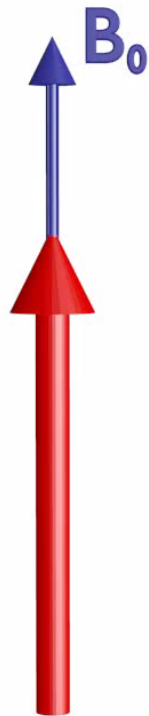


# Magnetization Dynamics II: Magnonics: Trends and Challenges

**Burkard Hillebrands**

Fachbereich Physik and Landesforschungszentrum OPTIMAS,  
Technische Universität Kaiserslautern, Germany

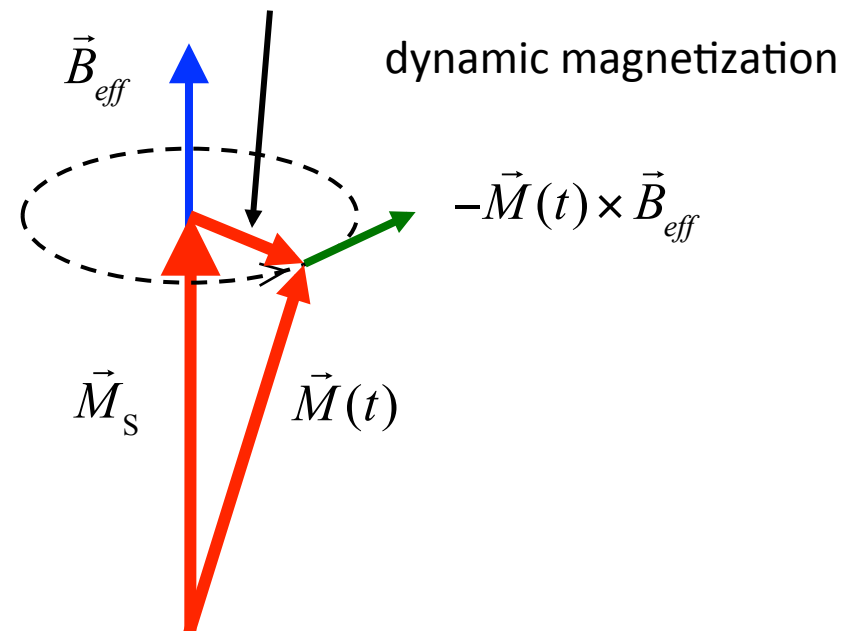
## Spin wave: collective motion of magnetic moments

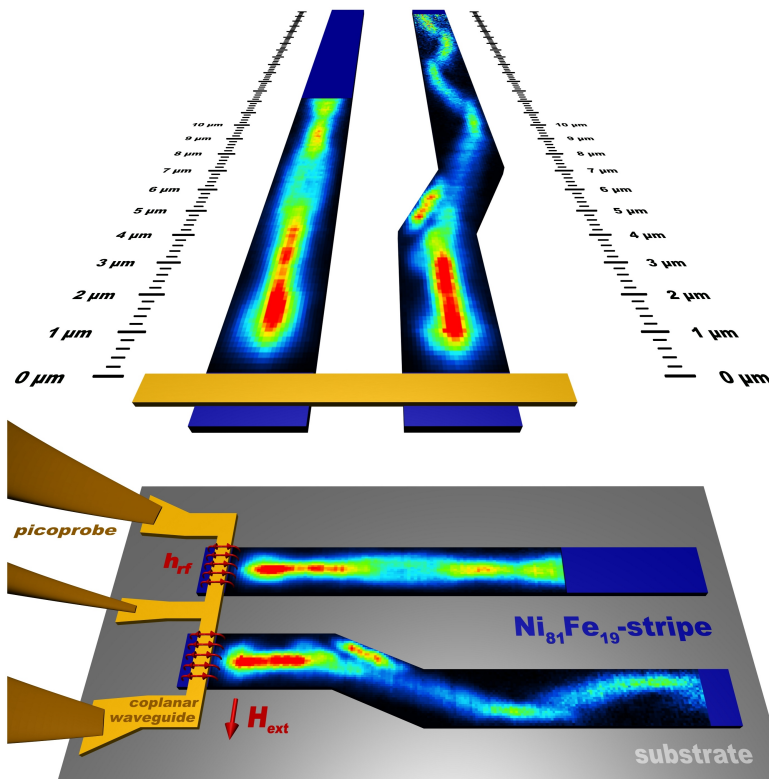


## Landau-Lifshitz torque equation

$$\frac{1}{|\gamma|} \frac{d\vec{M}(t)}{dt} = -\vec{M}(t) \times \vec{B}_{eff}(t) + \frac{\alpha}{M_s} \vec{M}(t) \times \frac{d\vec{M}(t)}{dt}$$

$$\vec{m}(\vec{r}, t) = \vec{m}_0(\vec{r}) \times e^{i(\vec{k}\vec{r} - \omega t)}$$





## Travelling magnons allow one to:

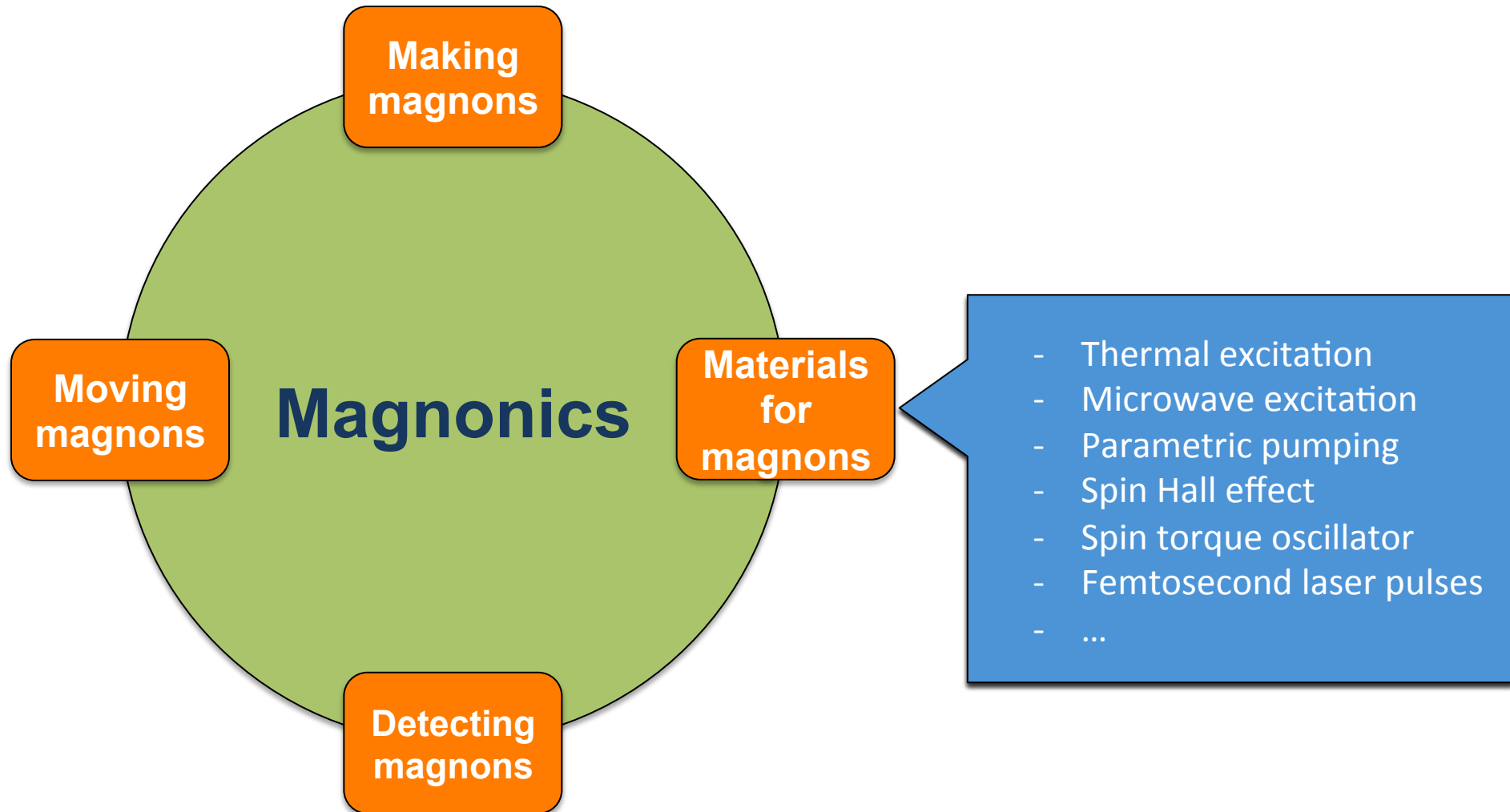
- **transfer** spin information over **centimeter** distances
- **process** the information (using wave nature of magnon)
- **operate** in **insulator**-based technology

## Fundamental properties:

- Minimal wavelength is down to **several nm**
- Frequency is in GHz and up to the **THz range**
- **Energy:**  $E_{\text{magnon}} \ll k_B T$
- **Lifetime:** up to several 100 ns

Making  
magnons

**Magnonics**



## Kaiserslautern PI Team



**A. Chumak**



**V. Vasyuchka**



**A. Serga**



**B. Leven**

## Main External Collaborators

**Y. Ando, E. Saitoh** (Tohoku University, Sendai, Japan)

**G.A. Melkov** (National Taras Shevchenko University of Kiev, Ukraine)

**A.N. Slavin** (University of Rochester, Michigan, U.S.A.)

**A. Karenowska** (Oxford University, U.K.)

**M. Kostylev** (University of Western Australia)



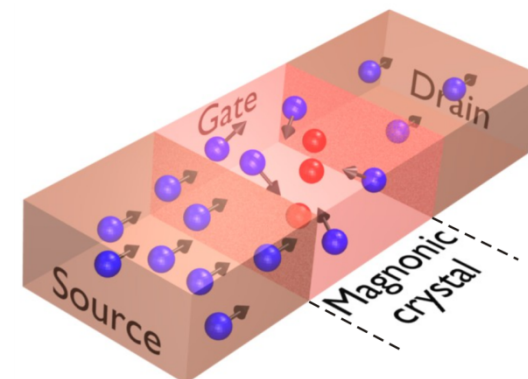
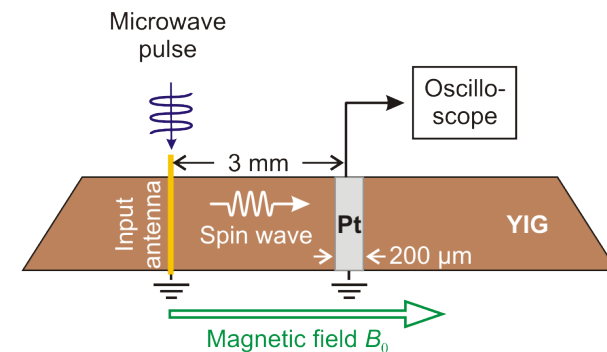
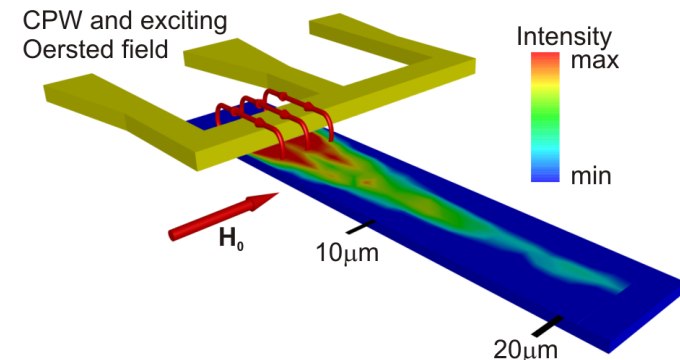
P. Pirro, Dr. A. Conca Parra, Dr. A. Chumak, T. Brächer, D. Pasarello, Prof. Dr. B. Hillebrands, T. Langner, R. Neb, B. Obry, Dr. V. Vasyuchka, M. Agrawal, Dr. B. Leven, P. Clausen, T. Meyer, B. Jungfleisch, T. Sebastian, Dr. E. Papaioannou, A. Kiriara, F. Heussner, V. Lauer, A. Ruiz Calaforra, Dr. F. Ciubotaru (+ Dr. A. Serga).

## I. New materials for magnonics

## II. Novel means for magnon detection

## III. Data processing using magnons

## IV. Magnonic supercurrents





## I. New materials for magnonics

Main requirement: small damping parameter

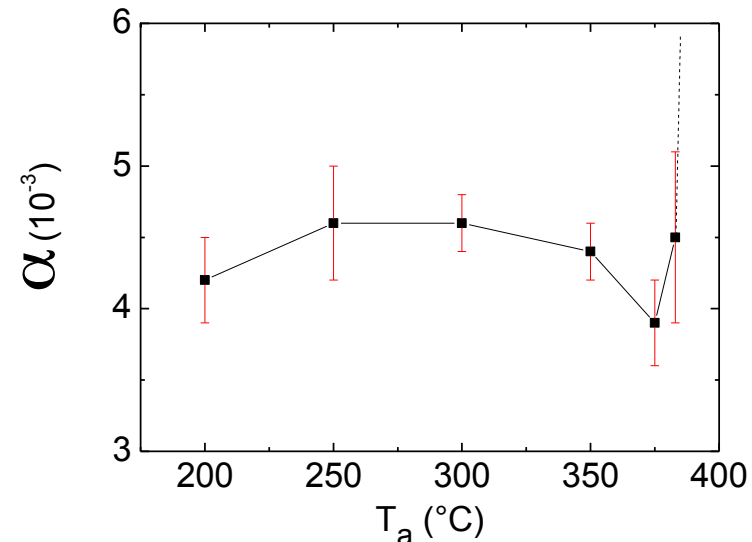


Commonly used material: Permalloy (Py, NiFe):  $\alpha = 8 \times 10^{-3}$

## I. New materials for magnonics

Main requirement: small damping parameter

- Commonly used material: Permalloy (Py, NiFe):  $\alpha = 8 \times 10^{-3}$
- ➔
- CoFeB: low damping (both am. and crystalline phase):  $\alpha = 4 \times 10^{-3}$



