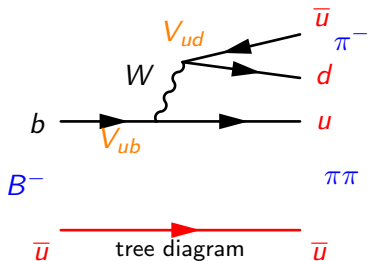
$$\mathcal{A}_{CP}(B \rightarrow f) = \frac{|\bar{\mathcal{A}}|^2 - |\mathcal{A}|^2}{|\bar{\mathcal{A}}|^2 + |\mathcal{A}|^2} \propto \sum_{ij} \sin(\delta_i - \delta_j) \sin(\phi_i - \phi_j)$$

- Conditions for Direct CP Violation:

- At least two amplitudes.**
- Non-zero weak phase difference, $\phi_i - \phi_j \neq 0$**
- Non-zero strong phase difference, $\delta_i - \delta_j \neq 0$**

BSS Model for the $B^\pm \rightarrow \pi^+ \pi^- \pi^\pm$ decay

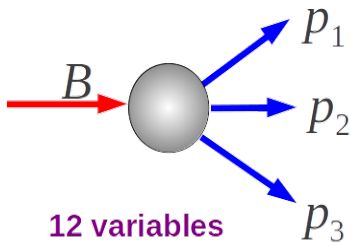
$$b \rightarrow du\bar{u}$$



- 1) **At least two amplitudes.** Tree \times Penguin
 - In both diagrams: **Initial State:** B meson, **Final State:** $\pi\pi\pi$
 - BSS model: b is considered as free. \bar{u} is considered an **espectator** (quark level)
- 2) **Non-zero weak phase difference:** **CKM:** $\mathcal{A}^T \propto V_{ub}V_{ud}$, $\mathcal{A}^P \propto V_{qb}V_{qd}$, $q = u, c, t$.
- 3) **Non-zero strong phase difference:** (penguin: q on its mass shell (u, c for b decays)).

Source of $\delta_i - \delta_j \neq 0$ are Short Distance Effects.!!!

Dalitz Plot



$$E_B = \sum_i E_i$$

1 constraint

$$\vec{p}_B = \sum_i \vec{p}_i$$

3 constraints

$$E_i = \vec{p}_i^2 + m_i^2$$

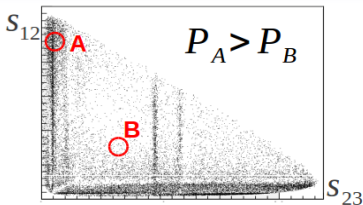
3 constraints

If p_1, p_2, p_3 pseudoscalars
3 constraints

12 variables – **10 constraints** = **2 variables**:

$$s_{12} = (p_1 + p_2)^2, s_{23} = (p_2 + p_3)^2$$

Dalitz Plot



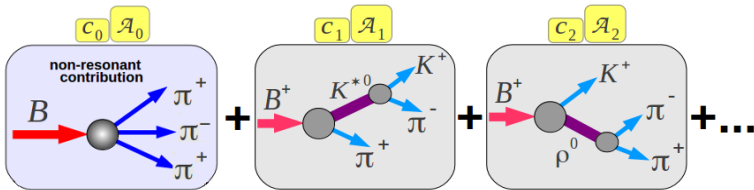
Probability Density Function:

$$\mathcal{P}(s_{12}, s_{23})$$

$$\mathcal{P} = |\mathcal{A}|^2$$

Amplitude: $\mathcal{A}(s_{12}, s_{23})$

Example: $B^+ \rightarrow K^+ \pi^- \pi^+$:



Isobar Model: the decay amplitude is a **coherent sum** of a non-resonant amplitude plus resonant amplitudes:

$$\mathcal{A}(s_{12}, s_{23}) = c_{nr} \mathcal{A}_{NR}(s_{12}, s_{23}) + \sum_k c_k \mathcal{A}_k(s_{12}, s_{23})$$

Amplitude Analysis

$$\mathcal{A}(s_{12}, s_{23}) = c_{nr} \mathcal{A}_{NR}(s_{12}, s_{23}) + \sum_k c_k \mathcal{A}_k(s_{12}, s_{23})$$

$\underbrace{\hspace{15em}}_{F^B(s_{12}, s_{23}) F^R(s_{12}, s_{23}) BW(s_{12}, s_{23}) \mathcal{M}(s_{12}, s_{23})}$

Fitting the model to data (DP plane) we obtain the **complex coefficients** c_{nr} , c_k which tell us the contribution of resonances.

Asymmetry : In order to consider asymmetry we define a contribution for the particle and the antiparticle:

$$\mathcal{A}(s_{12}, s_{23}) = \underbrace{\sum_j c_j \mathcal{A}_j(s_{12}, s_{23})}_{B^+ \text{ sample}} + \underbrace{\sum_j \bar{c}_j \bar{\mathcal{A}}_j(s_{12}, s_{23})}_{B^- \text{ sample}}, \quad \mathcal{A}_j(s_{12}, s_{23}) = \bar{\mathcal{A}}_j(s_{12}, s_{23})$$

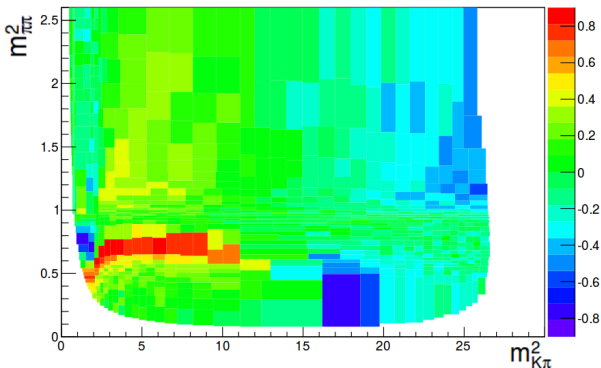
c_j and \bar{c}_j contains weak and strong phases.

$$A_{CP} = \frac{|\bar{c}_j|^2 - |c_j|^2}{|\bar{c}_j|^2 + |c_j|^2}$$

Asymmetry Map from Mirandizing Method

Phys.Rev.D 86,036005(2012).

I.Bediaga, J.Miranda, A.C.dosReis, I.I.Bigi, A.Gomes, J.M.Otalora Goicochea, and A.Veiga.

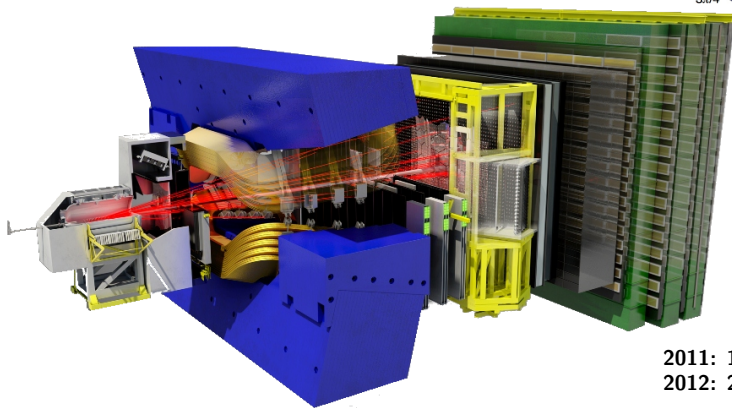
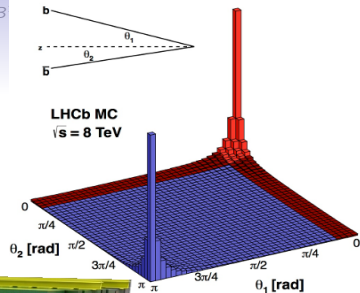


- Histogram performed by an adaptive binning algorithm.
- Each bin contains the same number of events.
- The asymmetry was calculated from the events inside the bin.
- The vertical color scale tells us the asymmetry value.

LHCb Experiment

The LHCb Detector

- Single-arm forward spectrometer ($2 < \eta < 5$),
- Designed to study particles containing b and c quarks
- Includes a High precision tracking system
- Ring Imaging Cherenkov Detectors (charged hadrons)
- Calorimeter System (photons, electrons and hadrons)
- Muon System, interleaved layers of iron and MWPC (muons)



2011: 1 fb^{-1} , $\sqrt{s} = 7 \text{ TeV}$
 2012: 2 fb^{-1} , $\sqrt{s} = 8 \text{ TeV}$

The LHCb Detector

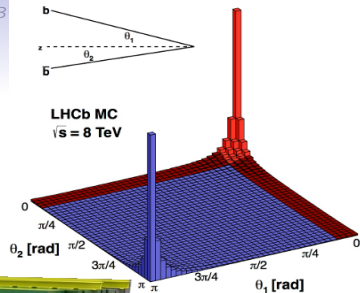
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Vertex
Detector

Magnet

Tracking Stations

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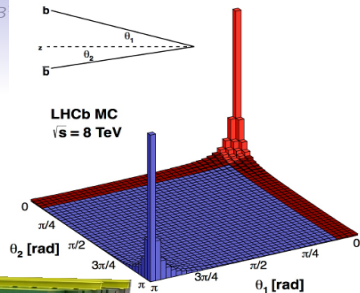
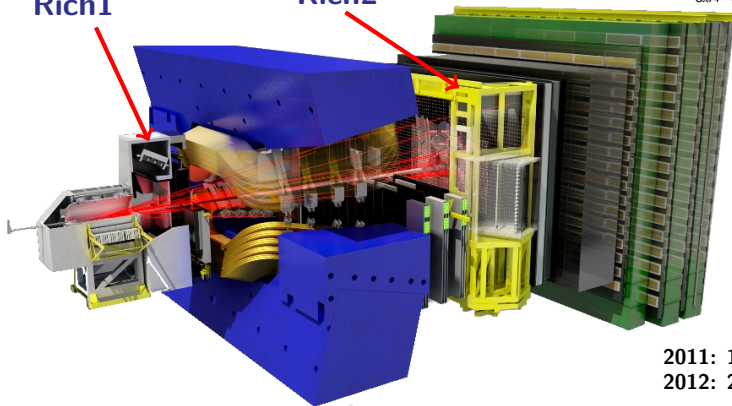
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Rich1