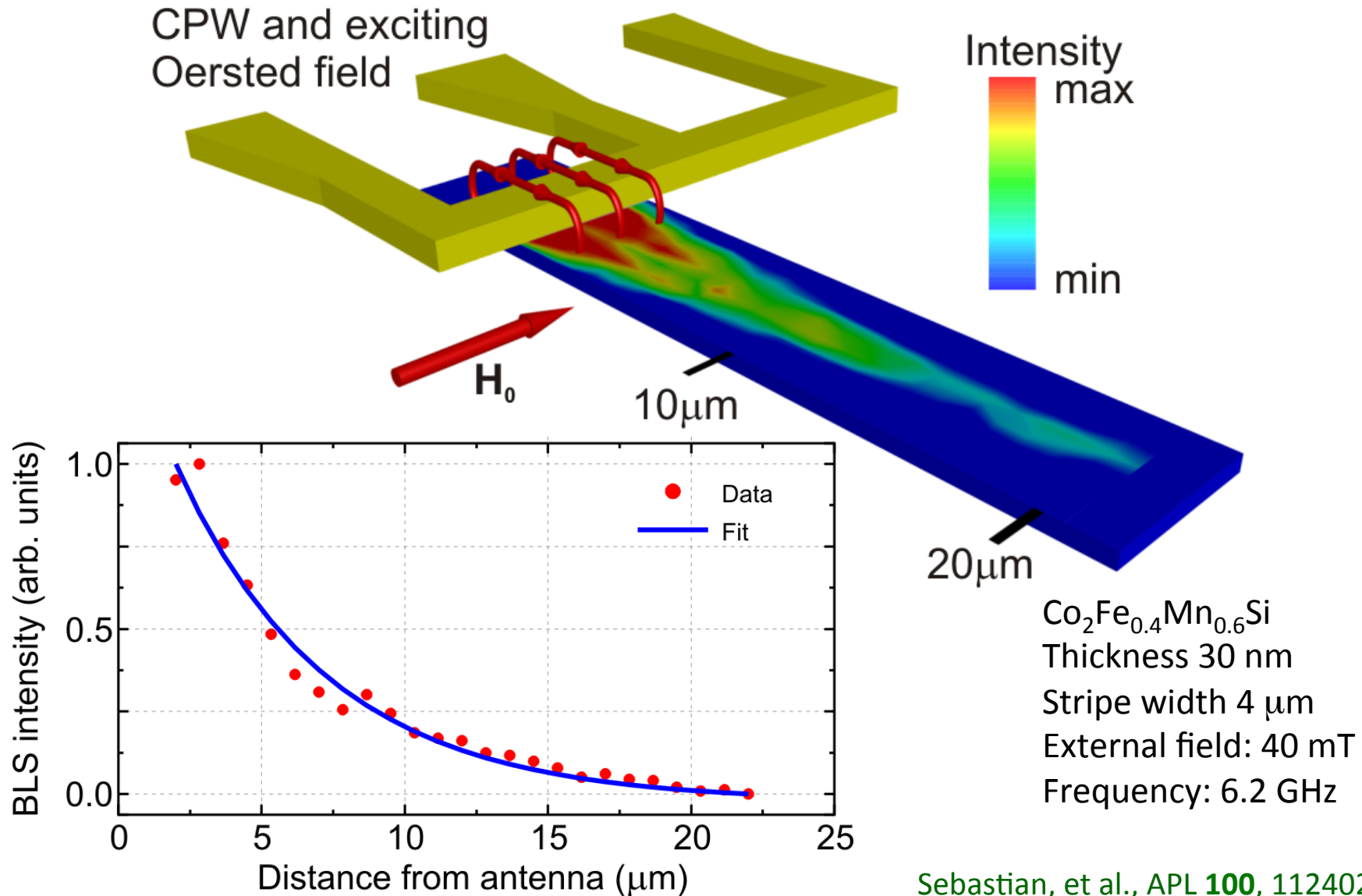
Liu, et al. JAP **110**, 033910 (2011)  
Conca, et al. APL **104**, 182407 (2014)

## I. New materials for magnonics

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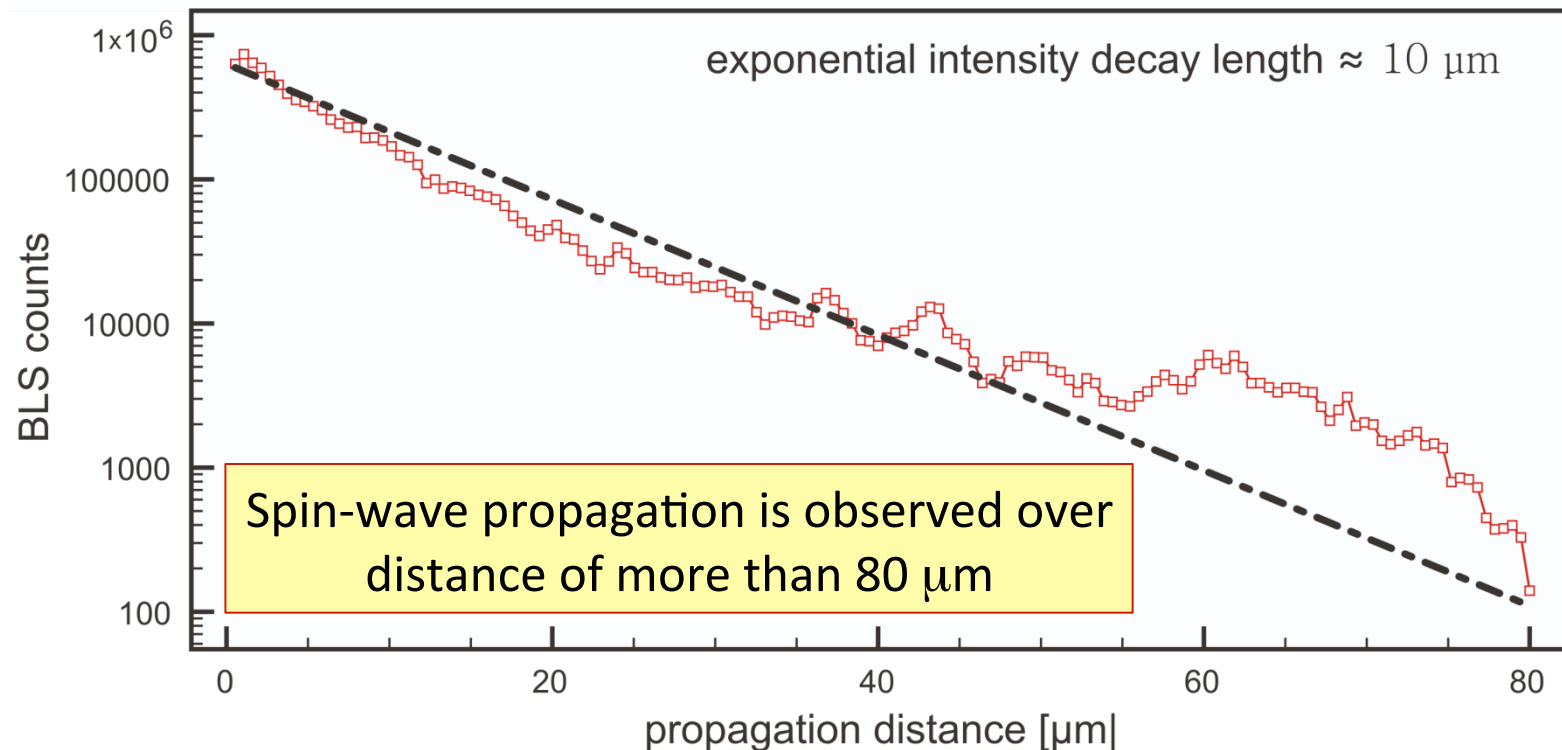
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# Spin-wave propagation in $\text{Co}_2\text{Fe}_{0.4}\text{Mn}_{0.6}\text{Si}$ Heusler waveguides



Sebastian, et al., *APL* **100**, 112402 (2012)

# Spin-wave propagation in $\text{Co}_2\text{Fe}_{0.4}\text{Mn}_{0.6}\text{Si}$ Heusler waveguides



$$I(x) = I_0 \exp\left(-\frac{2x}{\delta}\right) + b$$

$$\alpha = \frac{1}{\tau\gamma\mu_0(H_{\text{eff}} + M_s)} \quad \tau = \frac{\delta}{v_G}$$

Decay length:  $10.6 \mu\text{m}$

Damping  $\alpha$ :  $4.7 \times 10^{-3}$

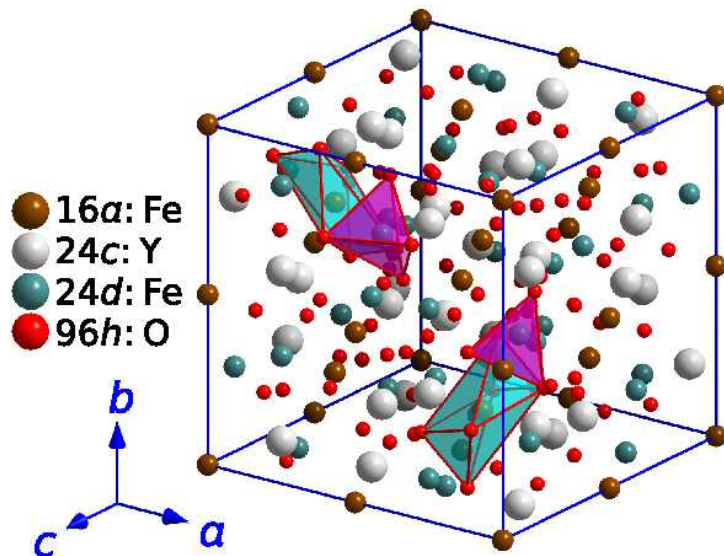
Sebastian, et al., APL **100**, 112402 (2012)

Sebastian, et al., PRL **110**, 067201 (2013)

## I. New materials for magnonics

- Commonly used material: Permalloy (Py, NiFe):  $\alpha = 8 \times 10^{-3}$
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  - Novel Heusler compounds:  $\alpha = 3 \times 10^{-3}$
- ➔ Micro-structured Yttrium Iron Garnet  $\text{Y}_3\text{Fe}_5\text{O}_{12}$  (YIG):  $\alpha = 4 \times 10^{-5}$

# Yttrium Iron Garnet $\text{Y}_3\text{Fe}_5\text{O}_{12}$ (YIG)



YIG:

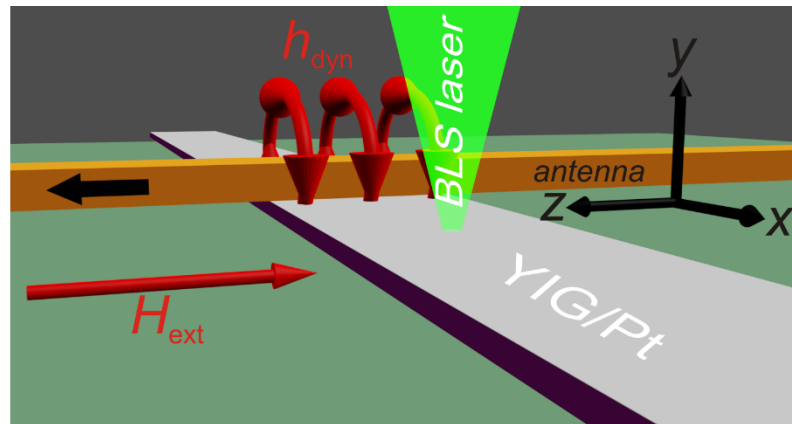
- magnetic insulator
- smallest spin-wave damping

Preparation via:

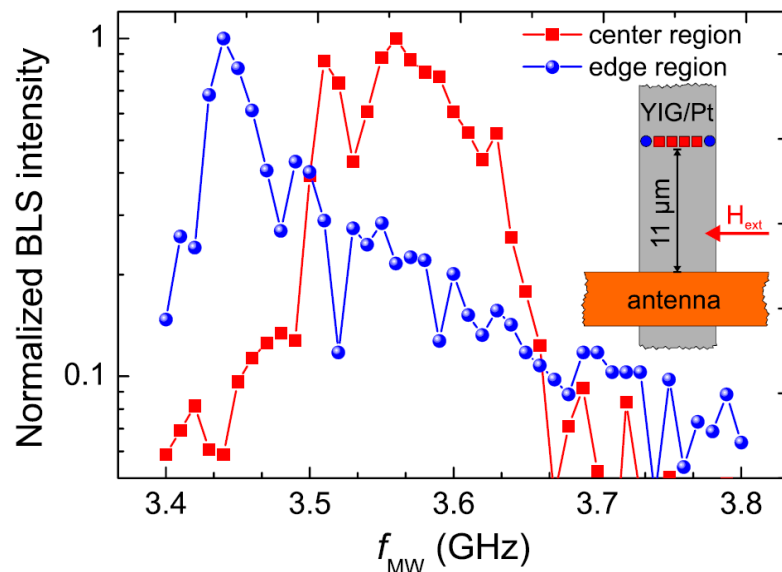
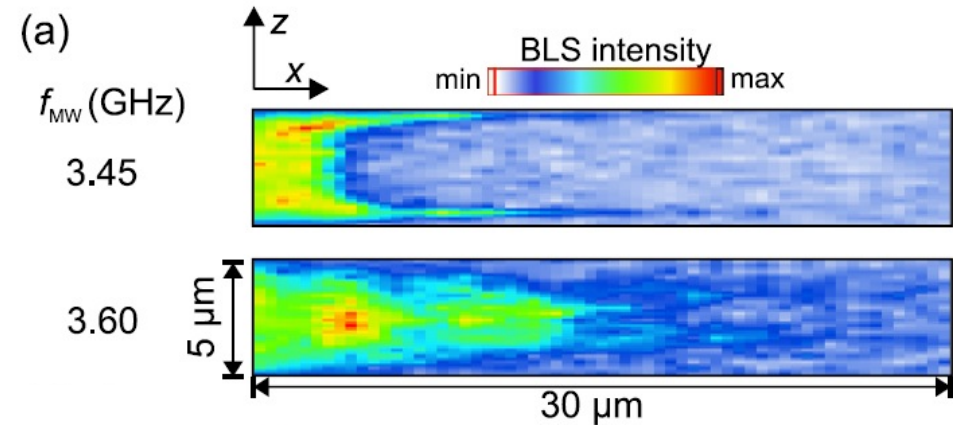
- liquid phase epitaxy
- sputtering
- pulsed laser deposition

A. Kreisel, Europhysics News (2006)

Micro-focused Brillouin Light Scattering setup was used for magnon detection



BLS intensity map: YIG thickness: 100 nm  
made by liquid phase epitaxy



For standard YIG quality:  
free path will be up to **1 mm**

P. Pirro, et al., APL **104**, 012402 (2014)



## I. New materials for magnonics

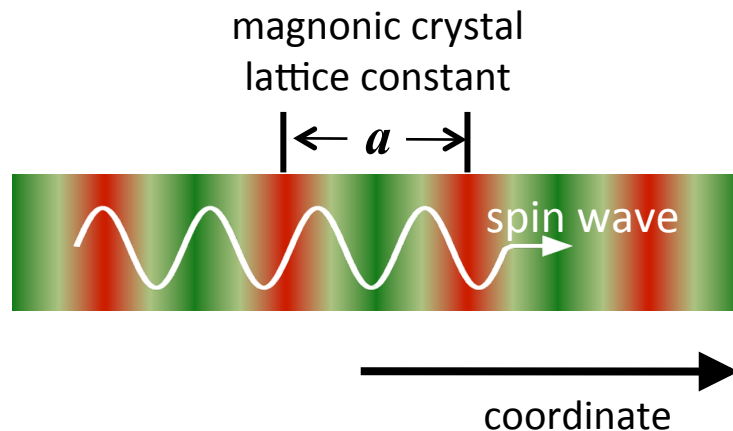
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- ➔ Magnonic crystals: artificial magnetic materials (static and dynamic)

# What is a “magnonic crystal”?

**Magnonic crystal** – magnetic meta-material:

- ❖ artificial medium with periodic lateral **variation in magnetic properties**

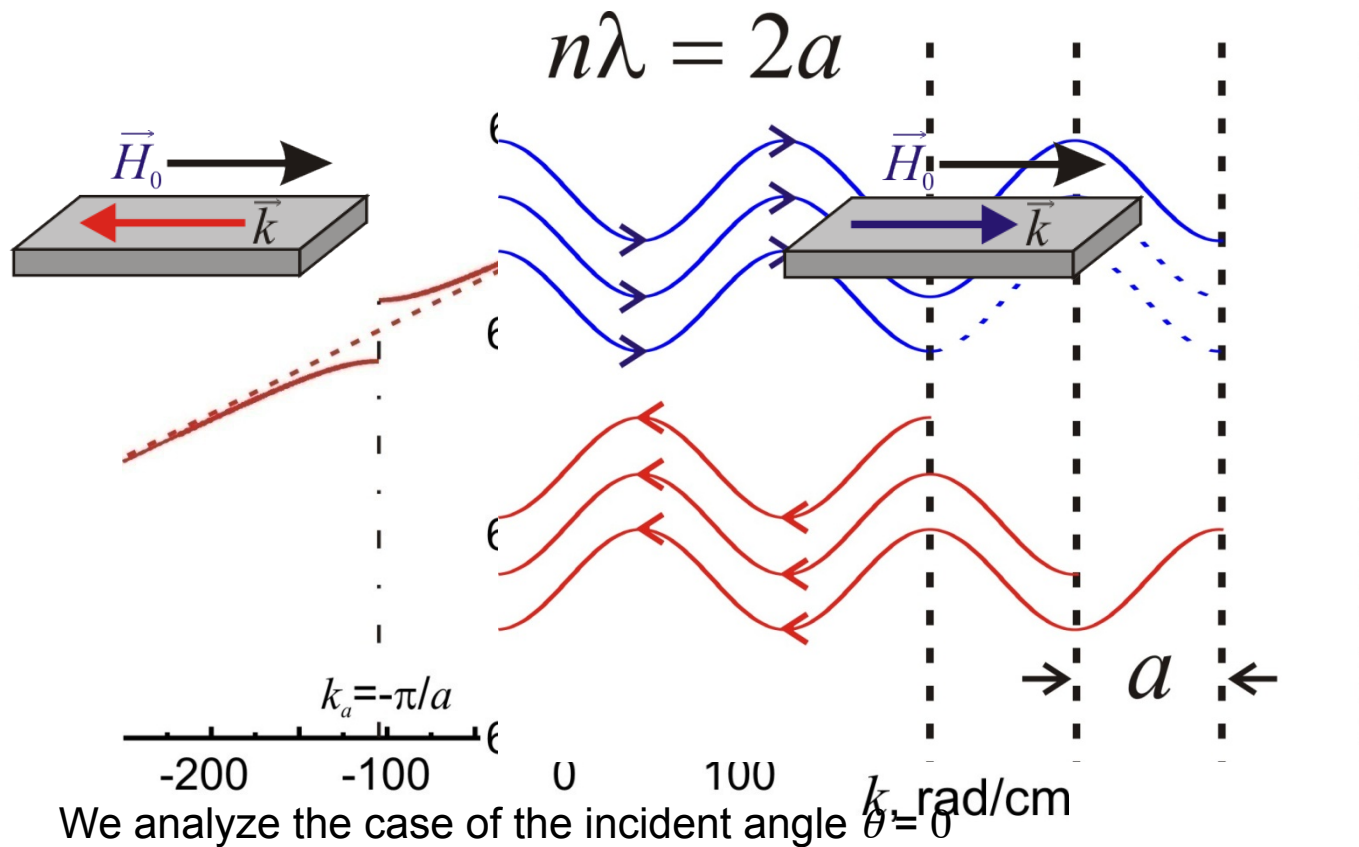
One-dimensional magnonic crystal:



Magnonic-crystal are **engineered** to have properties that may not be found in nature

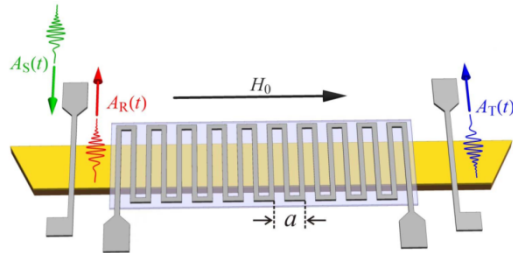
- ❖ analogous to **photonic and sonic** crystals but operates with spin waves in the GHz frequency range

**Band gaps** – regions of the spectrum over which waves are **not allowed** to propagate



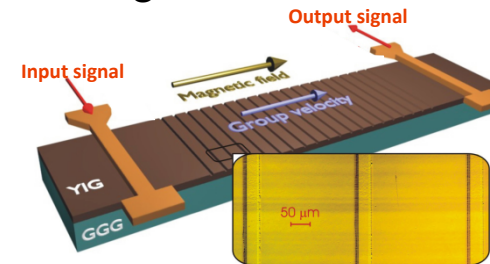
# Which magnetic property do we modulate?

## Bias magnetic field



Chumak et al., J. Phys. D **42**, 205005 (2009)

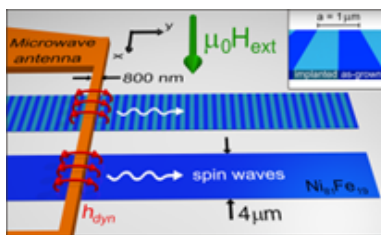
## Waveguide thickness



Sykes et al., APL **29**, 388 (1976)  
Chumak et al., APL **93**, (2008)

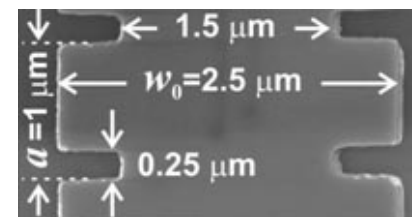
$$f(k) = \gamma \left( H_0 + 4\pi M_0 \frac{1 - \exp\{-\sqrt{(\pi/w)^2 + k^2}d\}}{\sqrt{(\pi/w)^2 + k^2}d} \right)$$

## Effective saturation magnetization



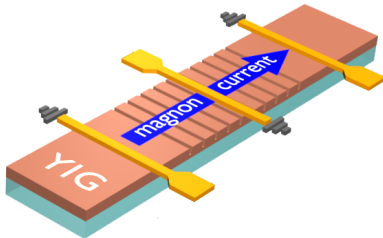
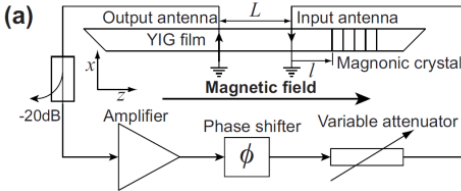
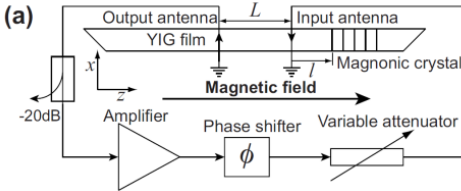
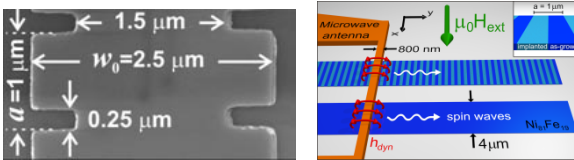
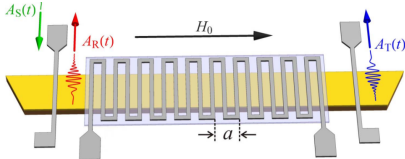
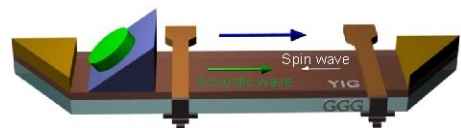
Chumak et al., PRB **81**, 140404 (2010)  
Obry et al., APL **102**, 202403 (2013)

## Waveguide width



Chumak et al., APL **95**, (2009)  
Lee et al., PRL **102**, 127202 (2009)

# Magnonic crystals - overview

|                                   |  |   |
|-----------------------------------|--|---|
| <p>microwave filter</p>           |    | <p>Chumak et al., APL <b>93</b>, 022508 (2008)<br/>Chumak et al., APL <b>94</b>, 172511 (2009)<br/>Chumak et al., JAP <b>105</b>, 083906 (2009)</p>   |
| <p>data storage element</p>       |    | <p>Chumak et al., PRL, <b>108</b>, 257207 (2012)</p>  |
| <p>stable microwave generator</p> |    | <p>Karenowska et al., APL <b>96</b>, 082505 (2010)</p>  |
| <p>micro-sized crystal</p>        |   | <p>Chumak et al., APL <b>95</b>, 262508 (2009)<br/>Ciubotaru et al., J.Phys.D <b>45</b>, 255002 (2012)<br/>Obry et al., APL, <b>102</b>, 202403 (2013)<br/>Ciubotaru, et al. PRB <b>88</b>, 134406 (2013)</p> |
| <p>switchable device</p>          |  | <p>Chumak, et al., J.Phys.D <b>42</b>, 205005 (2009)<br/>Chumak, et al., Nat. Commun. <b>1</b>:141 (2010)<br/>Karenowska, et al., PRL <b>108</b>, 015505 (2012)</p>   |
| <p>travelling crystal</p>         |  | <p>Chumak et al., PRB, <b>81</b>, 140404 (2010)</p>   |

## Localized ion implantation:

- Purely magnetic patterning
- No change in sample topography

## State of the art studies (YIG):

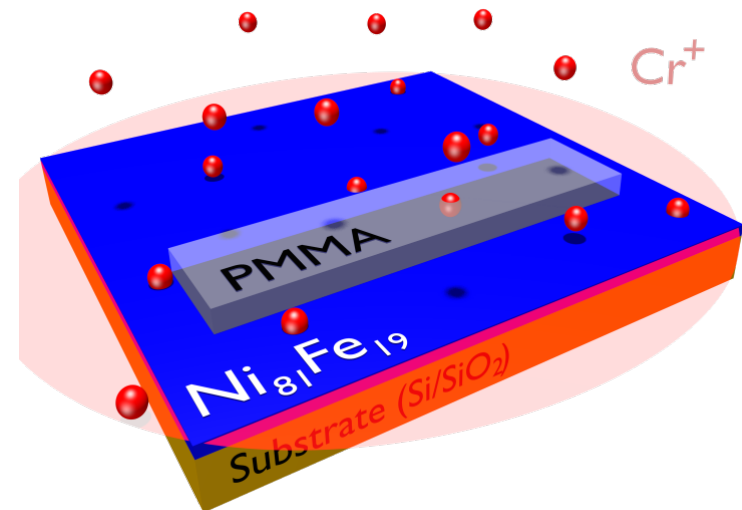
G. Volluet, P. Hartemann,  
*Reflection of magnetostatic forward volume waves by ion  
implanted gratings,*  
Proc. IEEE Ultrasonics Symp., 394 (1981).

R. L. Carter, J. M. Owens, C. V. Smith, Jr., K. W. Reed,  
*Ion-implanted magnetostatic wave reflective array filters,*  
J. Appl. Phys. 53 (1982), 2655.

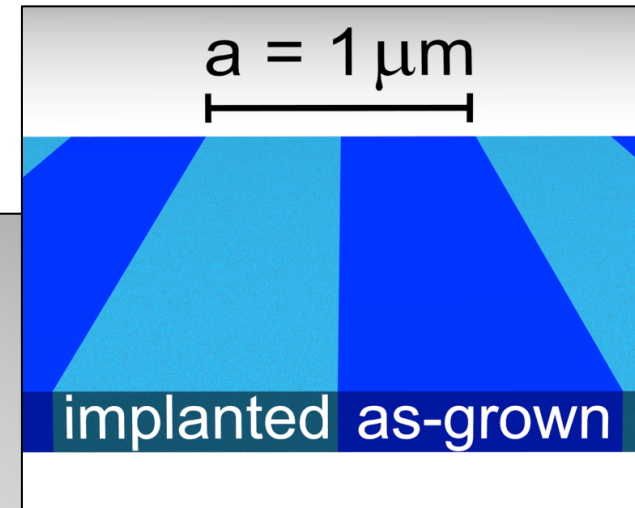
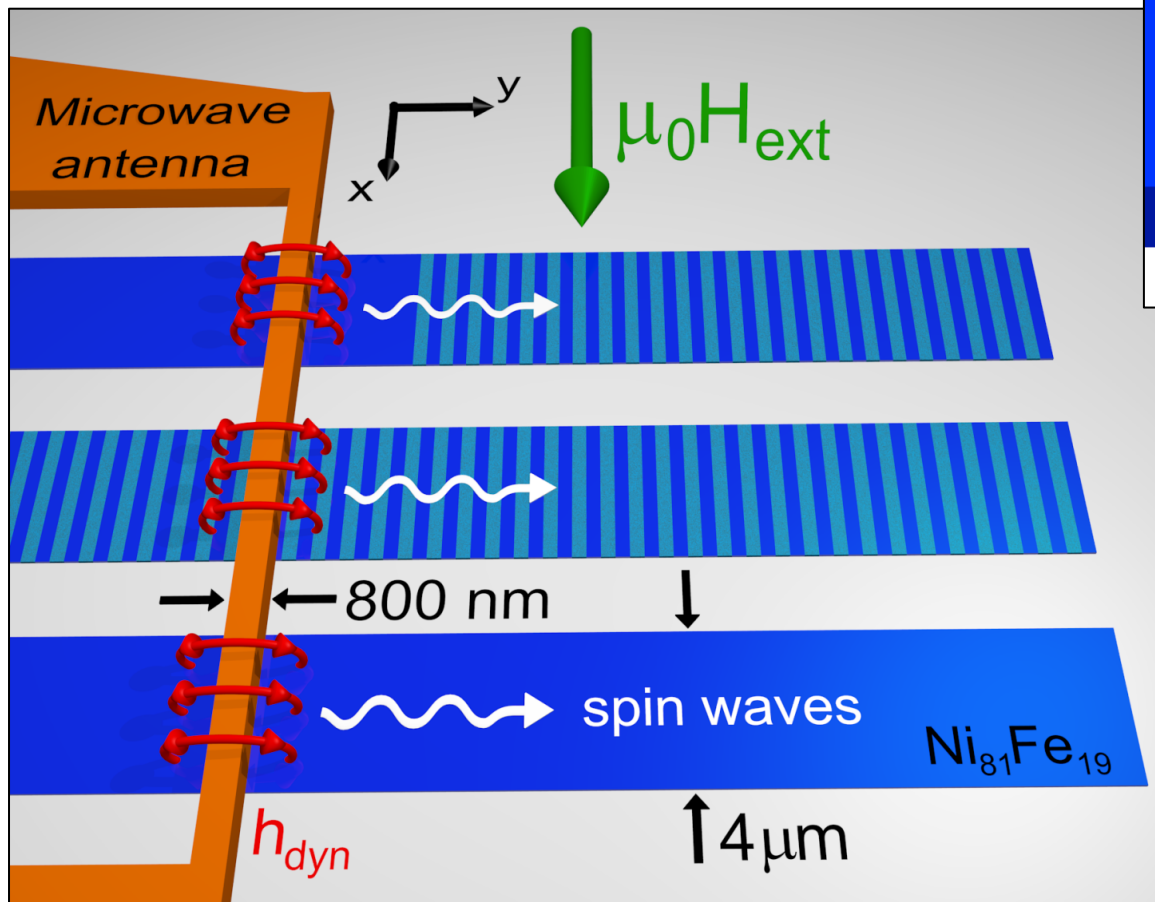
Irradiation of  $\text{Ni}_{81}\text{Fe}_{19}$  films with 30 keV  
 $\text{Cr}^+$  ions:

Control saturation magnetization  $M_S$   
and Gilbert damping  $\alpha$

Fassbender *et al.*, PRB **73**, 184410 (2006)