Rich2



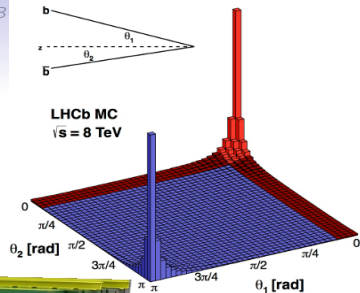
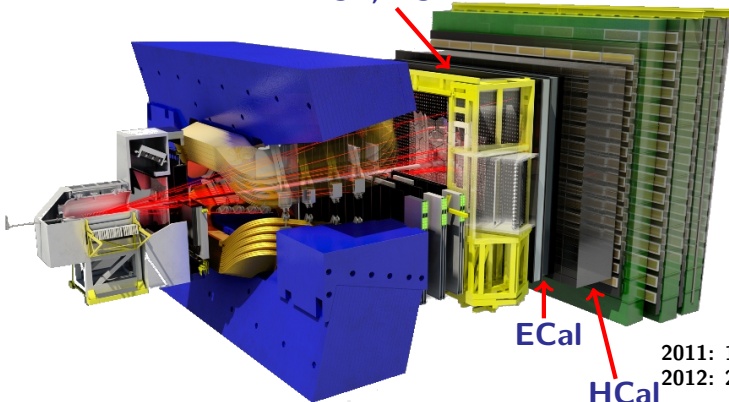
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SP, PS

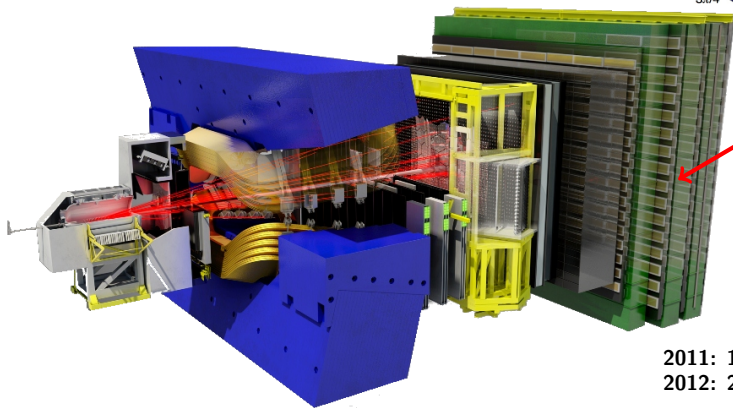
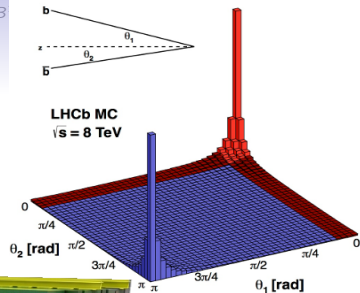


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Muon System

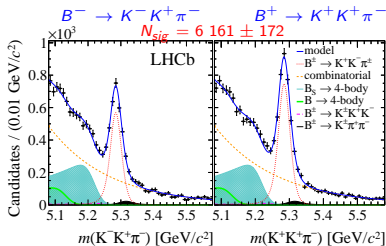
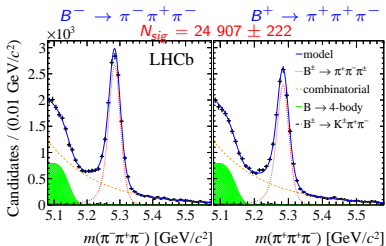
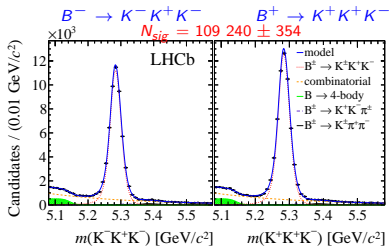
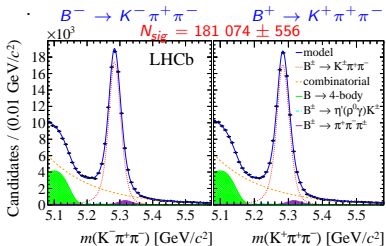
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$$B^\pm \rightarrow h^+ h^- h^\pm \text{ decays.}$$

Inclusive CP asymmetry [arXiv:1408.5373]

Measurement of the raw CP asymmetry from simultaneous mass fit to B^+ and B^- candidates:

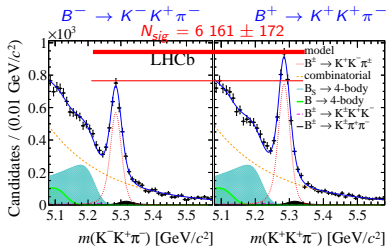
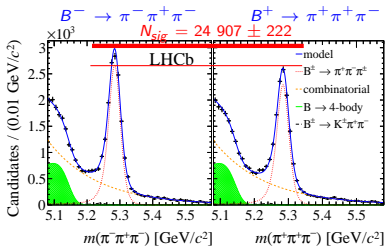
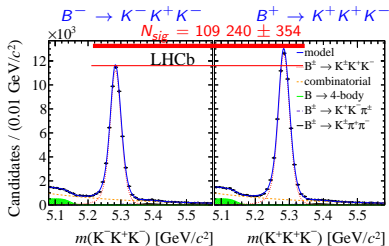
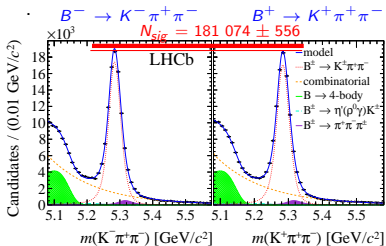
$$\mathcal{A}_{raw} = \frac{N_{B^-} - N_{B^+}}{N_{B^-} + N_{B^+}}$$



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- The raw asymmetry has to be corrected for the B-meson **production asymmetry** and the **detector asymmetry** :

$$\mathcal{A}_{raw} \approx \mathcal{A}_{CP} + \mathcal{A}_P + \mathcal{A}_D^{h'}$$

- Decays divided into two categories depending on the flavour of the unpaired hadron:

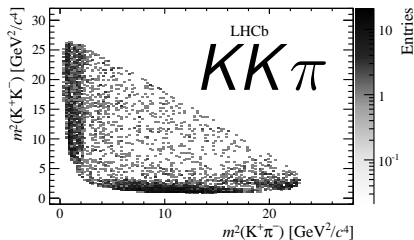
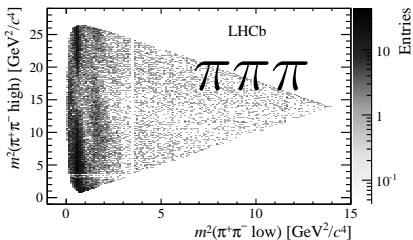
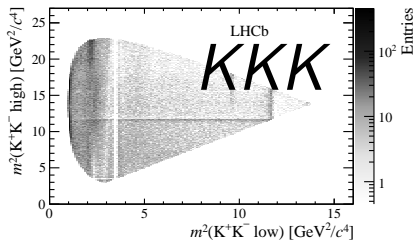
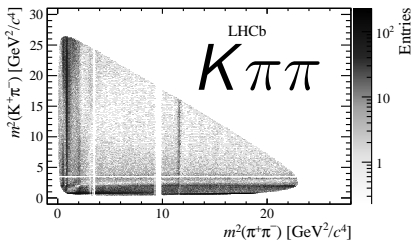
$$\begin{aligned} B^\pm \rightarrow h^+ h^- K^\pm & \quad \mathcal{A}_{CP} = \mathcal{A}_{raw} - \mathcal{A}_P(B^\pm) - \mathcal{A}_D(K^\pm) \\ B^\pm \rightarrow h^+ h^- \pi^\pm & \quad \mathcal{A}_{CP} = \mathcal{A}_{raw} - \mathcal{A}_P(B^\pm) - \mathcal{A}_D(\pi^\pm) \end{aligned}$$

- $\mathcal{A}_P(B)$ from $B \rightarrow J/\psi(\mu\mu)K$ studies and using $\mathcal{A}_D(K) = (-0.126 \pm 0.018)\%$ [PRL 108 (2012) 201601]
- $\mathcal{A}_D(\pi) = (0.00 \pm 0.25)\%$ from studies of prompt D^* decays [PLB 713 (2012) 186]
- Acceptance correction** to take into account non uniformity of efficiencies and raw asymmetries in the phase space

$A_{CP}(B^\pm \rightarrow K^\pm \pi^+ \pi^-)$	$= +0.025 \pm 0.004$ (stat) ± 0.004 (syst) ± 0.007 ($J/\psi K^\pm$)	2.8σ
$A_{CP}(B^\pm \rightarrow K^\pm K^+ K^-)$	$= -0.036 \pm 0.004$ (stat) ± 0.002 (syst) ± 0.007 ($J/\psi K^\pm$)	4.3σ
$A_{CP}(B^\pm \rightarrow \pi^\pm \pi^+ \pi^-)$	$= +0.058 \pm 0.008$ (stat) ± 0.009 (syst) ± 0.007 ($J/\psi K^\pm$)	4.2σ
$A_{CP}(B^\pm \rightarrow \pi^\pm K^+ K^-)$	$= -0.123 \pm 0.017$ (stat) ± 0.012 (syst) ± 0.007 ($J/\psi K^\pm$)	5.6σ

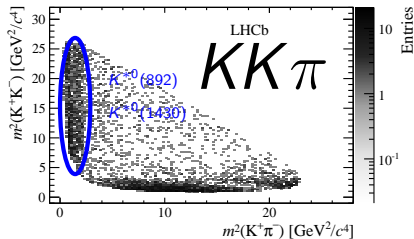
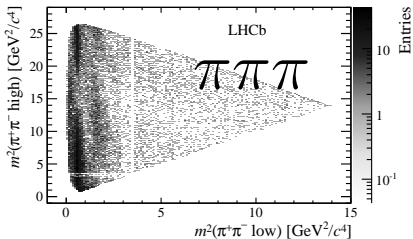
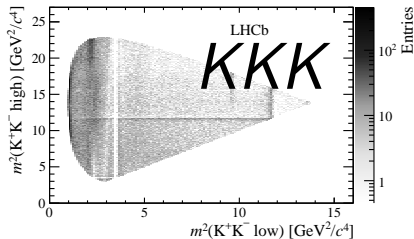
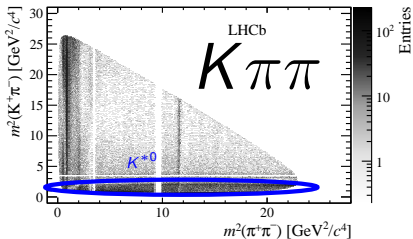
Dalitz Plot [\[arXiv:1408.5373\]](https://arxiv.org/abs/1408.5373)