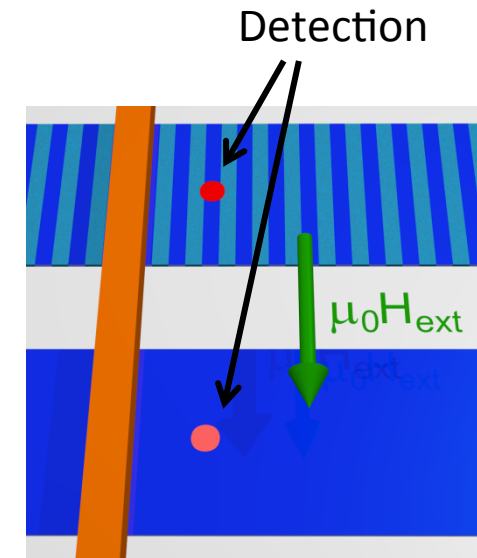
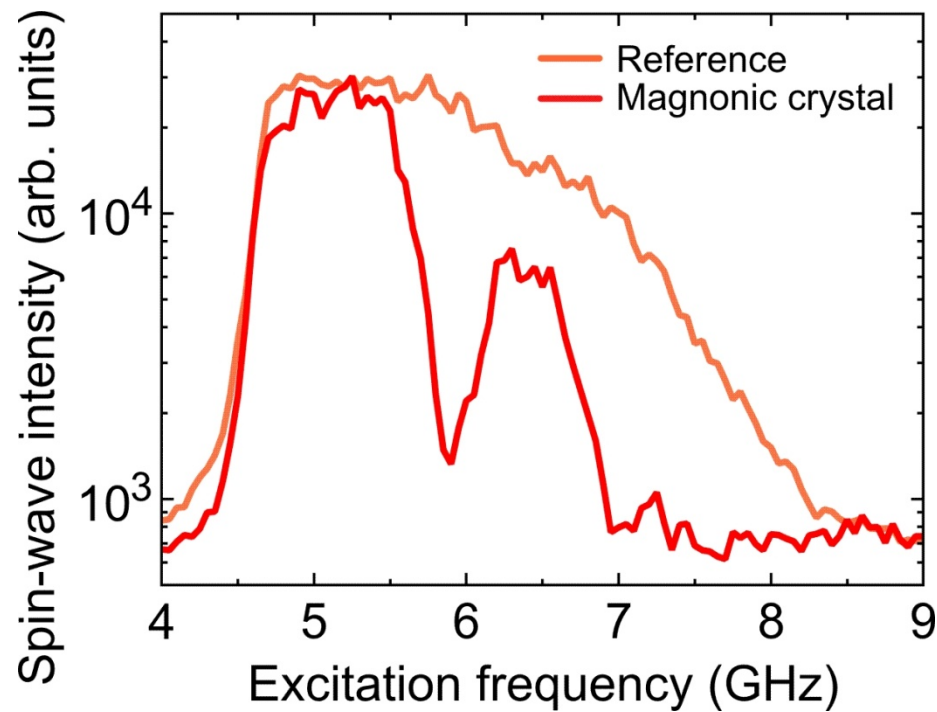


Fabrication of microscopic metallic **magnonic crystal** with **periodic change in saturation magnetization  $M_S$**



- Waveguides:  
 MBE evaporation  
 Lift-off techniques

Spin-wave excitation spectra:



$$\mu_0 H_{\text{ext}} = 27.3 \text{ mT}$$

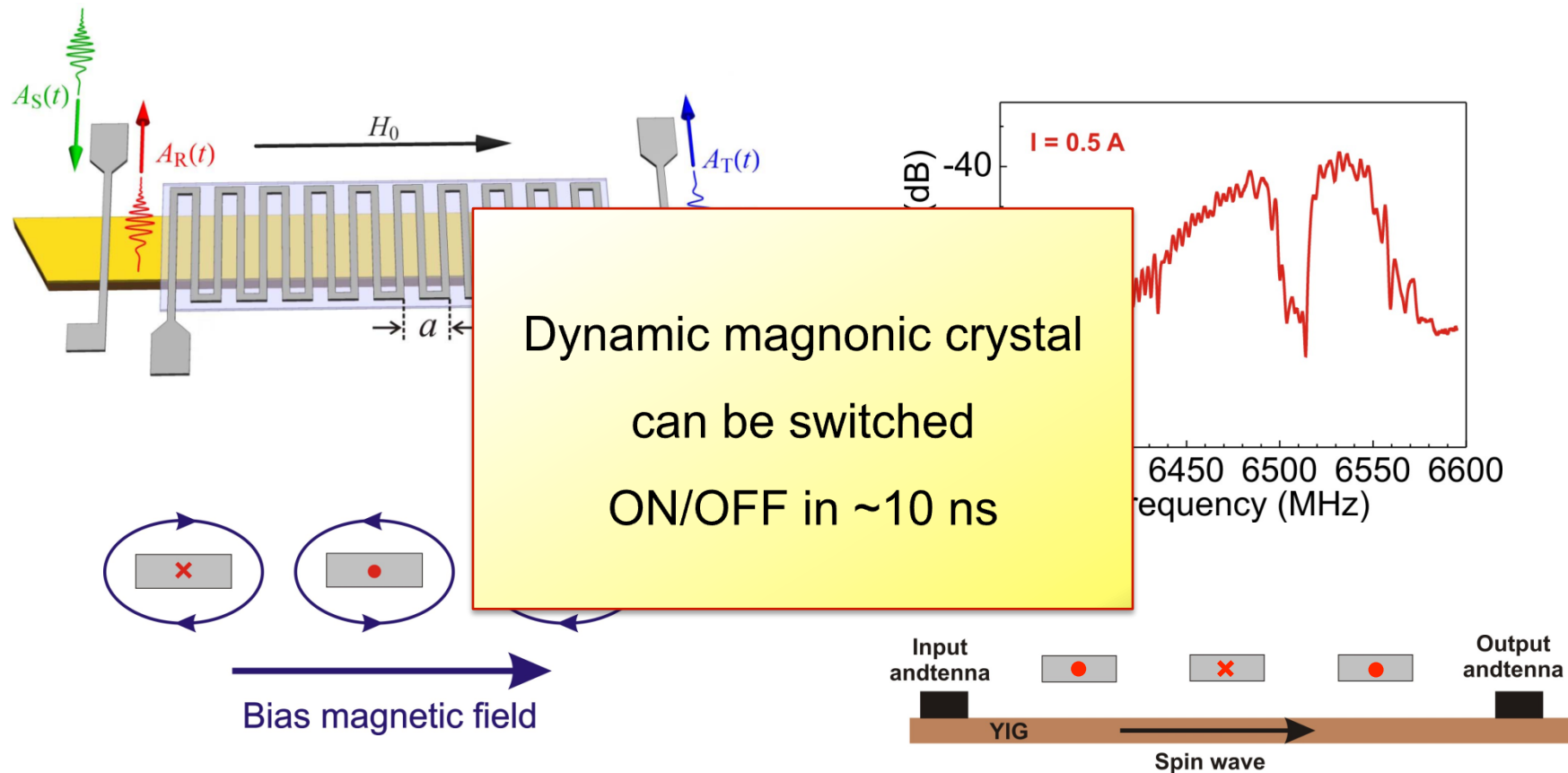
Two pronounced band gaps in transmission spectrum

Obry *et al.*, APL **102**, 202403 (2013)

Ciubotaru, *et al.* PRB **88**, 134406 (2013)



Periodic modulation of the bias magnetic field by **current-carrying wires**

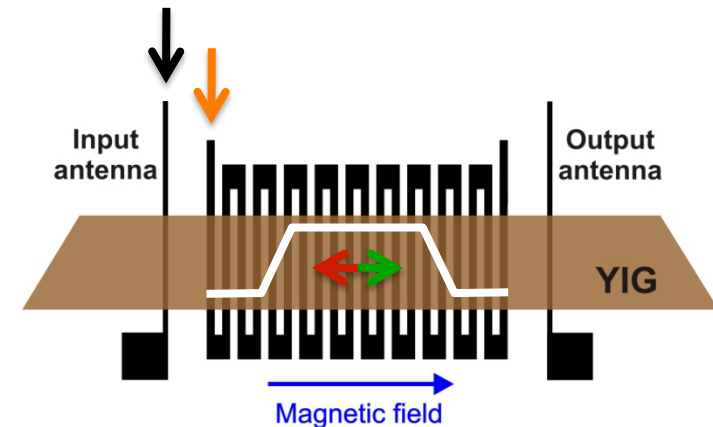
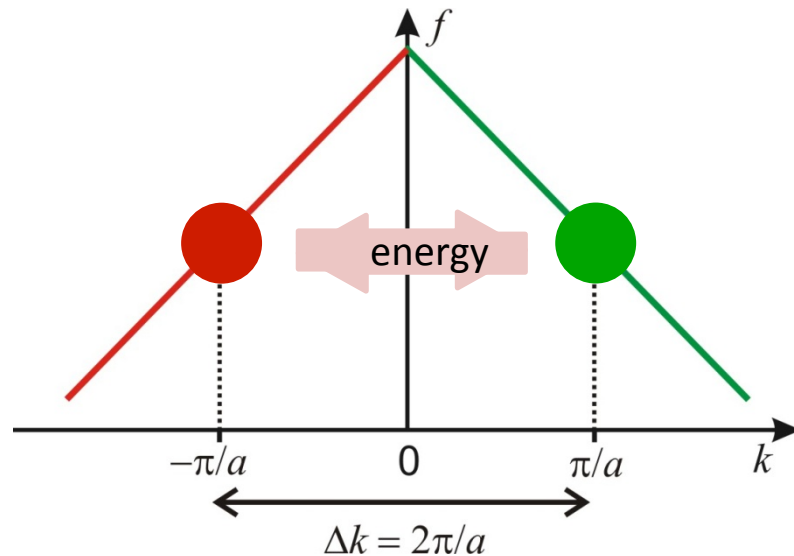


Lattice constant:  $a = 300 \mu\text{m}$

Number of periods:  $N_g = 20$

Chumak, et al., J. Phys. D **42**, 205005 (2009)

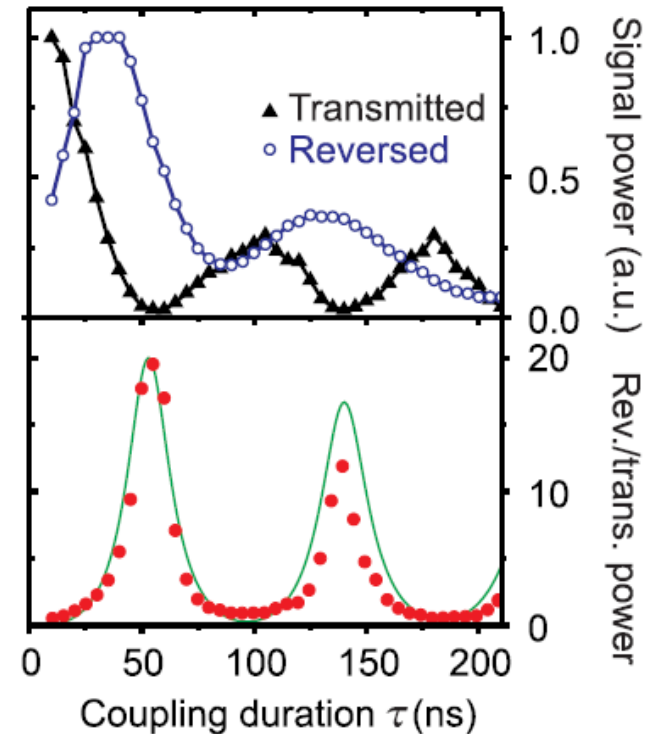
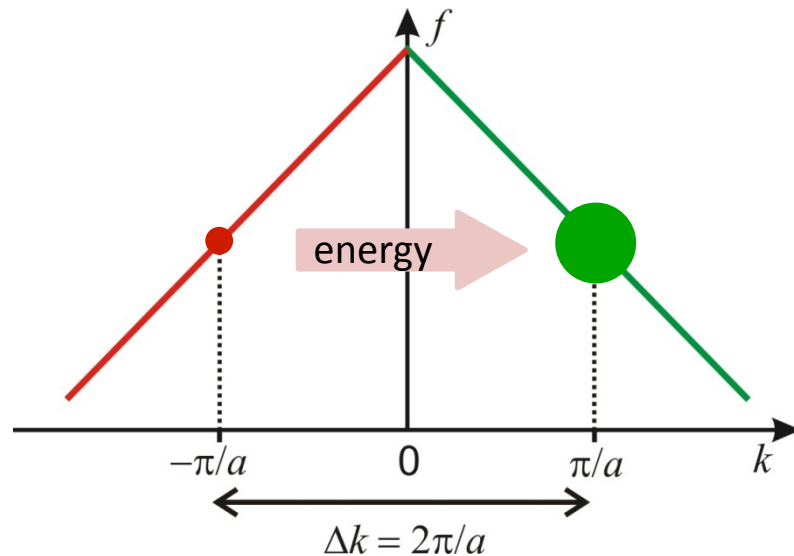
# Spin-wave mode coupling by dynamic magnonic crystal



Two modes with  $k = \pi/a$  and  $k = -\pi/a$  are coupled by periodic variation of field

Coupling provides a mechanism for **energy transfer**

# Spin-wave mode coupling by dynamic magnonic crystal



Chumak, et al., Nat. Commun. **1**:141 (2010)  
Karenowska, et al., PRL **108**, 015505 (2012)

Two modes with  $k = \pi/a$  and  $k = -\pi/a$  are coupled by periodic variation of field

Coupling provides a mechanism for **energy transfer**

# All-linear time reversal by DMC

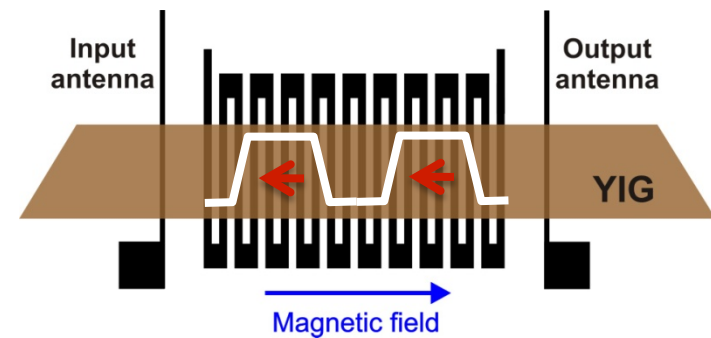
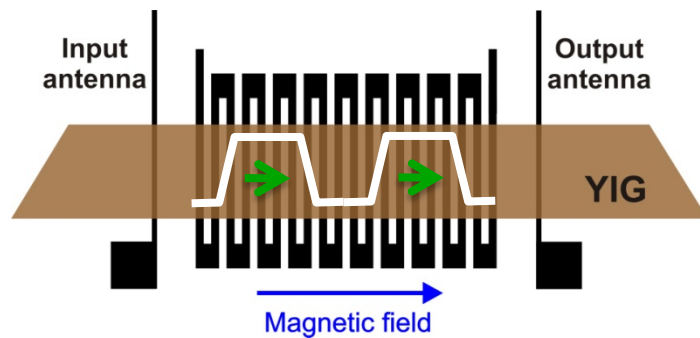
Input signal:

$$A_S(t) \sim \sum_{\Delta f} \exp(-i 2\pi \Delta f t)$$

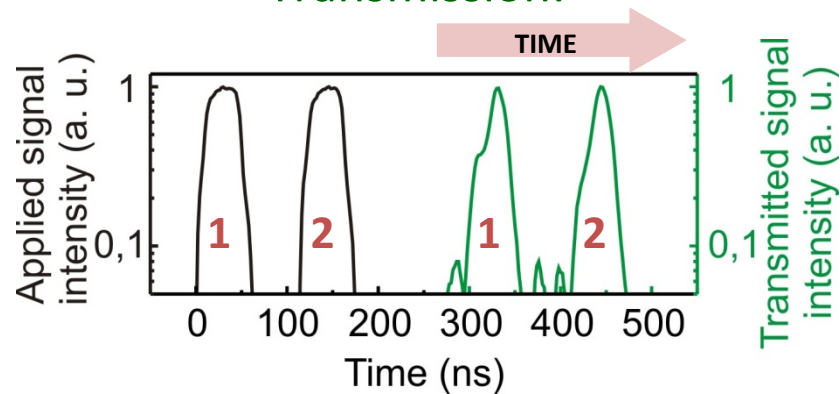
$\Delta f$  is a frequency shift from the Bragg frequency

Reflected signal:

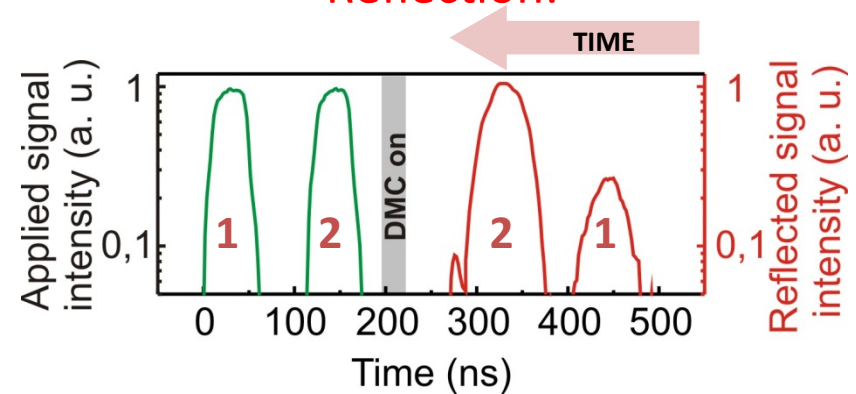
$$A_R(t) \sim \sum_{\Delta f} \exp(i 2\pi \Delta f t) \sim A_S(-t)$$



Transmission:

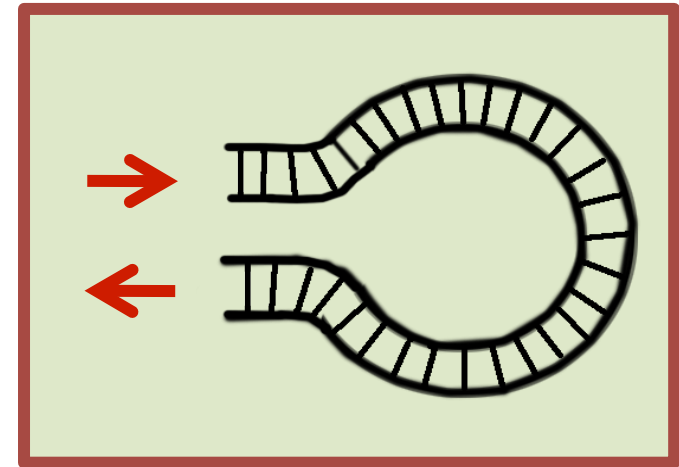
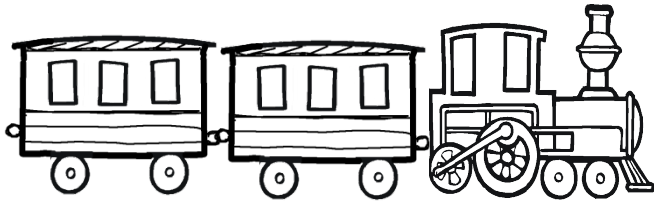


Reflection:

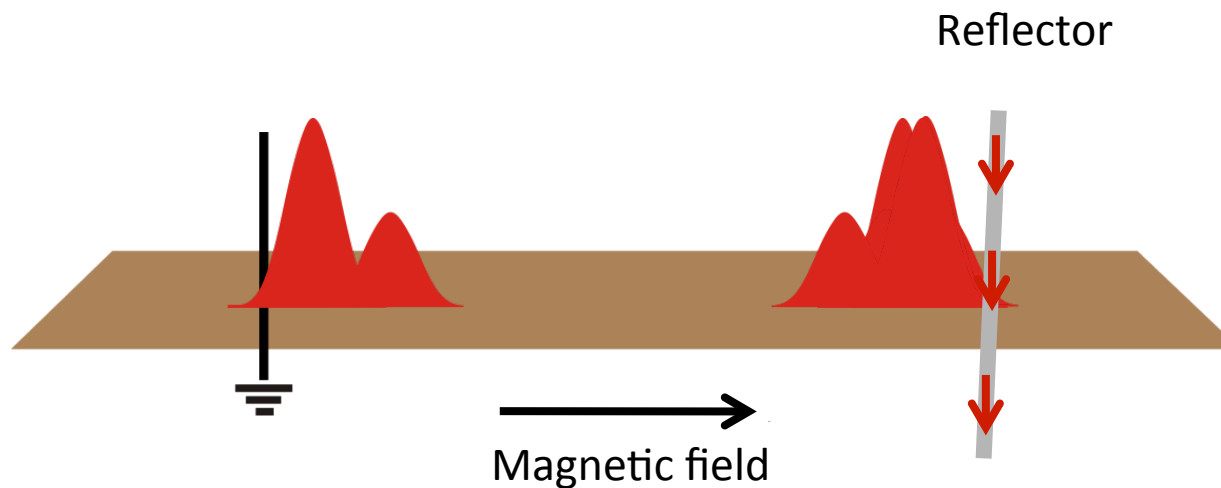


# Classical reflection from mirror

Railway analog:

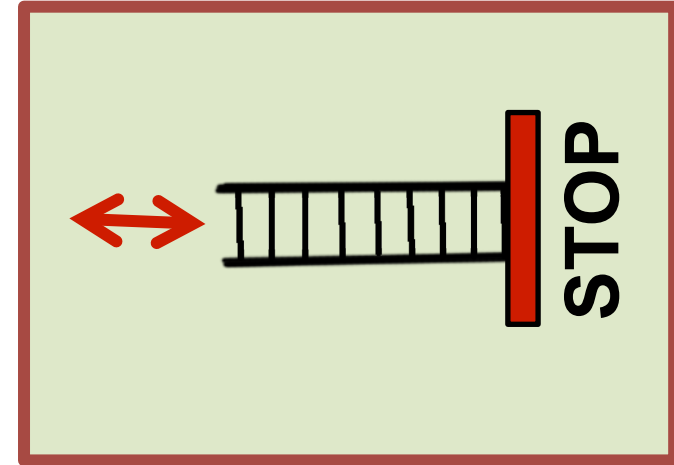
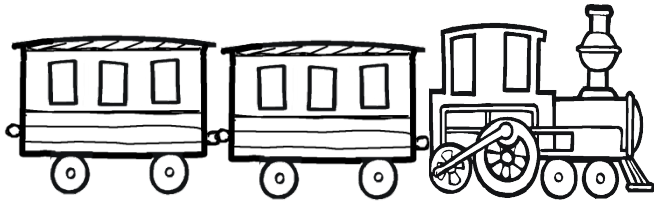


Spin-wave experiment:

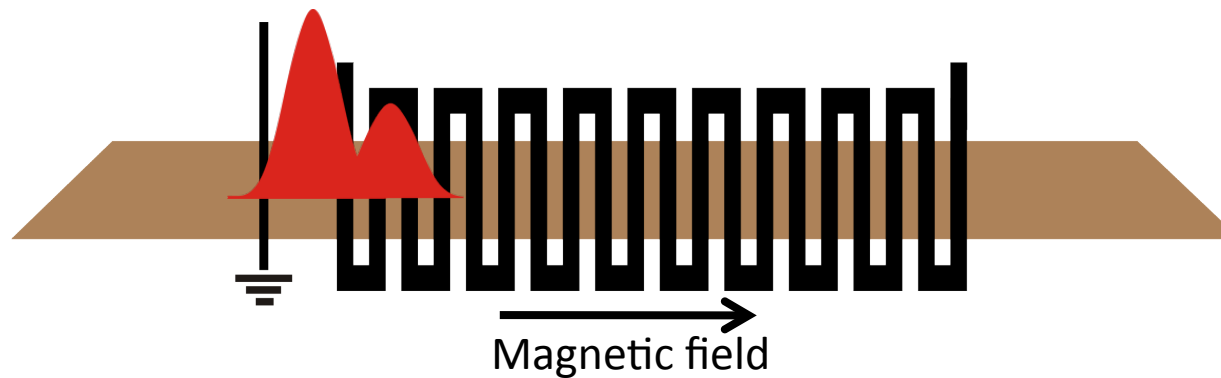


# Reflection via time reversal

Railway analog:



Spin-wave experiment:



## I. New materials for magnonics

- Commonly used material: Permalloy (Py, NiFe):  $\alpha = 8 \times 10^{-3}$
- CoFeB: low damping (both am. and crystalline phase):  $\alpha = 4 \times 10^{-3}$
- Novel Heusler compounds:  $\alpha = 3 \times 10^{-3}$
- Micro-structured Yttrium Iron Garnet  $\text{Y}_3\text{Fe}_5\text{O}_{12}$  (YIG):  $\alpha = 4 \times 10^{-5}$
- Magnonic crystals: artificial magnetic materials (static and dynamic)



Normally magnetized non-reciprocal materials

## Simulation of a **perpendicular magnetized Permalloy discs** (OOMMF)

### Parameters

$$\mu_0 M_s = 1 \text{ T}$$

$$H_k = 0$$

$$\alpha = 0.007$$

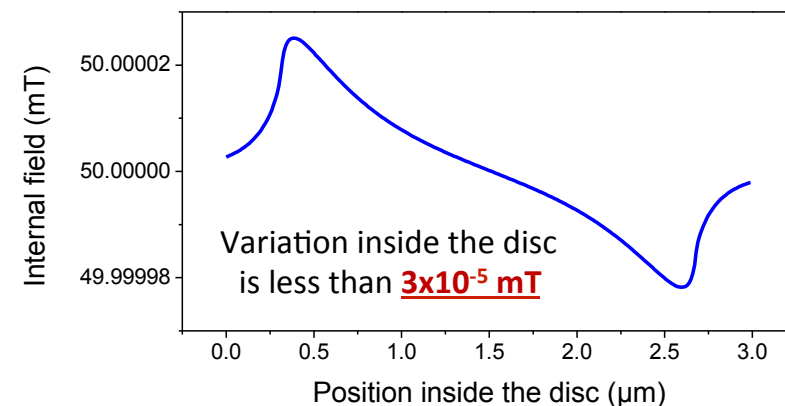
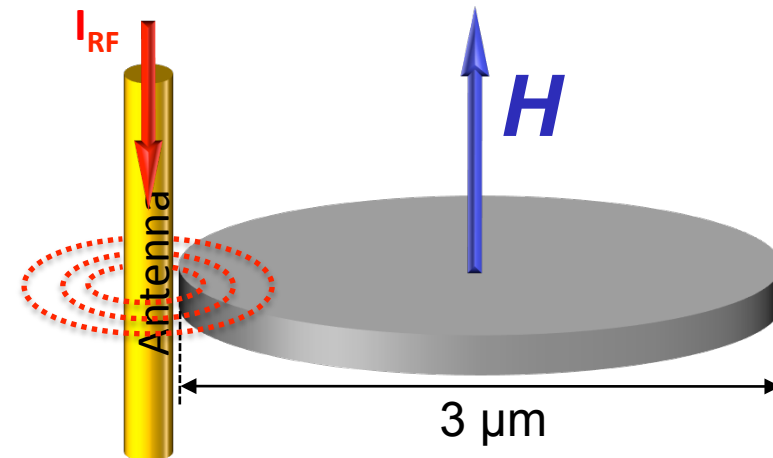
$$\mu_0 H = 1.050 \text{ T}$$

Spin waves are excited by the dynamic Oersted field created by injecting an RF current through antenna.

Diameter of antenna: 500 nm

Side charges were added in order to have an uniform distribution of the internal field.

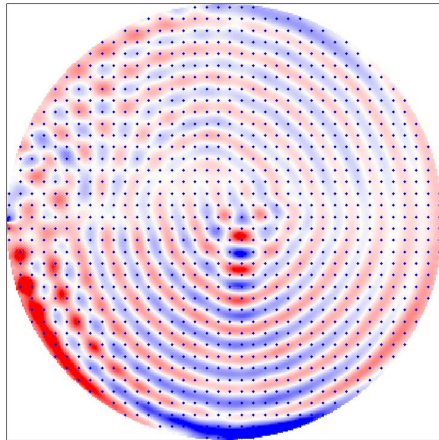
Internal field = 50 mT





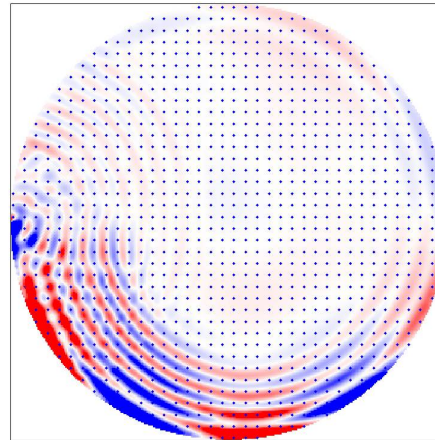
# Spin-wave boundary mode

$f = 8 \text{ GHz}$



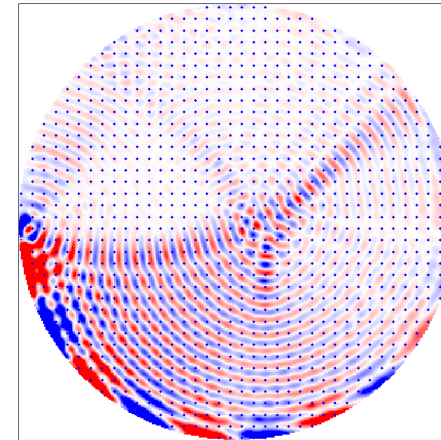
$\lambda_v = 278 \text{ nm}$   
 $\lambda_e = 3.7 \text{ }\mu\text{m}$

$f = 10 \text{ GHz}$

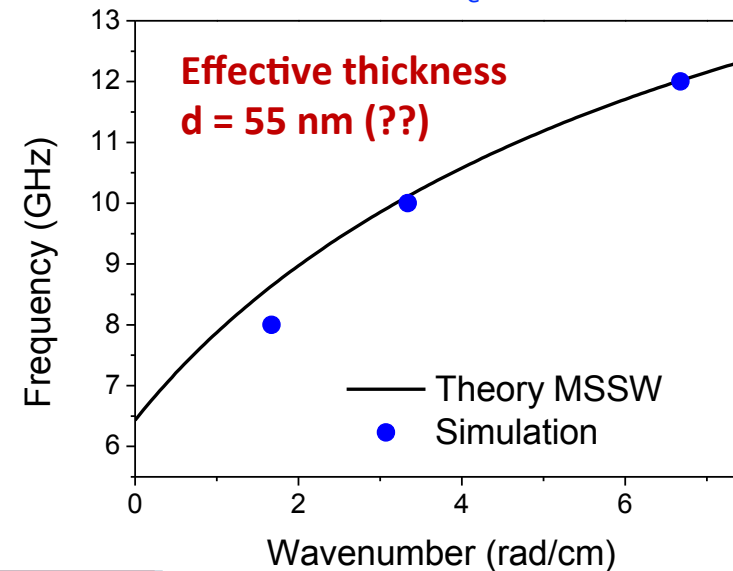
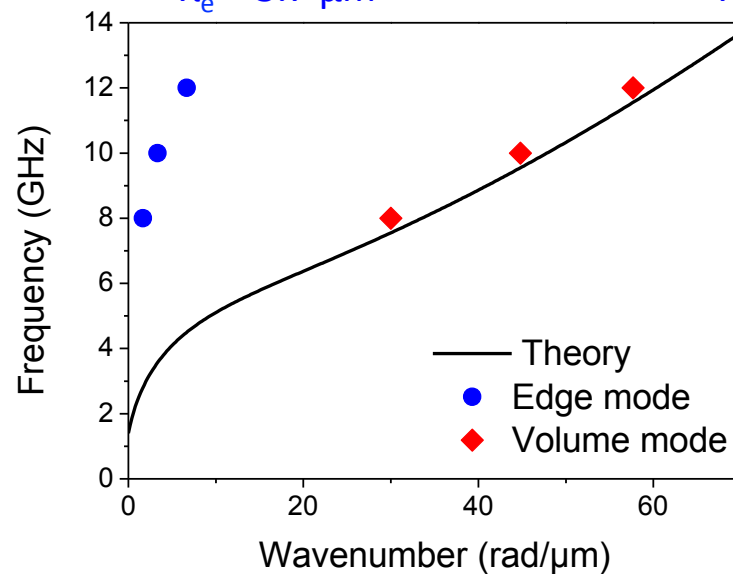