Dalitz plots in the signal region with bkg: $\pm 34 \text{ MeV}/c^2$ (hhh and hhK), $\pm 17 \text{ MeV}/c^2$ (πKK)



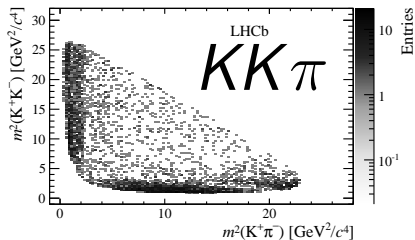
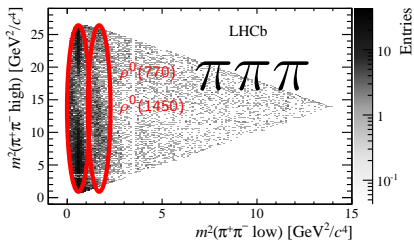
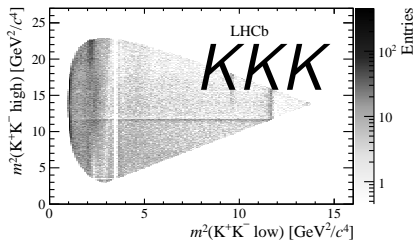
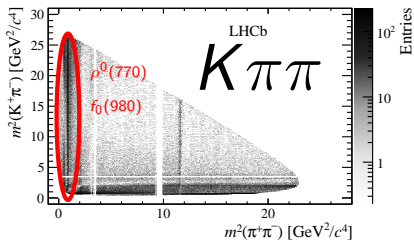
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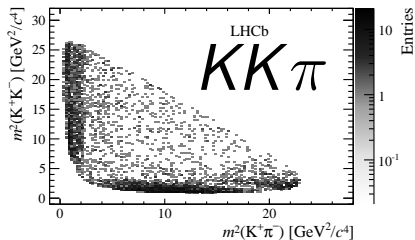
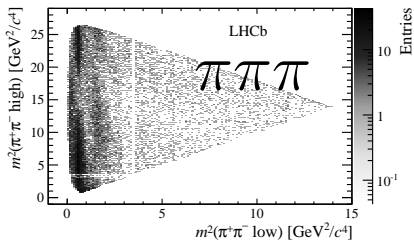
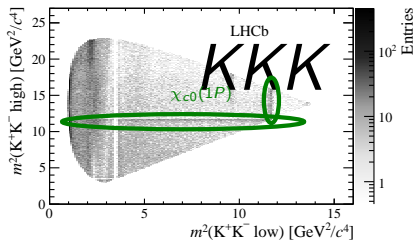
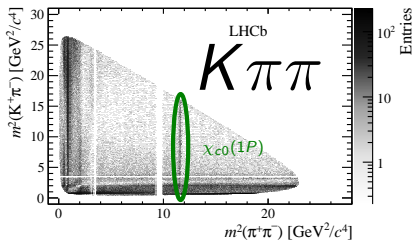
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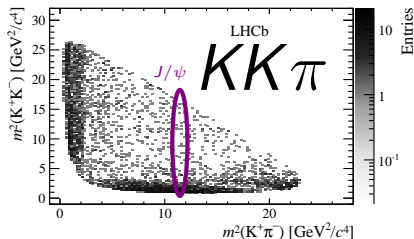
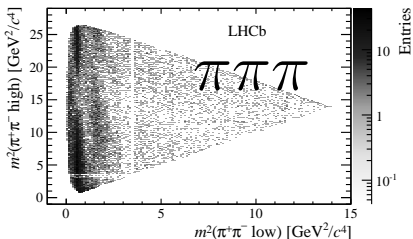
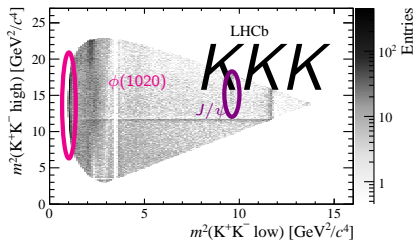
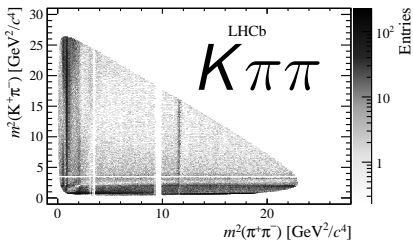
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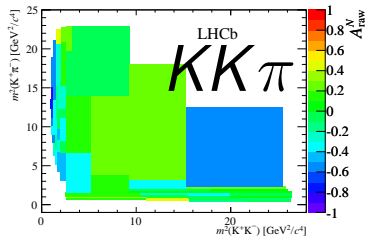
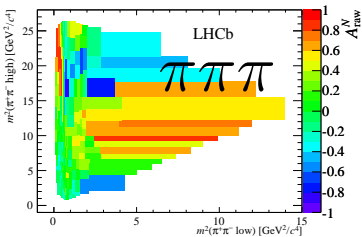
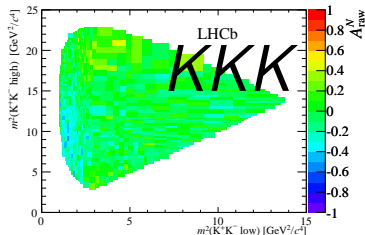
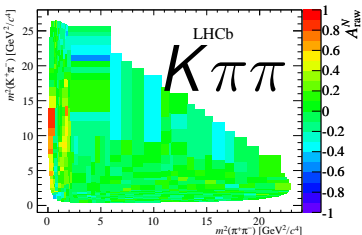
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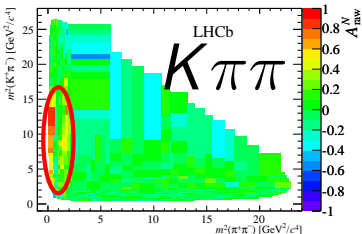
CP asymmetries in the phase space [arXiv:1408.5373]

- Also background subtracted (SPlot) and efficiency corrected

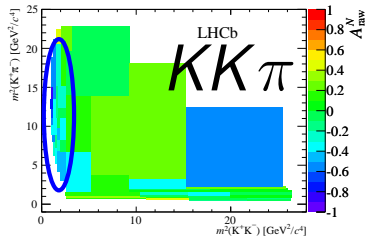
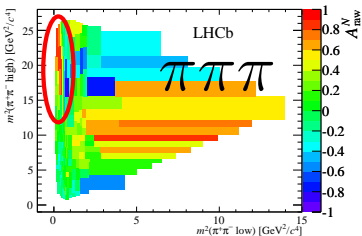
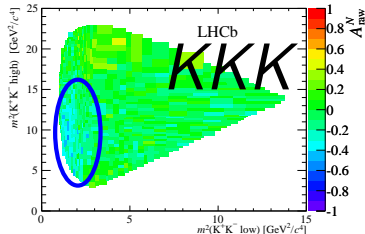


CP asymmetries in the phase space [arXiv:1408.5373]

Large **asymmetries** at low $m_{\pi\pi}^2$

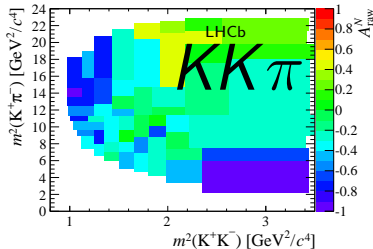
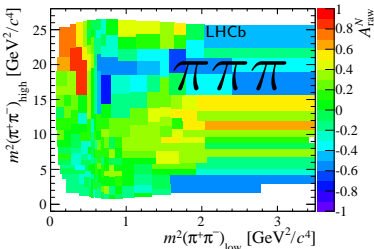
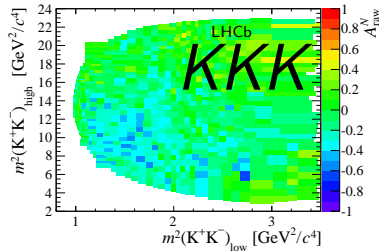
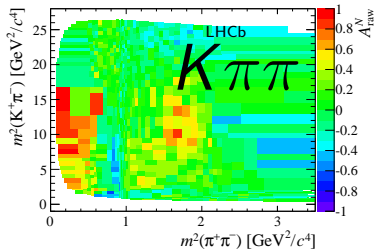


Large **asymmetries** at low m_{KK}^2



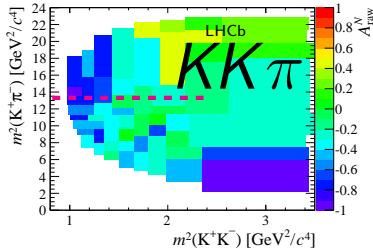
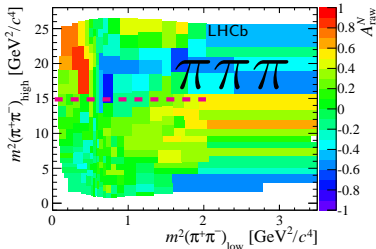
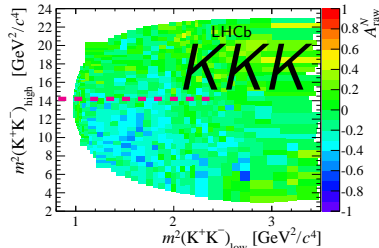
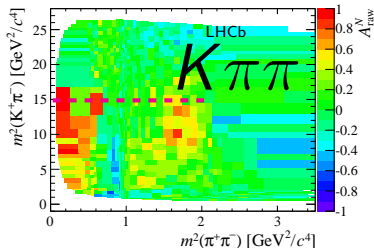
Interference

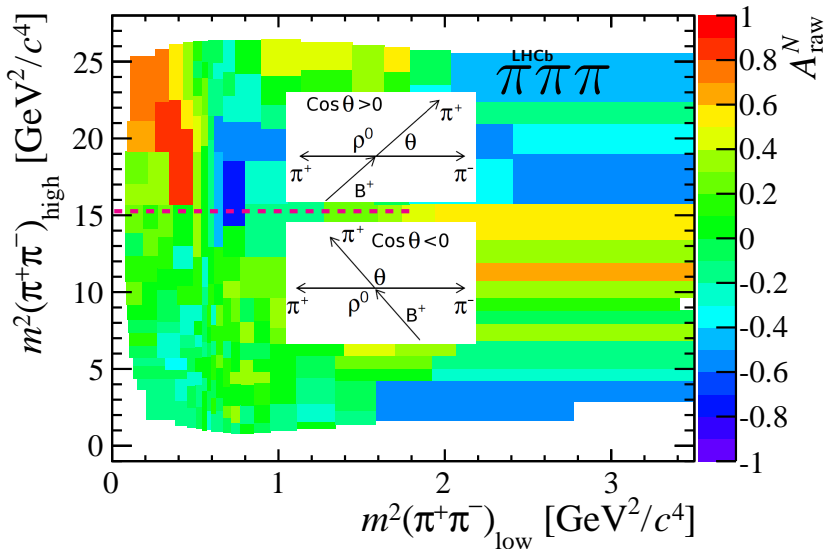
- Zoom at low mass region. Asymmetry is more evident.