$\lambda_v = 125 \text{ nm}$   
 $\lambda_e = 1.9 \text{ }\mu\text{m}$

$f = 12 \text{ GHz}$

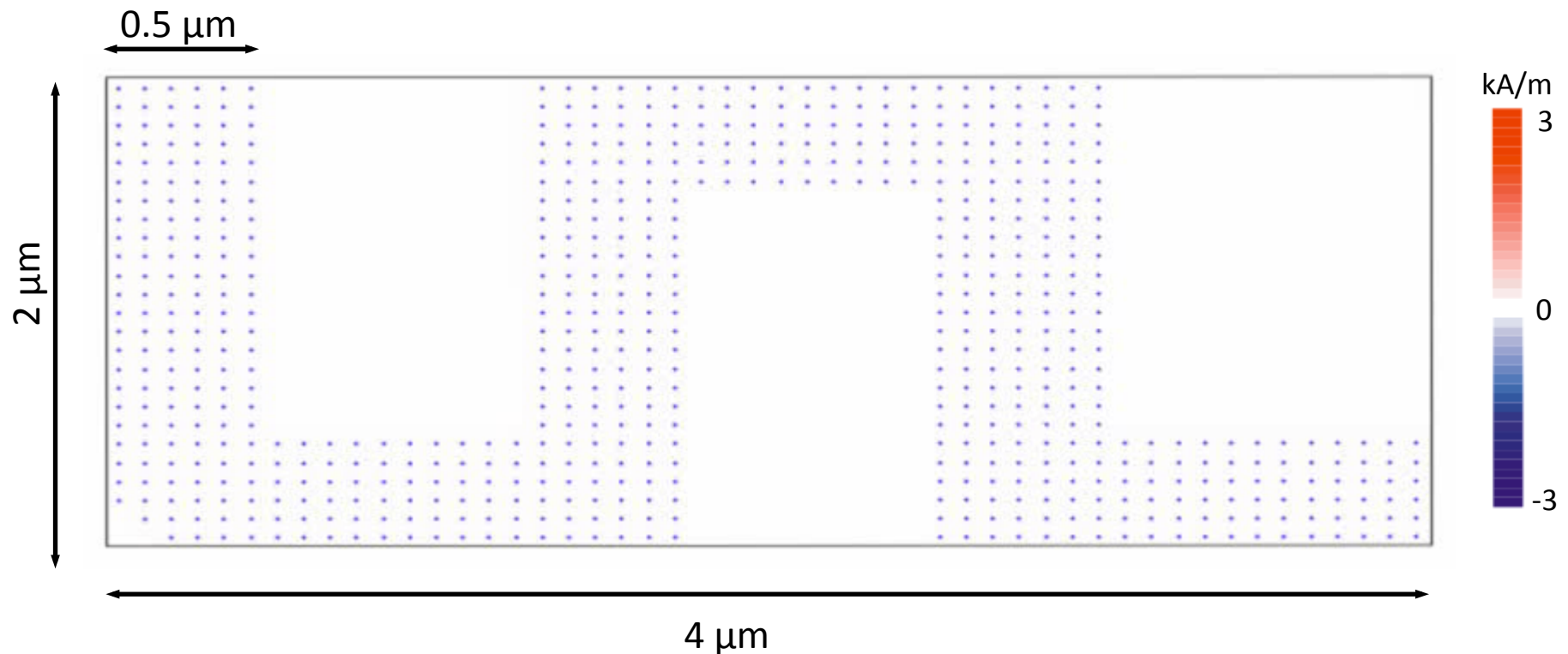


$\lambda_v = 98 \text{ nm}$   
 $\lambda_e = 0.94 \text{ }\mu\text{m}$



Thickness = 300 nm

Excitation frequency = 10 GHz



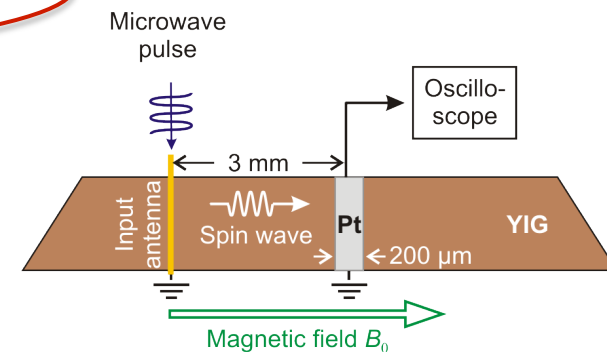
The boundary mode propagates around the corners without changing its properties

I. New materials for magnonics

II. Novel means for magnon detection

III. Data processing using magnons

IV. Magnonic supercurrents



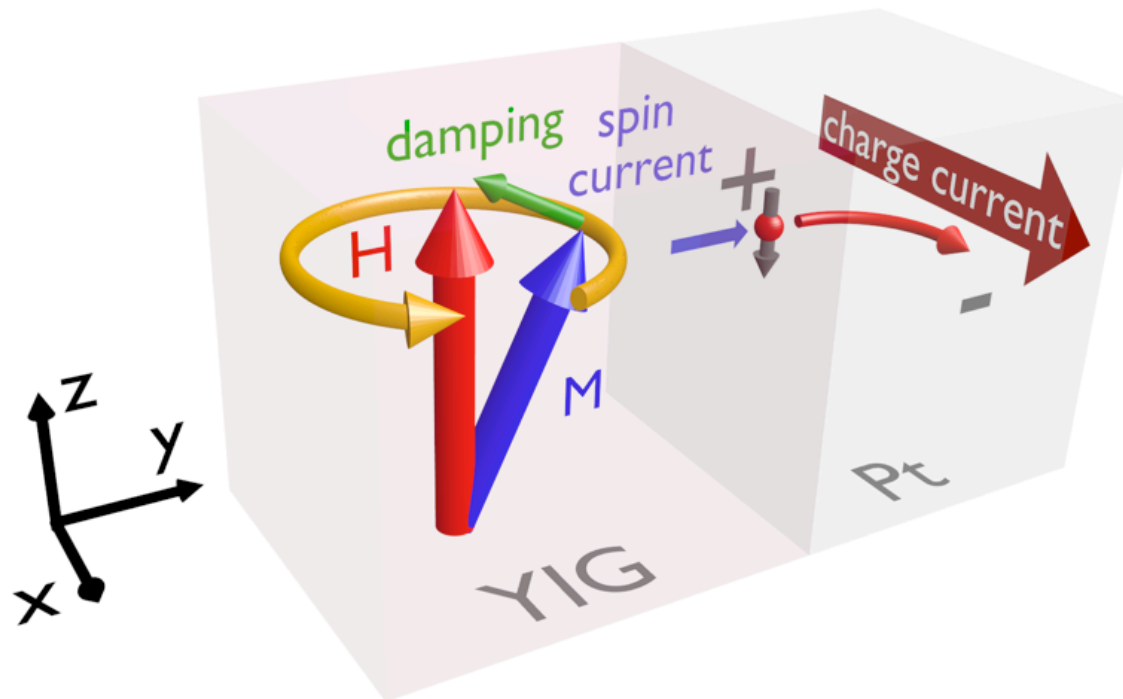
## II. Novel means for magnon detection



Spin pumping + inverse spin Hall effect

# Magnon to charge current conversion

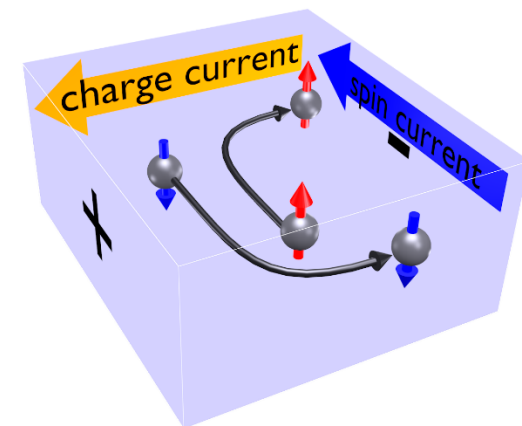
Detection of magnons by a combination of spin pumping and inverse spin Hall effect



## Spin pumping

Tserkovnyak et al., PRL (2002)  
Costache et al., PRL (2006)

## Inverse spin Hall effect (ISHE)



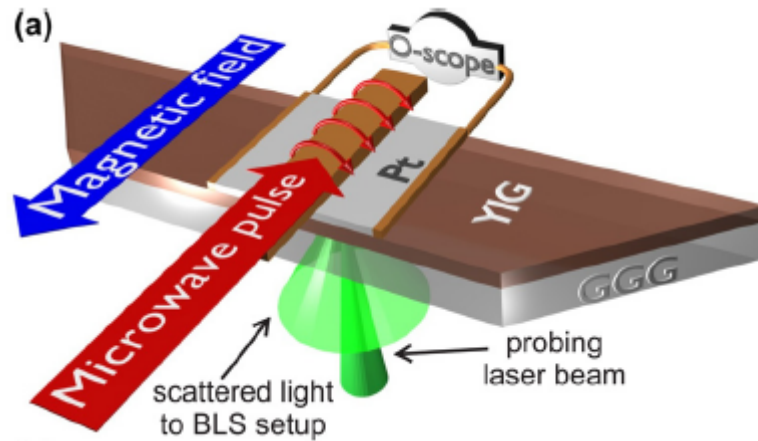
Hirsch, PRL (1999)  
Saitoh et al., APL **88** 182509 (2006)

# Time resolved ISHE voltage

Yttrium iron garnet (YIG) / platinum (Pt) bilayer was used

Magnetic field  $B = 0$

Microwave frequency 7 GHz

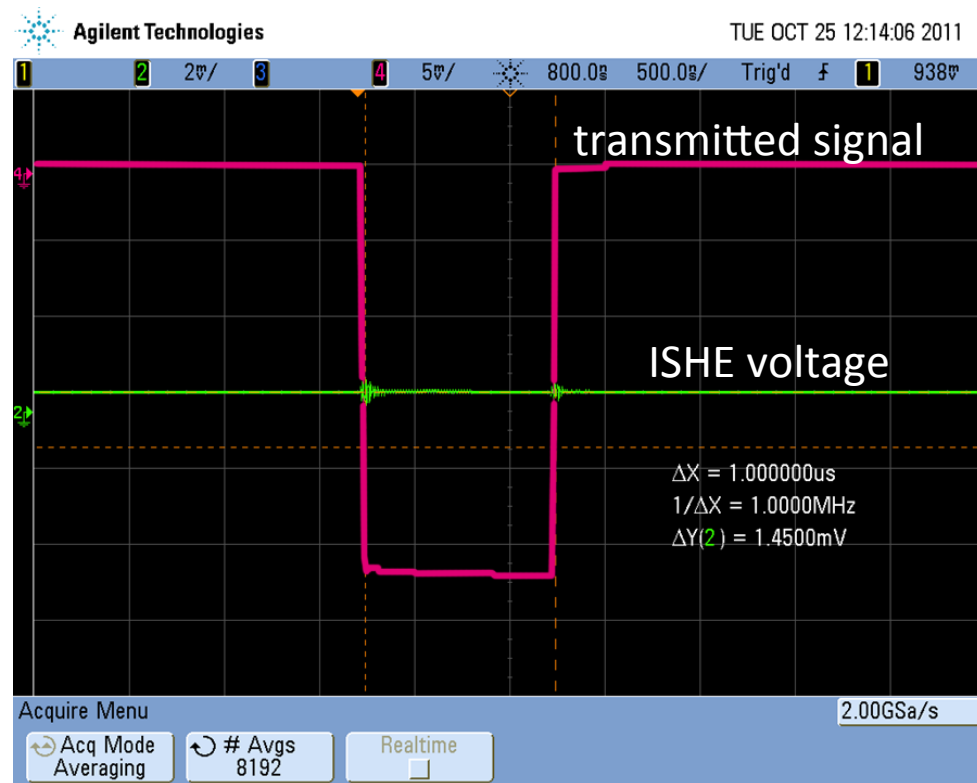


## Parameters:

YIG thickness: 2.1  $\mu\text{m}$

YIG/Pt width: 3 mm

Pt thickness: 10 nm



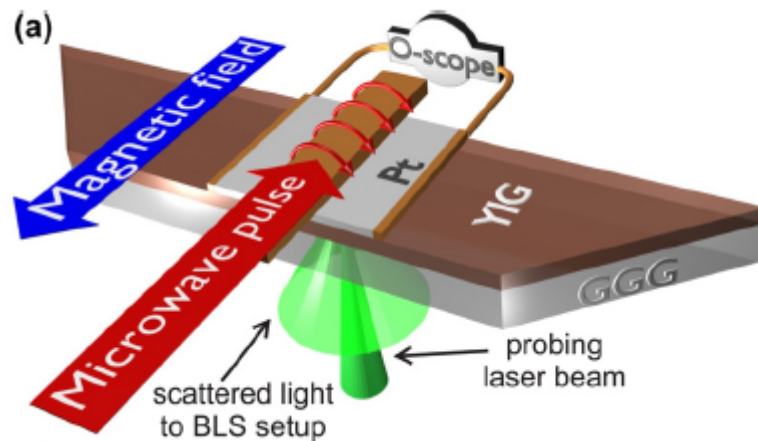
Jungfleisch et al., APL **99**, 182512 (2011)

# Time resolved ISHE voltage

Yttrium iron garnet (YIG) / platinum (Pt) bilayer was used

Magnetic field  $B = -175.5 \text{ mT}$

Microwave frequency 7 GHz

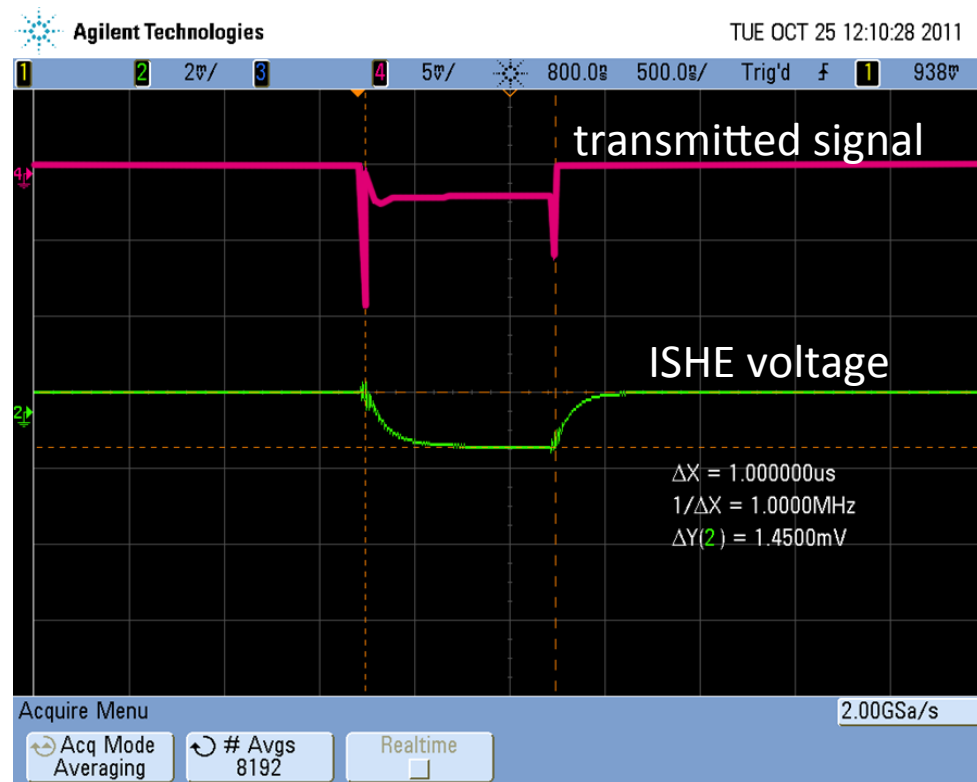


## Parameters:

YIG thickness:  $2.1 \mu\text{m}$

YIG/Pt width: 3 mm

Pt thickness: 10 nm



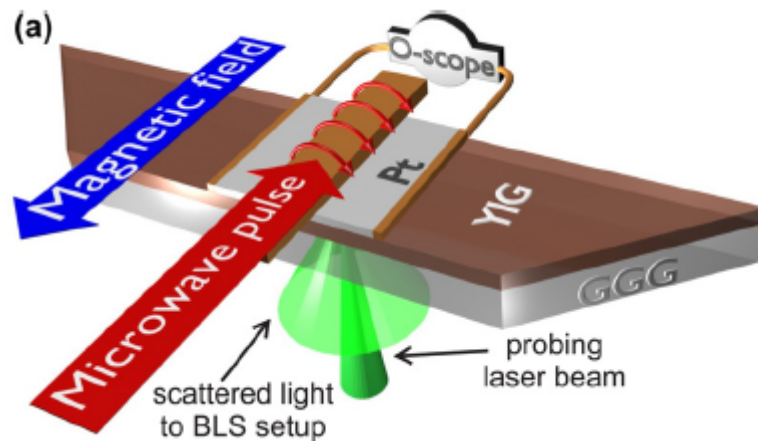
Jungfleisch et al., APL **99**, 182512 (2011)