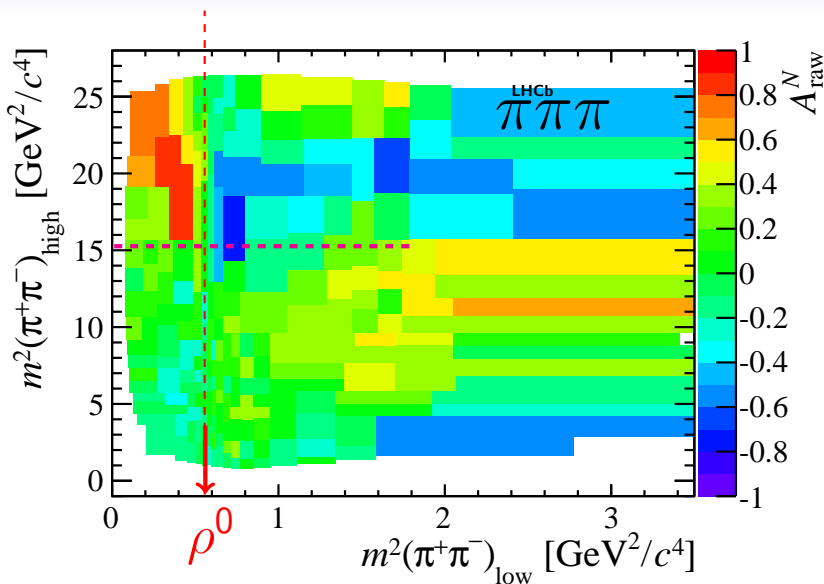
Interference

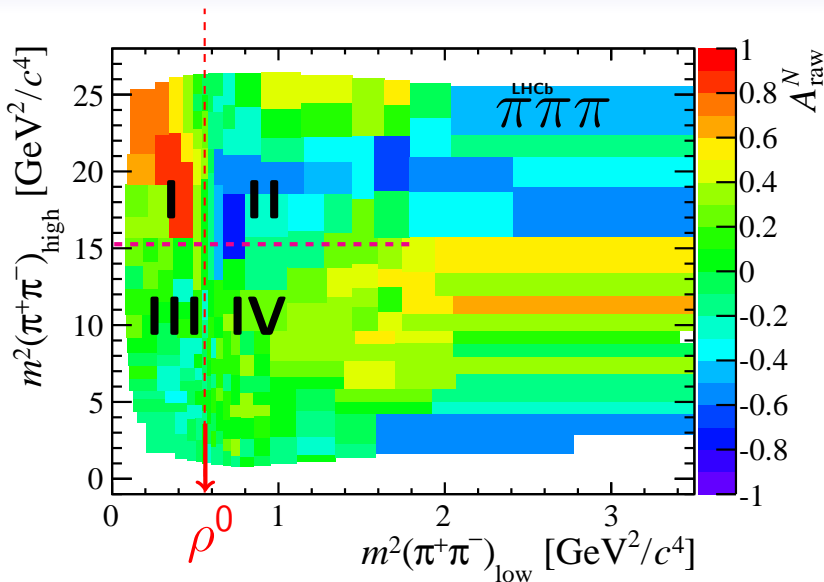
- The behavior of all channels change at middle of the vertical range



Interference: $B^\pm \rightarrow \pi^+ \pi^- \pi^\pm$ 

Interference: $B^\pm \rightarrow \pi^+ \pi^- \pi^\pm$

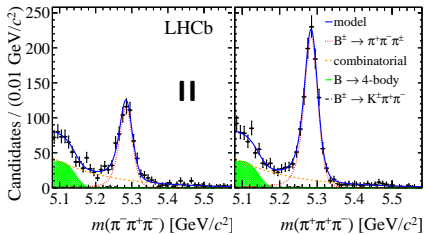
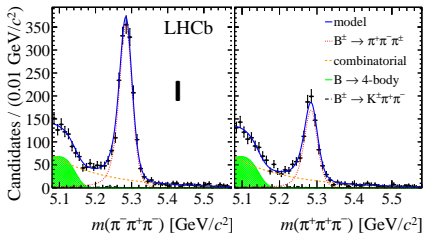
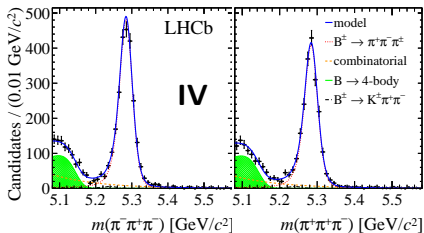
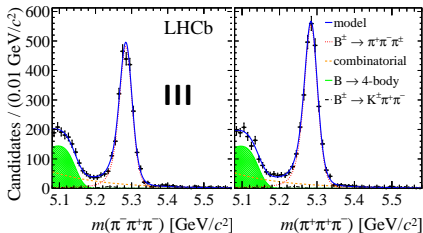


Interference: $B^\pm \rightarrow \pi^+ \pi^- \pi^\pm$ 

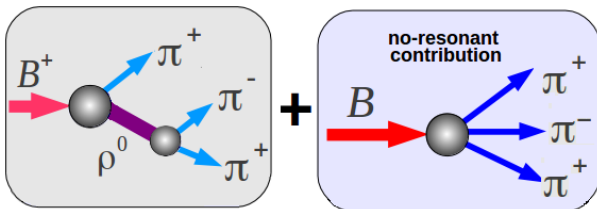
Interference: $B^{\pm} \rightarrow \pi^+ \pi^- \pi^{\pm}$

$$0.47 < m_{\pi\pi\text{low}} \text{ GeV}/c^2 < 0.77$$

$$0.77 < m_{\pi\pi\text{low}} \text{ GeV}/c^2 < 0.92$$

 $\cos\theta > 0$

 $\cos\theta < 0$


Interference: $B^\pm \rightarrow \pi^+ \pi^- \pi^\pm$ (Simple Isobar Model)



$$B^+: \quad \mathcal{A}_+ = A_+^\rho e^{i\Phi_+^\rho} F_\rho^{BW} \cos \theta + A_+^{nr} e^{i\Phi_+^{nr}} F_{nr}$$

$$B^-: \quad \mathcal{A}_- = A_-^\rho e^{i\Phi_-^\rho} F_\rho^{BW} \cos \theta + A_-^{nr} e^{i\Phi_-^{nr}} F_{nr}$$

The phase (Φ) contains the weak (ϕ) and strong (δ) phases.

$$F_\rho^{BW} = \frac{1}{m_\rho^2 - s - im_\rho \Gamma_\rho(s)} \quad F_{nr} = 1$$

Interference: $B^\pm \rightarrow \pi^+ \pi^- \pi^\pm$ (Simple Isobar Model)

- Diference of magnitudes
(Short Distance Effect)

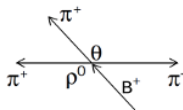
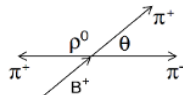
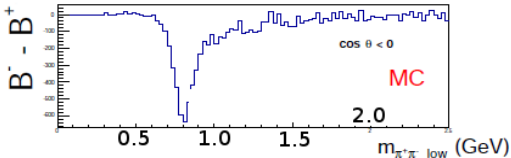
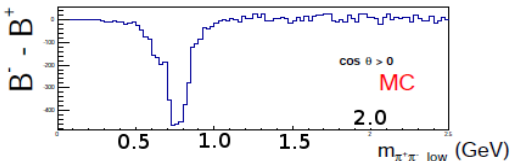
$$\Delta |\mathcal{A}_+|^2 = |\mathcal{A}_+|^2 - |\mathcal{A}_-|^2 = [(A_+^\rho)^2 - (A_-^\rho)^2] |F_\rho^{BW}|^2 \cos^2 \theta + [(A_+^{nr})^2 - (A_-^{nr})^2] |F_{nr}|^2 + 2 \cos \theta |F_\rho^{BW}|^2 |F_{nr}| \{ (m_\rho^2 - s) [A_+^\rho A_+^{nr} \cos(\Phi_+^\rho - \Phi_+^{nr}) - A_-^\rho A_-^{nr} \cos(\Phi_-^\rho - \Phi_-^{nr})] - m_\rho \Gamma_\rho [A_+^\rho A_+^{nr} \sin(\Phi_+^\rho - \Phi_+^{nr}) - A_-^\rho A_-^{nr} \sin(\Phi_-^\rho - \Phi_-^{nr})] \}$$

- Real part of the BW
(Long Distance Effect)
- Imag part of the BW
(Long Distance Effect)

Interference: $B^\pm \rightarrow \pi^+ \pi^- \pi^\pm$ (Simple Isobar Model)

Monte Carlo simulation for the short distance term:

$$\begin{aligned} \mathcal{A}_{CP} \propto & [(A_+^\rho)^2 - (A_-^\rho)^2] |F_\rho^{BW}|^2 \cos^2 \theta + \dots \\ & - 2(m_\rho^2 - s) |F_\rho^{BW}|^2 |F_{nr}|^2 \cos \theta \dots \\ & + 2m_\rho \Gamma_\rho |F_\rho^{BW}|^2 |F_{nr}|^2 \cos \theta \dots \end{aligned}$$



- If it were the dominant term, we should see a peak at the ρ mass.
- The peak should have the same sign for $\cos \theta > 0$ and for $\cos \theta < 0$

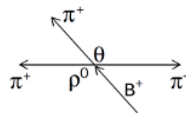
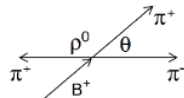
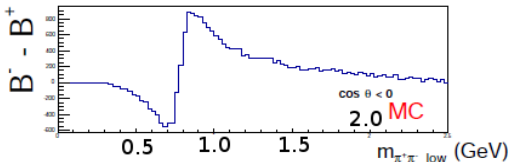
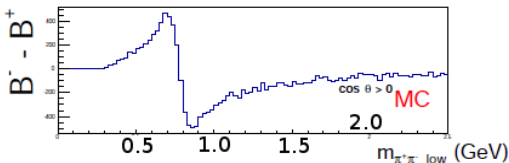
Interference: $B^\pm \rightarrow \pi^+ \pi^- \pi^\pm$ (Simple Isobar Model)

Monte Carlo simulation for the long distance term (Re BW):

$$\mathcal{A}_{CP} \propto [(A_+^\rho)^2 - (A_-^\rho)^2] |F_\rho^{BW}|^2 \cos^2 \theta + \dots$$

$$-2(m_\rho^2 - s) |F_\rho^{BW}|^2 |F_{nr}|^2 \cos \theta \dots$$

$$+2m_\rho \Gamma_\rho |F_\rho^{BW}|^2 |F_{nr}|^2 \cos \theta \dots$$

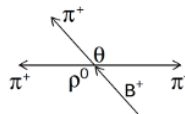
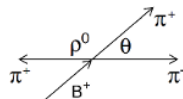
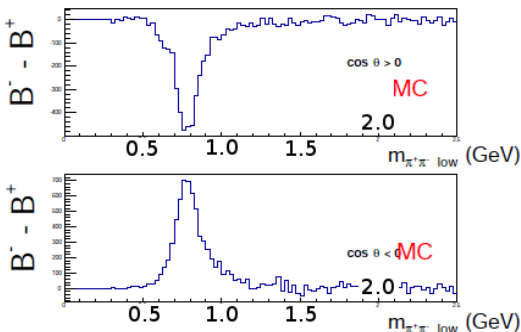


- In this case, we should see an interferent pattern with asymmetry zero at the ρ mass.
- For $\cos \theta > 0$ the asymmetry is (+) below the ρ mass and (-) above.
- For $\cos \theta < 0$ the behaviour is opposite.

Interference: $B^\pm \rightarrow \pi^+ \pi^- \pi^\pm$ (Simple Isobar Model)

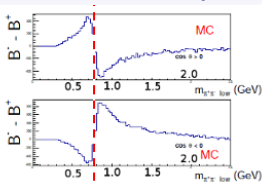
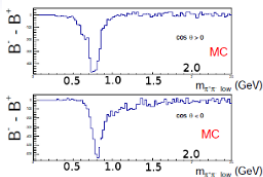
Monte Carlo simulation for the long distance term (Im BW):

$$\begin{aligned} \mathcal{A}_{CP} \propto & [(A_+^\rho)^2 - (A_-^\rho)^2] |F_\rho^{BW}|^2 \cos^2 \theta + \dots \\ & - 2(m_\rho^2 - s) |F_\rho^{BW}|^2 |F_{nr}|^2 \cos \theta \dots \\ & + 2m_\rho \Gamma_\rho |F_\rho^{BW}|^2 |F_{nr}|^2 \cos \theta \dots \end{aligned}$$

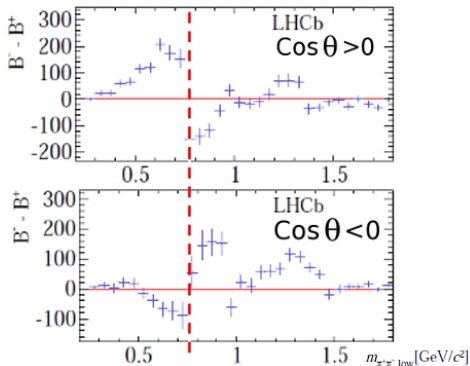
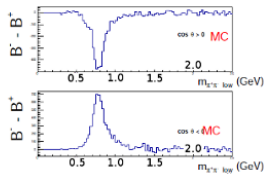


- In this case, also we should see a peak at the ρ mass.
- But the peak has opposite sign for $\cos \theta > 0$ and $\cos \theta < 0$.

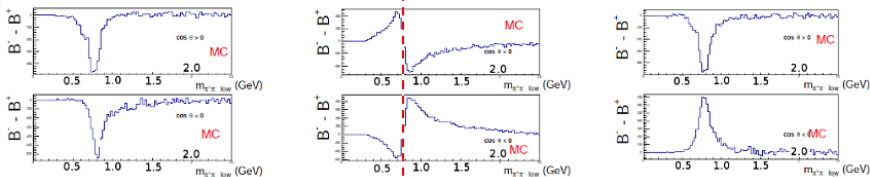
Interference: $B^{\pm} \rightarrow \pi^{+}\pi^{-}\pi^{\pm}$ (Simple Isobar Model)



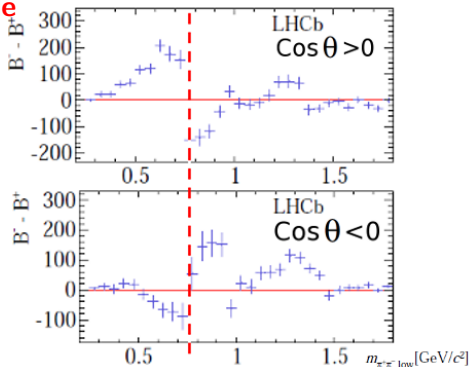
Long distance term (Re BW)



Interference: $B^{\pm} \rightarrow \pi^{+}\pi^{-}\pi^{\pm}$ (Simple Isobar Model)

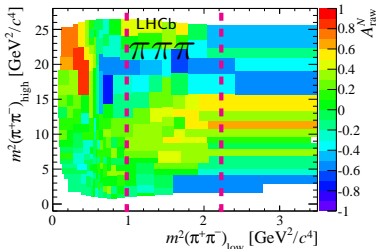
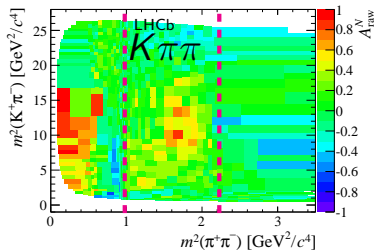


Long-distance effects
play an important role
generating strong
phase.

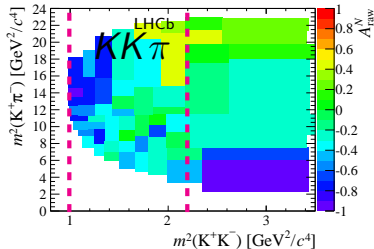
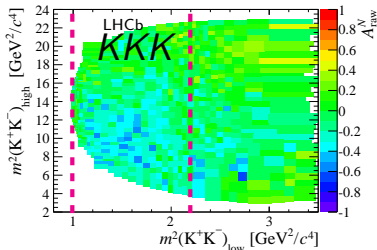


Rescattering $\pi\pi \rightarrow KK$

Large asymmetries: $1 < m_{\pi\pi} < 1.5$



Large asymmetries: $1 < m_{KK} < 1.5$

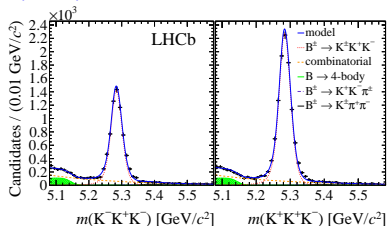
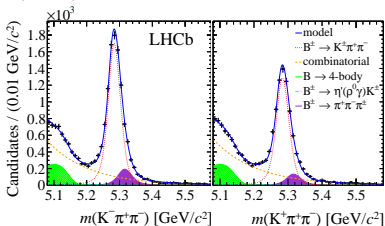


Rescattering $\pi\pi \rightarrow KK$

Invariant masses with $\pi\pi$ and KK in the "rescattering region": $(1.0 - 1.5) \text{ GeV}/c^2$

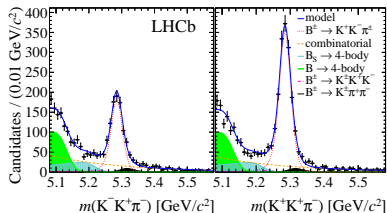
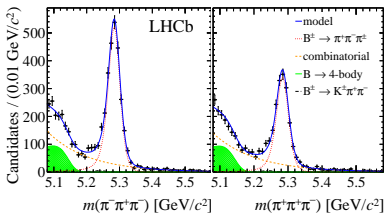
$$A_{CP}(K\pi\pi) = +0.121 \pm 0.012 \pm 0.017 \pm 0.007$$

$$A_{CP}(KKK) = -0.211 \pm 0.011 \pm 0.004 \pm 0.007$$



$$A_{CP}(\pi\pi\pi) = +0.172 \pm 0.021 \pm 0.015 \pm 0.007$$

$$A_{CP}(\pi KK) = -0.328 \pm 0.028 \pm 0.029 \pm 0.007$$



All the asymmetries have more than 5σ of significance

Scattering and CPT constraint

High local asymmetries not obviously associated to resonances.

positive for $K^\pm \pi^+ \pi^-$

negative for $K^\pm K^+ K^-$

positive for $\pi^+ \pi^- \pi^\pm$

negative for $K^+ K^- \pi^\pm$

$$\sum_{f_\alpha^{(i)} \in F_i} \Gamma(P \rightarrow f_\alpha^{(i)}) = \sum_{\bar{f}_\alpha^{(i)} \in \bar{F}_i} \Gamma(\bar{P} \rightarrow \bar{f}_\alpha^{(i)}) \quad (\text{Bigi \& Sunda 2nd edition pp 57})$$