# Time resolved ISHE voltage

Yttrium iron garnet (YIG) / platinum (Pt) bilayer was used

Magnetic field  $B = +175.5 \text{ mT}$

Microwave frequency 7 GHz

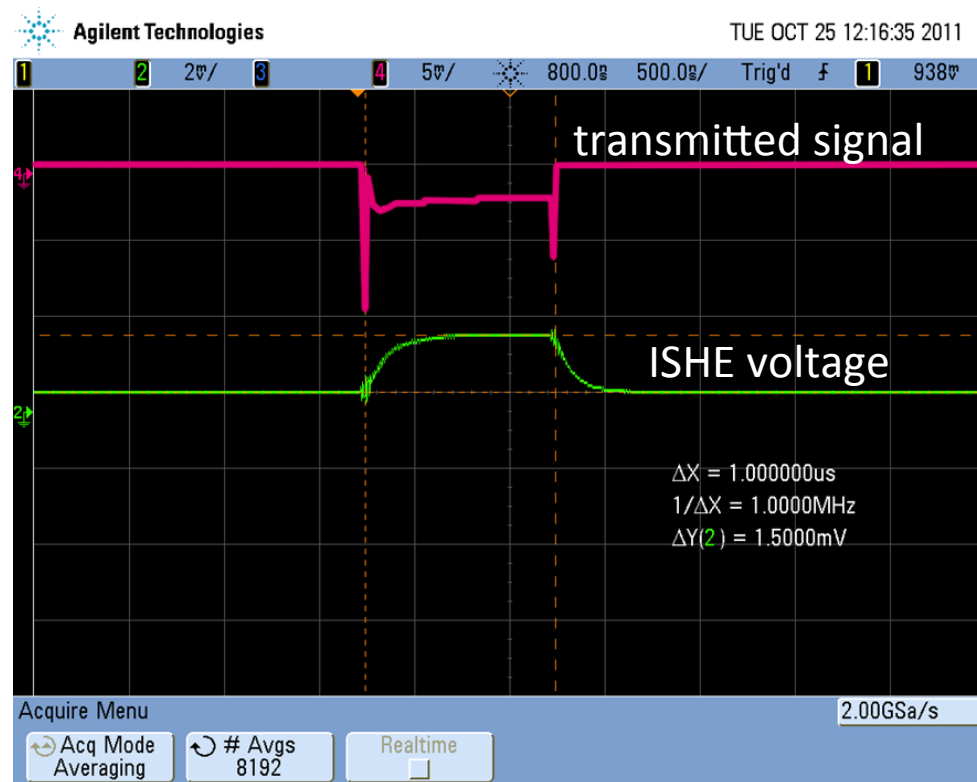


## Parameters:

YIG thickness:  $2.1 \mu\text{m}$

YIG/Pt width: 3 mm

Pt thickness: 10 nm



Jungfleisch et al., APL **99**, 182512 (2011)

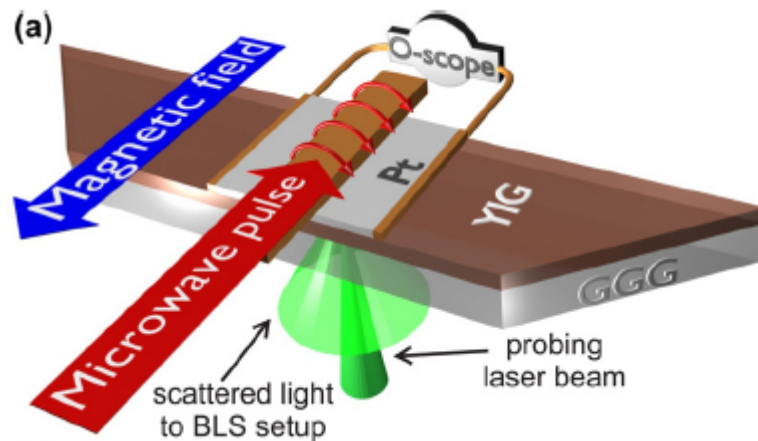


# Time resolved ISHE voltage

Yttrium iron garnet (YIG) / platinum (Pt) bilayer was used

Magnetic field  $B = + 175.5 \text{ mT}$

Microwave frequency 7 GHz

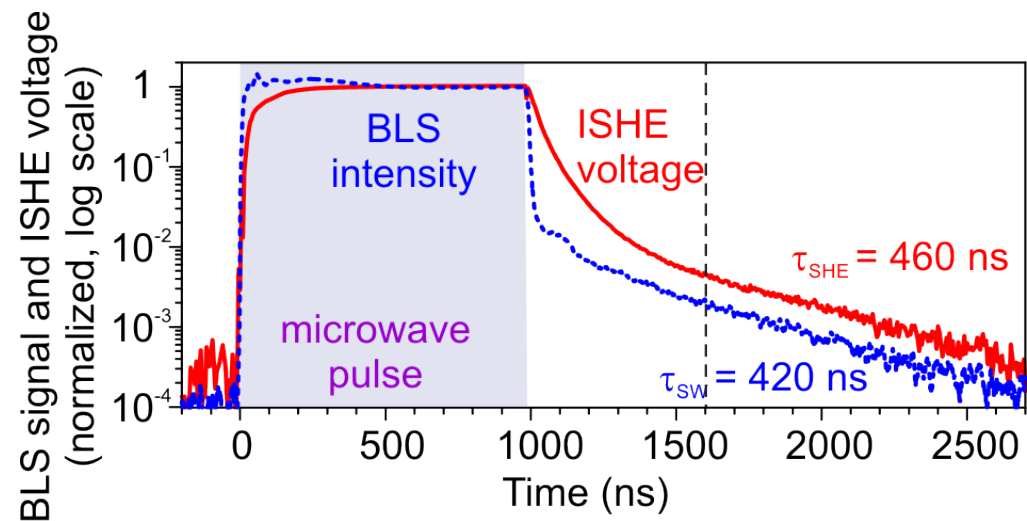


## Parameters:

YIG thickness:  $2.1 \mu\text{m}$

YIG/Pt width: 3 mm

Pt thickness: 10 nm



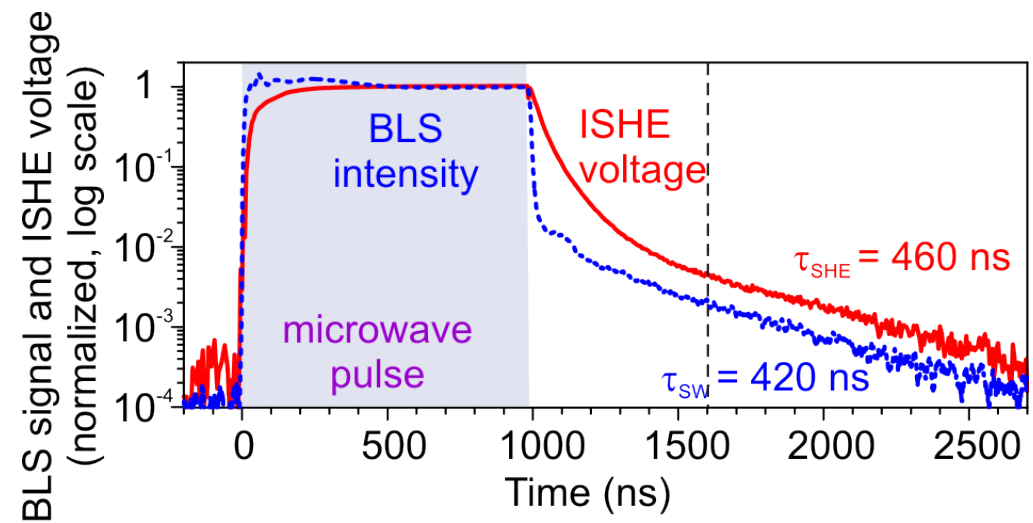
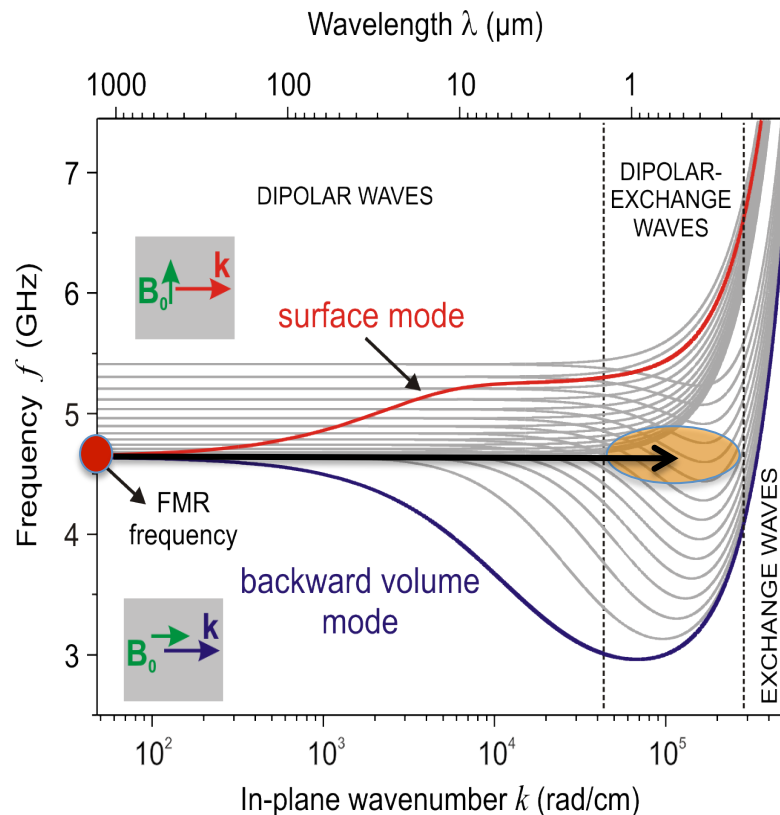
- ❖ ISHE pulse has a long rise and fall times
- ❖ Secondary magnons contribute to ISHE

Jungfleisch et al., APL 99, 182512 (2011)

Yttrium iron garnet (YIG) / platinum (Pt) bilayer was used

Magnetic field  $B = + 175.5$  mT

Dipolar-exchange waves contribute to spin pumping!

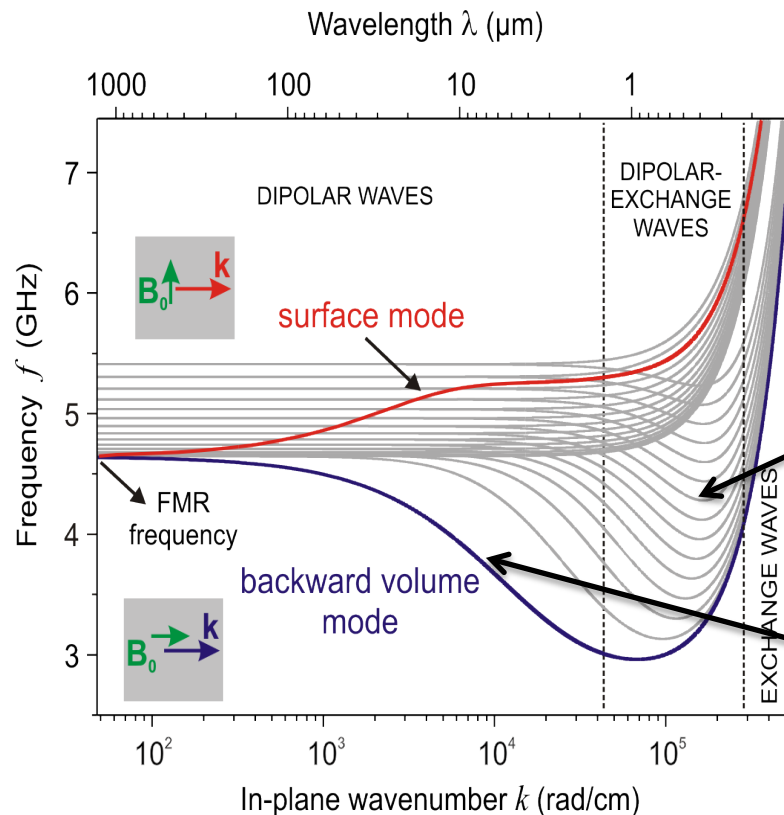


- ❖ ISHE pulse has a long rise and fall times
- ❖ Secondary magnons contribute to ISHE

Jungfleisch et al., APL 99, 182512 (2011)

# Surface modes contribute to spin pumping

Yttrium iron garnet (YIG) / platinum (Pt) bilayer was used

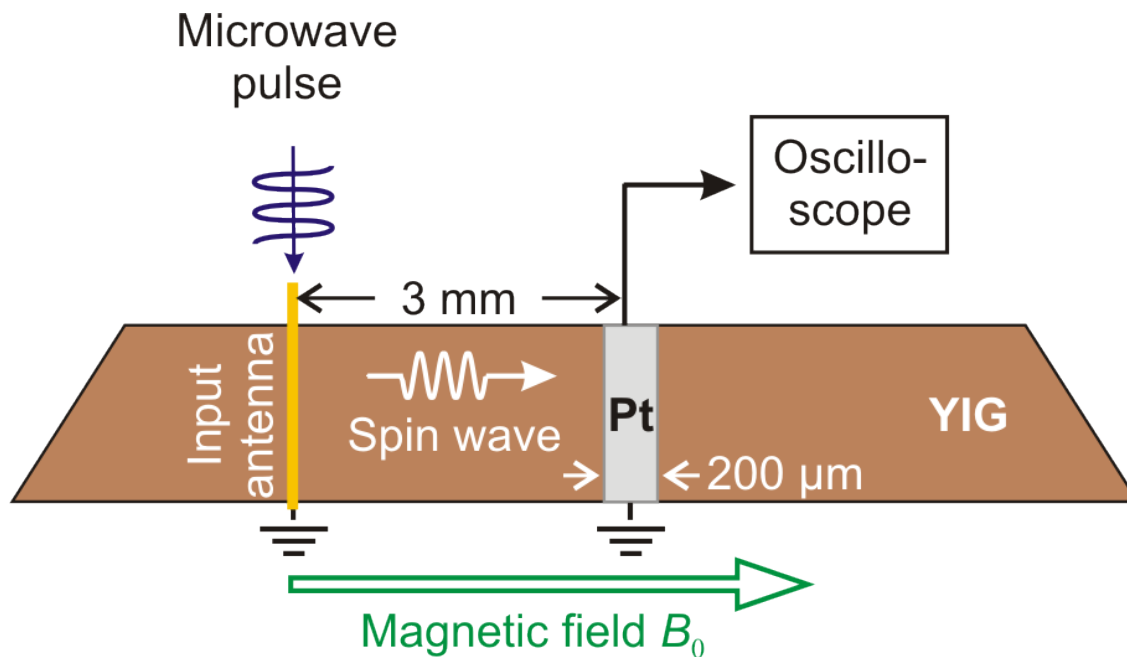


But dipolar-exchange waves have zero velocities  $\rightarrow$  no spin transport



Spin pumping by propagating magnons?