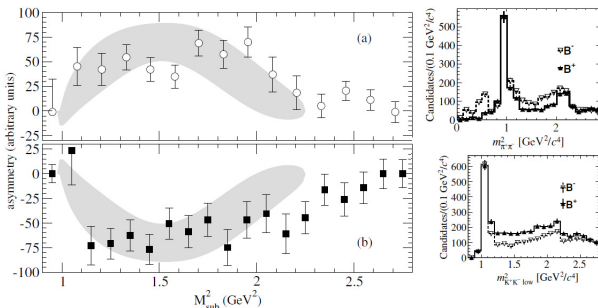
all f_α in F_i connected via strong interactions

for two modes $\pi\pi$ and KK : $\Gamma(A_{\pi\pi}^+) + \Gamma(A_{KK}^+) = \Gamma(A_{\pi\pi}^-) + \Gamma(A_{KK}^-)$, then:

$$\Delta\Gamma_{\pi\pi} = -\Delta\Gamma_{KK}$$

I.Bediaga, T.Frederico, O.Lourenço, Phys.Rev.D 89,094013 (2014)

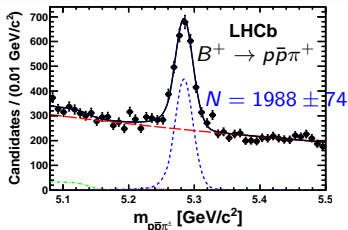
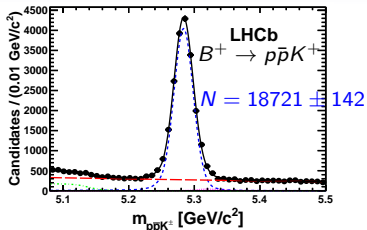
$\Delta\Gamma_{KK} = (\sin\gamma)\sqrt{1 - \eta^2 \cos(\delta_{KK} + \delta_{\pi\pi} + \Phi)} F(M_{KK}^2)$ (Inelasticity and Unitarity)



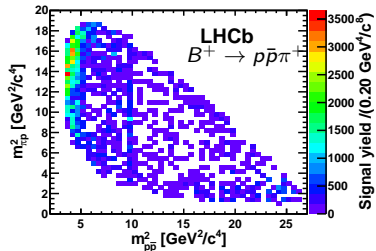
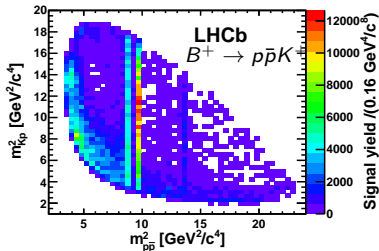
$$B^\pm \rightarrow p\bar{p}h^\pm \text{ decays.}$$

$B^\pm \rightarrow p\bar{p}h^\pm$ decays

- Yields extracted with an unbinned maximum likelihood fit



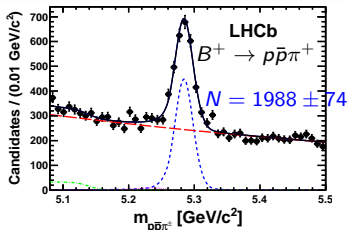
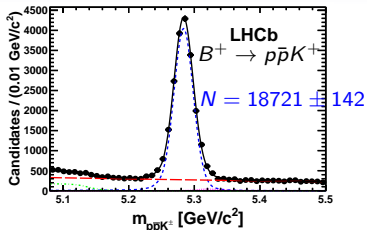
- Background subtracted Dalitz distributions using sPlot technique



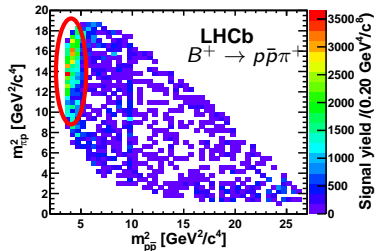
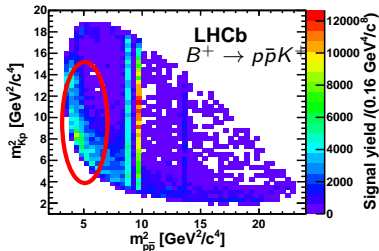
- **At low $m_{p\bar{p}}^2$** invariant mass the behaviour is differently distributed in the two modes
- **Charmonium bands** clearly visible: $J\psi$, $\psi(2S)$ and η_c
- **At low m_{pk}^2** invariant mass we see $\Lambda(1520)$

$B^\pm \rightarrow p\bar{p}h^\pm$ decays

- Yields extracted with an unbinned maximum likelihood fit



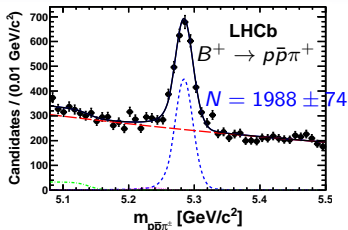
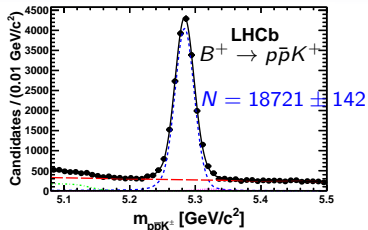
- Background subtracted Dalitz distributions using sPlot technique



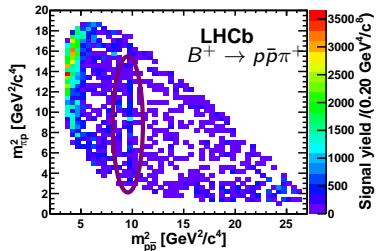
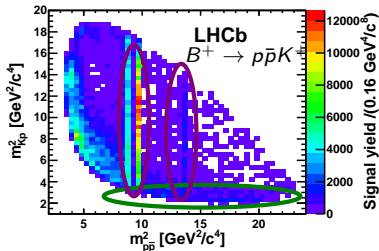
- **At low $m_{p\bar{p}}^2$** invariant mass the behaviour is differently distributed in the two modes
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- **At low m_{pk}^2** invariant mass we see $\Lambda(1520)$

$B^\pm \rightarrow p\bar{p}h^\pm$ decays

- Yields extracted with an unbinned maximum likelihood fit



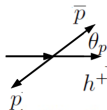
- Background subtracted Dalitz distributions using sPlot technique



- **At low $m_{p\bar{p}}^2$** invariant mass the behaviour is differently distributed in the two modes
- **Charmonium bands** clearly visible: $J\psi$, $\psi(2S)$ and η_c
- **At low m_{pk}^2** invariant mass we see $\Lambda(1520)$

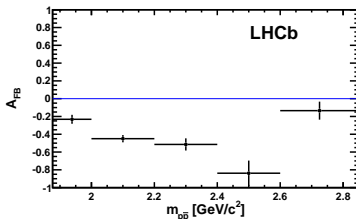
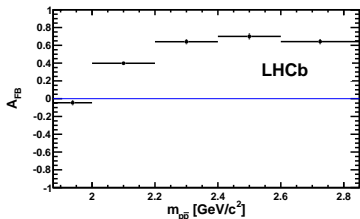
$B^\pm \rightarrow p\bar{p}h^\pm$ decays: Dynamics

- Measurement of the forward-backward asymmetry



$$A_{FB} = \frac{N(\cos\theta_p > 0) - N(\cos\theta_p < 0)}{N(\cos\theta_p > 0) + N(\cos\theta_p < 0)}$$

- Variation of the A_{FB} as a function of $m_{p\bar{p}}$



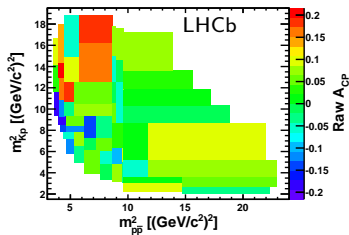
- Opposite behaviour for the two decay modes

$$A_{FB}(p\bar{p}K^+, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2) = 0.495 \pm 0.012(\text{stat}) \pm 0.007(\text{syst})$$

$$A_{FB}(p\bar{p}\pi^+, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2) = -0.409 \pm 0.033(\text{stat}) \pm 0.006(\text{syst})$$

$B^\pm \rightarrow p\bar{p}h^\pm$ decays: CP asymmetries

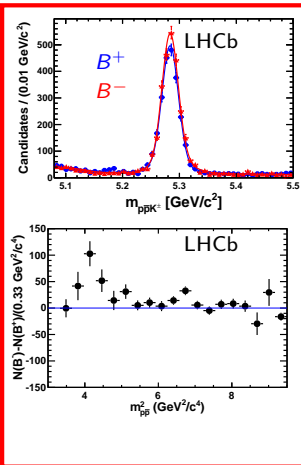
- Variation of A_{CP} as a function of the Dalitz-plot variables only for $B^\pm \rightarrow p\bar{p}K^\pm$
- Adaptive binning analysis



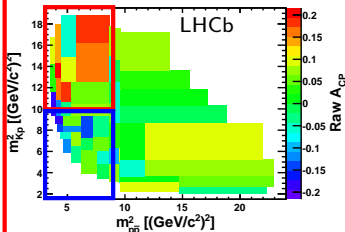
$B^\pm \rightarrow p\bar{p}h^\pm$ decays: CP asymmetries

- Variation of A_{CP} as a function of the Dalitz-plot variables only for $B^\pm \rightarrow p\bar{p}K^\pm$
- Adaptive binning analysis

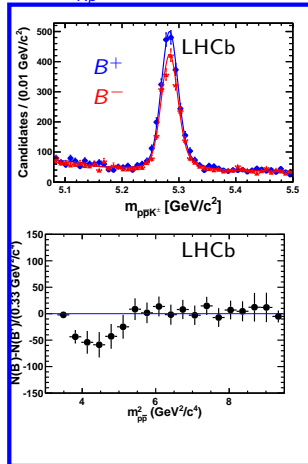
$$m_{Kp}^2 > 10 \text{ GeV}^2/c^4$$



Clear sign-flip pattern at low $m_{p\bar{p}}^2$



$$m_{Kp}^2 < 10 \text{ GeV}^2/c^4$$



$B^\pm \rightarrow p\bar{p}h^\pm$ decays: CP asymmetries

- The raw CP is corrected for production and detection asymmetries as in $B^\pm \rightarrow h^+ h^- h^\pm$ decays.

$$\begin{aligned} B^\pm \rightarrow p\bar{p}K^\pm & \quad \mathcal{A}_{CP} = \mathcal{A}_{raw} - \mathcal{A}_P(B^\pm) - \mathcal{A}_D(K^\pm) \\ B^\pm \rightarrow p\bar{p}\pi^\pm & \quad \mathcal{A}_{CP} = \mathcal{A}_{raw} - \mathcal{A}_P(B^\pm) - \mathcal{A}_D(\pi^\pm) \end{aligned}$$

First evidence of CPV in baryonic B decays

Mode/region	\mathcal{A}_{CP}	
$\eta_c(\rightarrow p\bar{p})K^\pm$	0.040 ± 0.034 (stat) ± 0.004 (syst)	
$\psi(2S)(\rightarrow p\bar{p})K^\pm$	0.092 ± 0.058 (stat) ± 0.004 (syst)	
$p\bar{p}K^\pm, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2$	0.021 ± 0.020 (stat) ± 0.004 (syst)	
$p\bar{p}K^\pm, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2, m_{Kp}^2 < 10 \text{ GeV}^2/c^4$	-0.036 ± 0.023 (stat) ± 0.004 (syst)	
$p\bar{p}K^\pm, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2, m_{Kp}^2 > 10 \text{ GeV}^2/c^4$	0.096 ± 0.024 (stat) ± 0.004 (syst)	4σ
$p\bar{p}K^\pm, m_{p\bar{p}}^2 < 6 \text{ GeV}^2/c^4, m_{Kp}^2 < 10 \text{ GeV}^2/c^4$	-0.066 ± 0.026 (stat) ± 0.004 (syst)	
$p\bar{p}K^\pm, m_{p\bar{p}}^2 < 6 \text{ GeV}^2/c^4, m_{Kp}^2 > 10 \text{ GeV}^2/c^4$	0.087 ± 0.026 (stat) ± 0.004 (syst)	3.5σ
$p\bar{p}\pi^\pm, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2$	-0.041 ± 0.039 (stat) ± 0.005 (syst)	

- Systematics uncertainties dominated by the uncertainty on the $\mathcal{A}_{CP}(J/\psi K)$ measurement

$B^\pm \rightarrow p\bar{p}h^\pm$ decays: B.F. measurements

- Branching fraction of $B^+ \rightarrow \bar{\Lambda}(1520)(K^+\bar{p})p$ relative to $B^+ \rightarrow J/\psi(p\bar{p})K^+$

$$\frac{\mathcal{B}(B^+ \rightarrow \bar{\Lambda}(1520)(K^+\bar{p})p)}{\mathcal{B}(B^+ \rightarrow J/\psi(p\bar{p})K^+)} = \frac{N_{\Lambda \rightarrow Kp}}{N_{J/\psi \rightarrow p\bar{p}}} \times \frac{\epsilon_{J/\psi \rightarrow p\bar{p}}^{gen}}{\epsilon_{\Lambda \rightarrow Kp}^{gen}} \times \frac{\epsilon_{J/\psi \rightarrow p\bar{p}}^{sel}}{\epsilon_{\Lambda \rightarrow Kp}^{sel}}$$

- Similar equation for the ratio $B^+ \rightarrow p\bar{p}\pi^+$ to $B^+ \rightarrow J/\psi(p\bar{p})\pi^+$
- Resonant modes extracted with a 2D fit to $p\bar{p}h^+$ and $p\bar{p}/K^+\bar{p}$

$$\frac{\mathcal{B}(B^+ \rightarrow \bar{\Lambda}(1520)(K^+\bar{p})p)}{\mathcal{B}(B^+ \rightarrow J/\psi(p\bar{p})K^+)} = 0.033 \pm 0.005(stat) \pm 0.007(syst)$$

$$\frac{\mathcal{B}(B^+ \rightarrow p\bar{p}\pi^+, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2)}{\mathcal{B}(B^+ \rightarrow J/\psi(p\bar{p})\pi^+)} = 12.0 \pm 1.2(stat) \pm 0.3(syst)$$

- Using

- $\mathcal{B}(B^+ \rightarrow J/\psi K^+) = (1.016 \pm 0.033) \times 10^{-3}$ [PDG]
- $\mathcal{B}(J/\psi \rightarrow p\bar{p}) = (2.17 \pm 0.07) \times 10^{-3}$ [PDG]
- $\mathcal{B}(\Lambda(1520) \rightarrow K^+\bar{p}) = 0.234 \pm 0.016$ [Eur.Phys.J. A47(2011)133]

$$\mathcal{B}(B^+ \rightarrow \bar{\Lambda}(1520)(K^+\bar{p})p) = (3.15 \pm 0.48(stat) \pm 0.07(syst) \pm 0.26(BF)) \times 10^{-7}$$

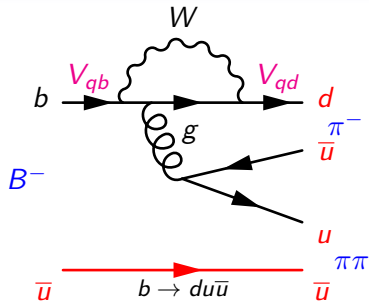
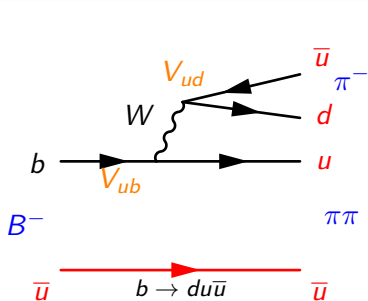
$$\mathcal{B}(B^+ \rightarrow p\bar{p}\pi^+, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2) = (1.07 \pm 0.11(stat) \pm 0.03(syst) \pm 0.11(BF)) \times 10^{-6}$$

Summary

- **New results with the full LHCb data set ($3fb^{-1}$)**
- $B^\pm \rightarrow h^+ h^- h^\pm$ decays
 - **Evidence of global direct CP violation**
 - **High localised CP asymmetries** across the Dalitz plot
 - **Long-distance effects** play an important role in **generating a strong phase difference**:
 - Interference between resonances.
 - Rescattering.
- $B^\pm \rightarrow p\bar{p}h^\pm$ decays
 - **Large forward-backward asymmetries**
 - **First evidence CP violation in decays involving baryons**
 - **Sign-flip of CP asymmetry probably generated by interference of long-distance $p\bar{p}$ waves**
- **Next Step: Amplitude Analyses.**

BackUp Slides

BSS Model for the $B^\pm \rightarrow \pi^+\pi^-\pi^\pm$ decay

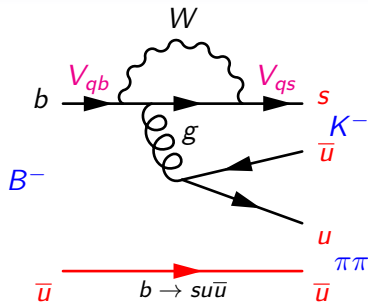
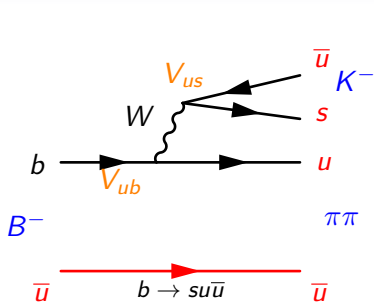


- Strangeness = 0
- Penguin: $q = u, c, t$
- Tree Dominant.
- Different weak phase (CKM mechanism).
- Different strong phase (for u and c in the penguin).

$$\begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \quad (1)$$

$$\begin{bmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A[\lambda^3(1 - \rho - i\eta)] & -A\lambda^2 & 1 \end{bmatrix}, \quad (2)$$

BSS Model for $B^\pm \rightarrow K^\pm \pi^+ \pi^-$ & $B^\pm \rightarrow K^\pm K^+ K^-$ decays



- Strangeness = 1
- Penguin: $q = u, c, t$
- Penguin Dominant.
- CPV expected from interference between tree and penguin diagrams

$$\begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \quad (3)$$

$$\begin{bmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A[\lambda^3(1 - \rho - i\eta)] & -A\lambda^2 & 1 \end{bmatrix}, \quad (4)$$

Amplitude Analysis

Problems in the usual Isobar Model:

- **Many** broad states (**scalars**) squeezed in a **narrow mass window**
- For **D mesons** the **Non-Resonant amplitude** A_0^{NR} is assumed to be **constant** (due to the small phase space), but this is not the case for **B meson** decays.
- **High Non-Resonant** contribution in **B meson** decays.
- In Isobar Model, hard to **disentangle** the **Non-Resonant** and **broad structures** in the **S-Wave**.

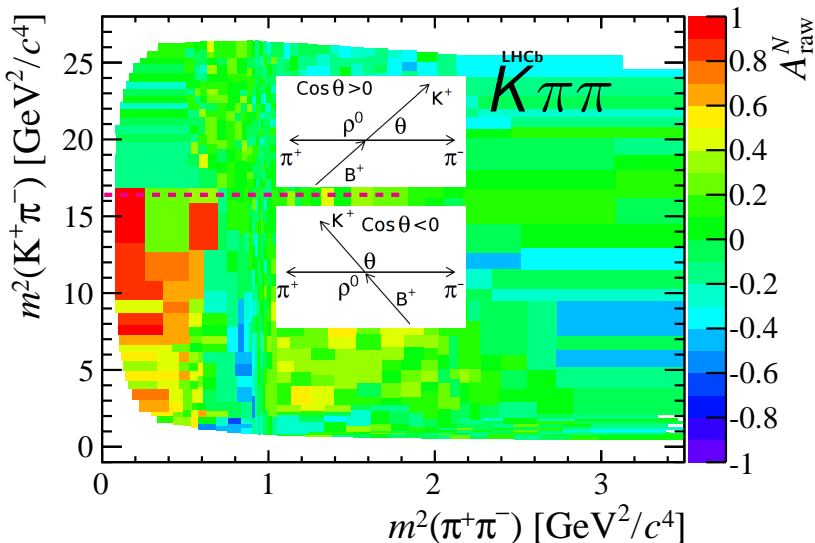
The Partial Wave Analysis:

- This method was developed by **E791 collaboration**. PRD 73, 032004 (2006)

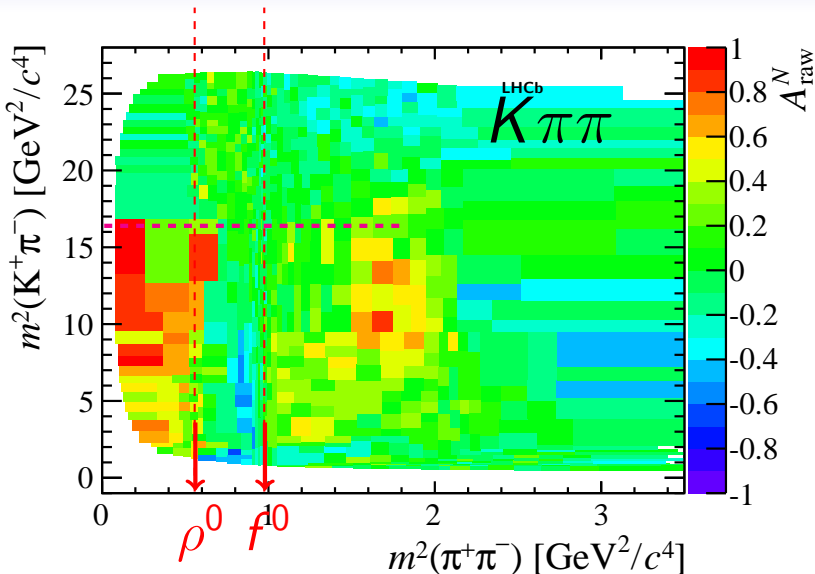
$$\mathcal{A} = \underbrace{S - Wave}_{a_0(s_i) e^{i\phi_0(s_i)}} + \underbrace{P - Wave + D - Wave}_{\text{Isobar Model}} +$$

- The real functions $a_0(s_i)$ and $\phi_0(s_i)$ are **extracted directly from data**.
- **The measurement is inclusive**: convolution of elastic, inelastic scattering, mixed isospin, FSI, etc...
- **Accuracy** depends on the features of **P-(or D-waves)** - an **interferometry analysis**.

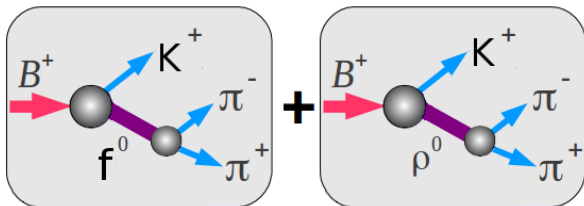
Interference: $B^\pm \rightarrow K^\pm \pi^+ \pi^-$



Interference: $B^\pm \rightarrow K^\pm \pi^+ \pi^-$



Interference: $B^\pm \rightarrow K^\pm \pi^+ \pi^-$ (Simple Isobar Model)



$$\text{B positive } \mathcal{M}_+ = a_+^\rho e^{i\delta_+^\rho} F_\rho^{\text{BW}} \cos \theta + a_+^f e^{i\delta_+^f} F_f^{\text{BW}}$$

$$\text{B negative } \mathcal{M}_- = a_-^\rho e^{i\delta_-^\rho} F_\rho^{\text{BW}} \cos \theta + a_-^f e^{i\delta_-^f} F_f^{\text{BW}}$$

$$F_R^{\text{BW}}(s) = \frac{1}{m_R^2 - s - im_R \Gamma_R(s)} \quad R = \rho, f$$

Interference: $B^\pm \rightarrow K^\pm \pi^+ \pi^-$ (Simple Isobar Model)

$$\begin{aligned}
 |\Delta\mathcal{M}|^2 &= |\mathcal{M}_+|^2 - |\mathcal{M}_-|^2 \\
 &= [(a_+^\rho)^2 - (a_-^\rho)^2] |F_\rho^{\text{BW}}|^2 \cos^2 \theta + [(a_+^f)^2 - (a_-^f)^2] |F_f^{\text{BW}}|^2 + 2 \cos \theta |F_\rho^{\text{BW}}|^2 |F_f^{\text{BW}}|^2 \times \\
 &\quad \{ [(m_\rho^2 - s)(m_f^2 - s) - m_\rho \Gamma_\rho m_f \Gamma_f] [a_+^\rho a_+^f \cos(\delta_+^\rho - \delta_+^f) - a_-^\rho a_-^f \cos(\delta_-^\rho - \delta_-^f)] \\
 &\quad - [m_\rho \Gamma_\rho (m_f^2 - s) - m_f \Gamma_f (m_\rho^2 - s)] [a_+^\rho a_+^f \sin(\delta_+^\rho - \delta_+^f) - a_-^\rho a_-^f \sin(\delta_-^\rho - \delta_-^f)] \}
 \end{aligned}$$

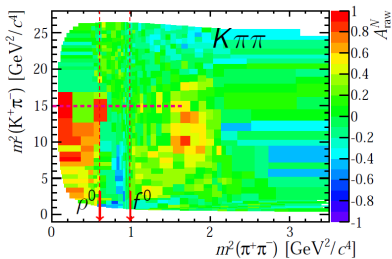
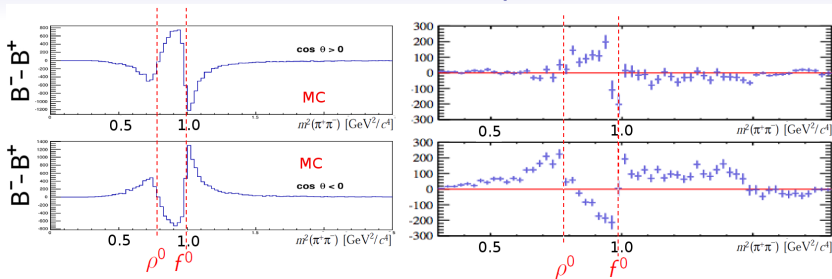
$$[(a_+^\rho)^2 - (a_-^\rho)^2] |F_\rho^{\text{BW}}|^2 \cos^2 \theta + [(a_+^{nr})^2 - (a_-^{nr})^2] |F^{\text{NR}}|^2$$

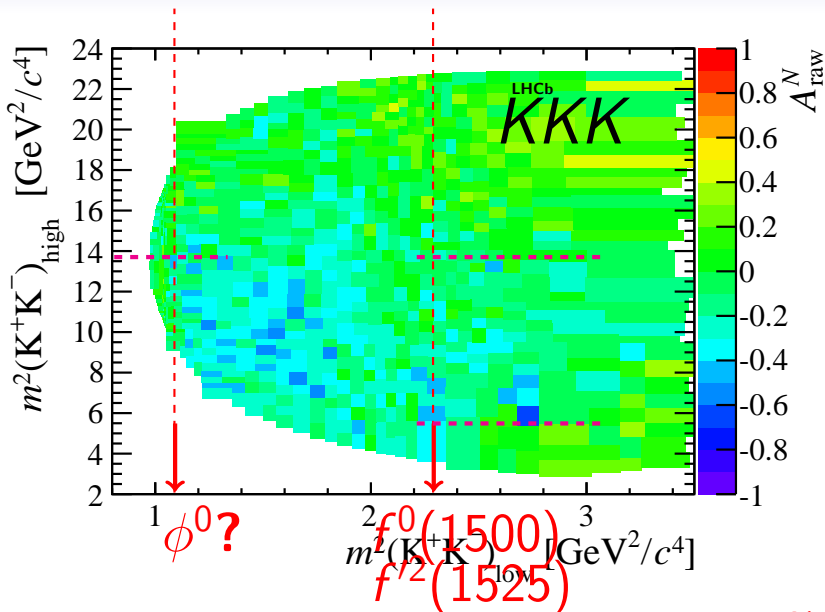
$$2 \cos \theta |F_\rho^{\text{BW}}|^2 |F^{\text{NR}}|^2 \left\{ \begin{array}{l} (m_\rho^2 - s)(m_f^2 - s) - m_\rho \Gamma_\rho m_f \Gamma_f \\ m_\rho \Gamma_\rho (m_f^2 - s) - m_f \Gamma_f (m_\rho^2 - s) \end{array} \right.$$

Long distance interference:
 Real part of Dalitz CP
 asymmetry

Long distance interference:
 Imaginary part of Dalitz CP
 asymmetry

Interference: $B^\pm \rightarrow K^\pm \pi^+ \pi^-$ (Simple Isobar Model)



Interference: $B^\pm \rightarrow K^\pm K^+ K^-$ 

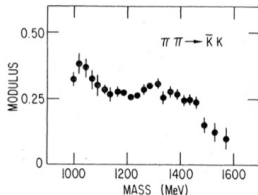
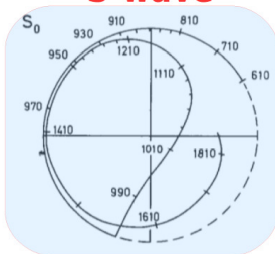
Scattering and CPT constraint

- Scattering:**

CERN-Munich collab: $\pi^+\pi^- \rightarrow \pi^+\pi^-$ **scattering** Nuclear Physics B64 (1973) 134-162

Strongly coupled channels: $\pi^+\pi^- \rightarrow K^+K^-$ PRD 22 (1980) 2595

S-wave



Modulus of the $\pi\pi \rightarrow \bar{K}K$ scattering amplitude $|\mathcal{T}(\pi\pi \rightarrow \bar{K}K)|$ from solution I(b).

- CPT constraint:**

High local asymmetries not obviously associated to resonances.

positive for $K^\pm \pi^+\pi^-$

negative for $K^\pm K^+K^-$

positive for $\pi^+\pi^- \pi^\pm$

negative for $K^+K^- \pi^\pm$

$$\sum_{f_\alpha^{(i)} \in F_i} \Gamma(P \rightarrow f_\alpha^{(i)}) = \sum_{\bar{f}_\alpha^{(i)} \in \bar{F}_i} \Gamma(\bar{P} \rightarrow \bar{f}_\alpha^{(i)}) \quad (\text{Bigi \& Sanda 2nd edition pp 57})$$

all f_α in F_i connected via strong interactions

for two channels α and β : $\Gamma(A_\alpha^+) + \Gamma(A_\beta^+) = \Gamma(A_\alpha^-) + \Gamma(A_\beta^-)$, then: $\Delta\Gamma_\alpha = -\Delta\Gamma_\beta$