Spin-wave source and Pt detector are separated in space



### Parameters:

YIG thickness: 2.1 μm

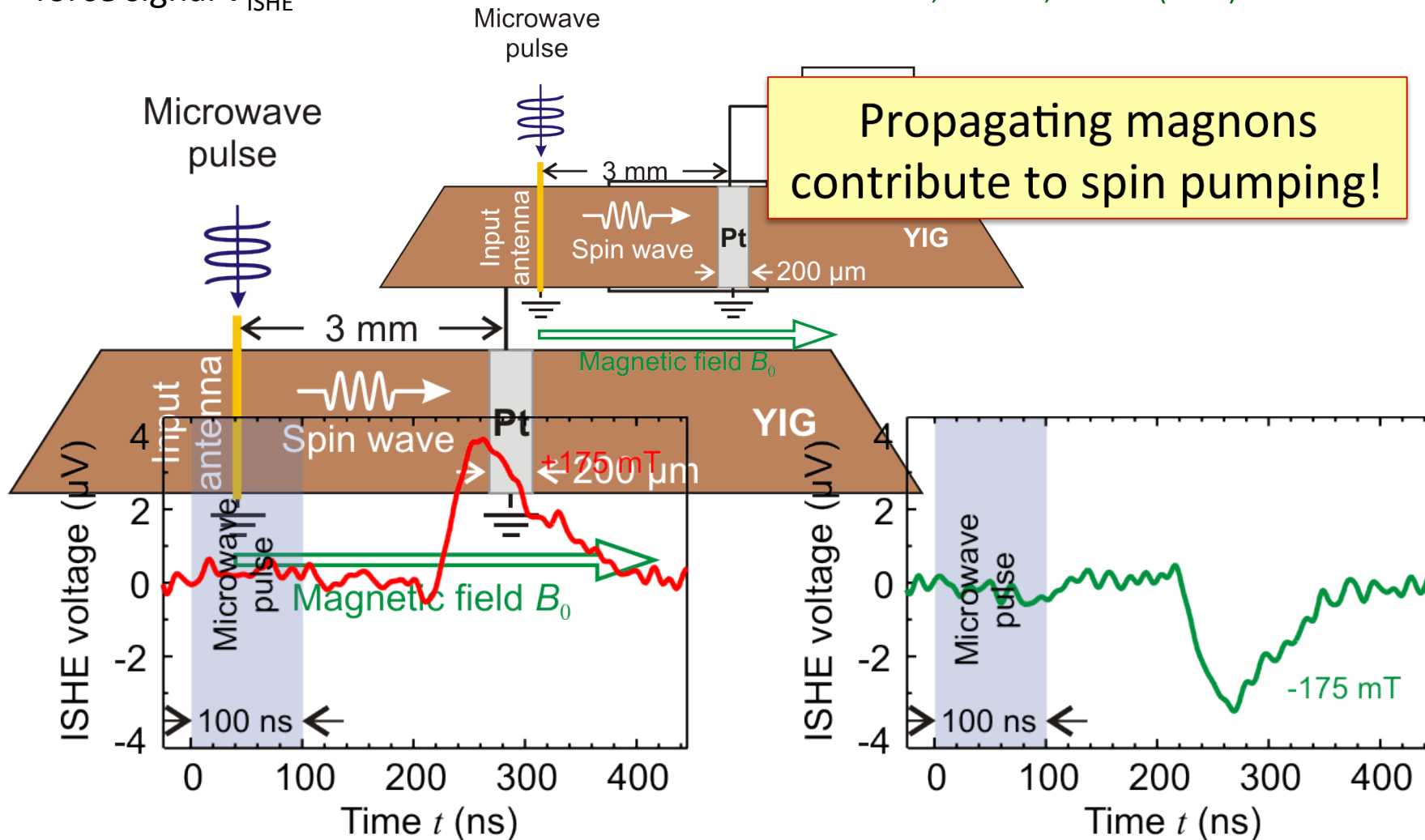
Pt size: 3 x 0.2 mm

Pt thickness: 10 nm

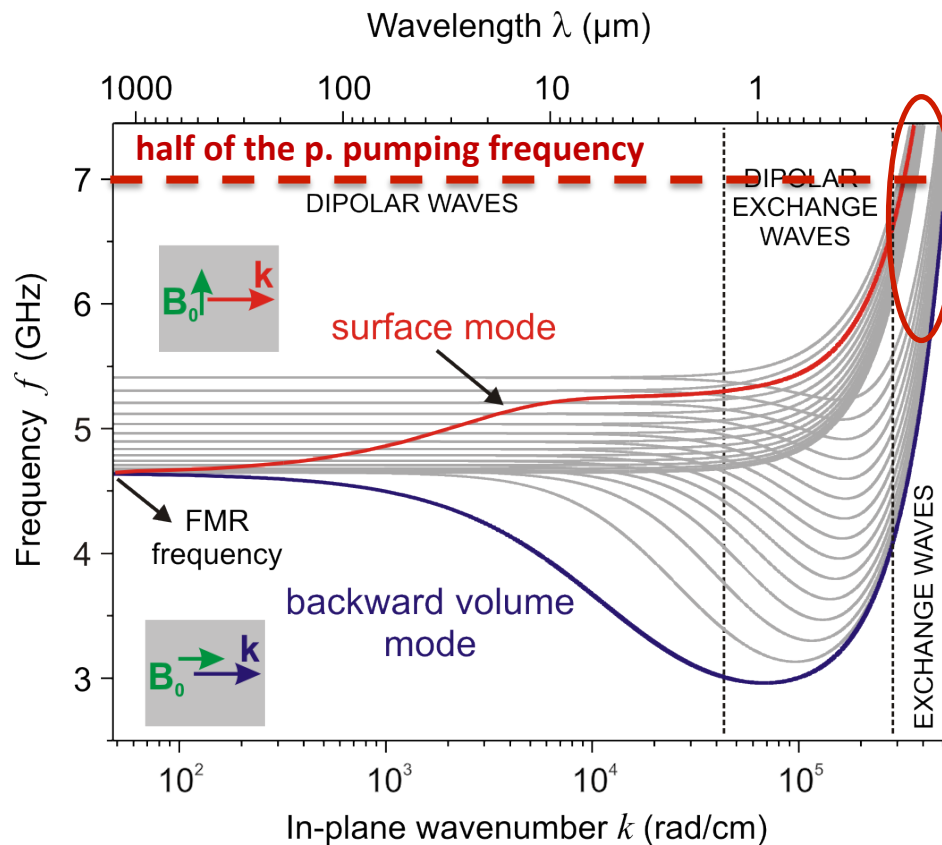
Signal frequency: 7 GHz

Waveforms of the electromotive force signal  $V_{\text{ISHE}}$

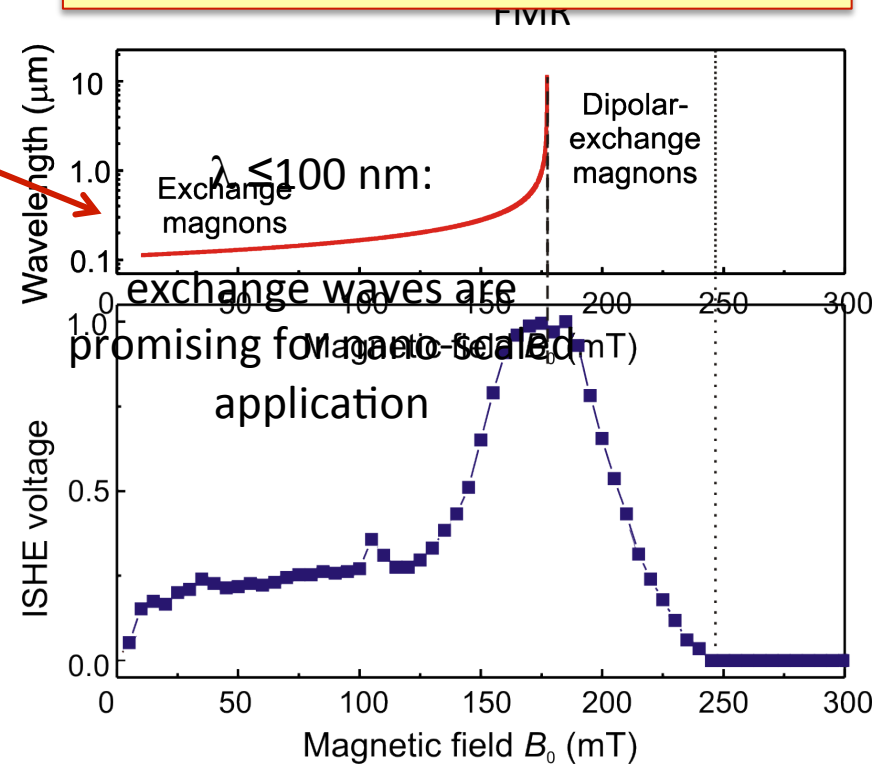
Chumak et al., APL **100**, 082405 (2012)



Parametric pumping at 14 GHz



Exchange magnons  
contribute to spin pumping!



Sandweg et al., PRL **106**, 216601 (2011)

Kurebayashi, Dzyapko et al., APL **99**, 162502 (2011)

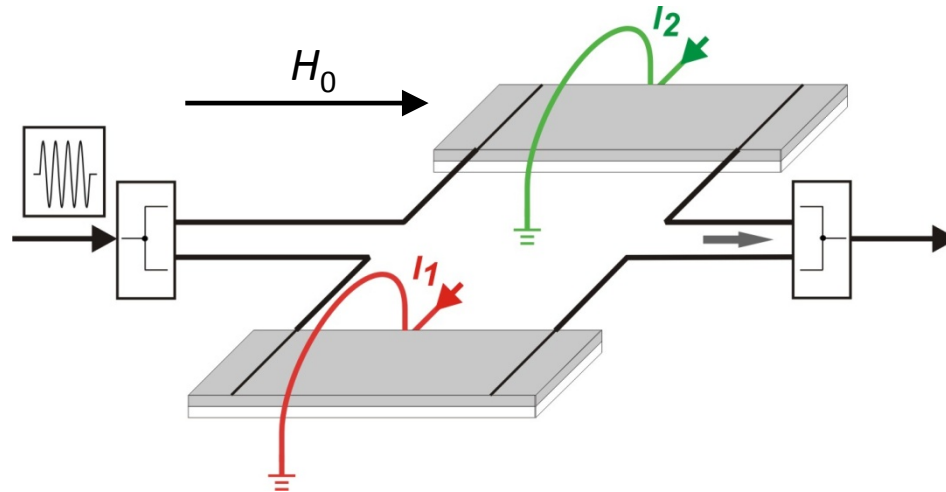
Ando et al., APL **99**, 092510 (2011)

## III. Data processing using magnons



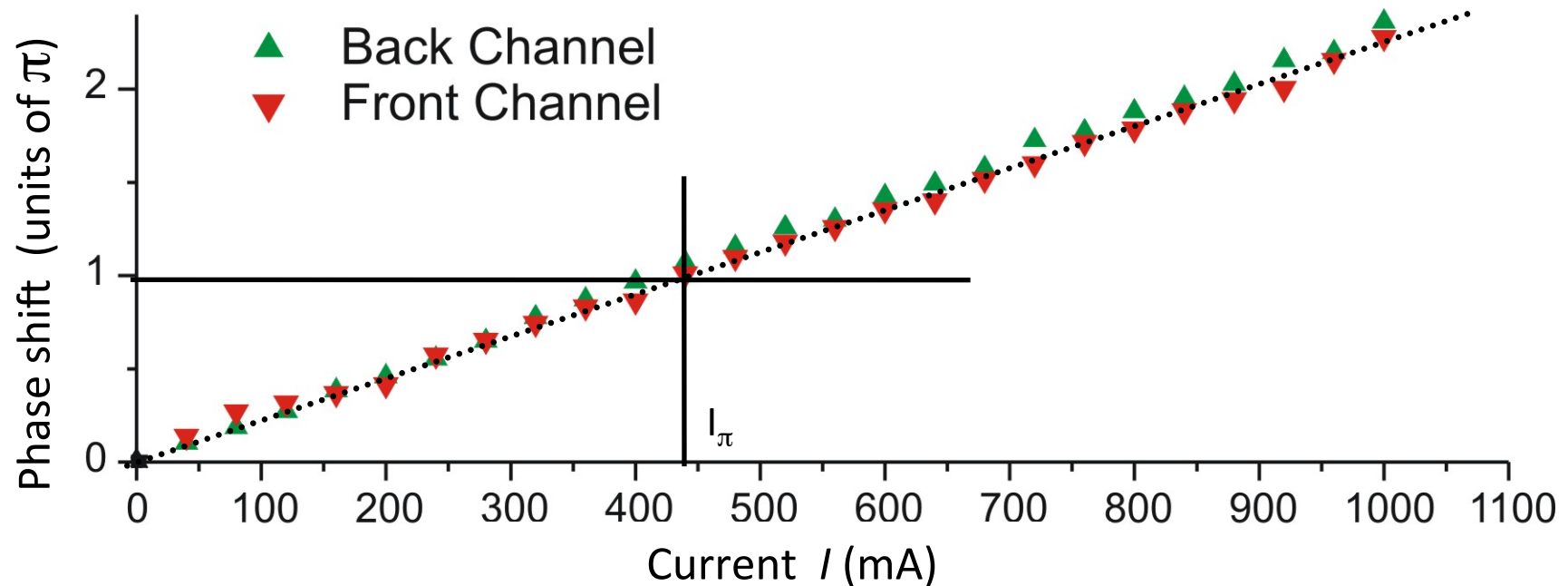
Spin-wave logic gates

# Mach-Zehnder interferometer based spin-wave logic gate



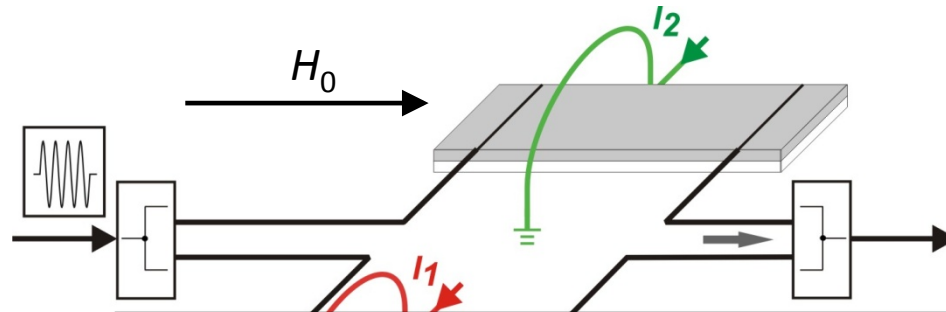
Kostylev et al., **APL** **87**, 153501 (2005)

Schneider et al., **APL** **92**, 022505 (2008)





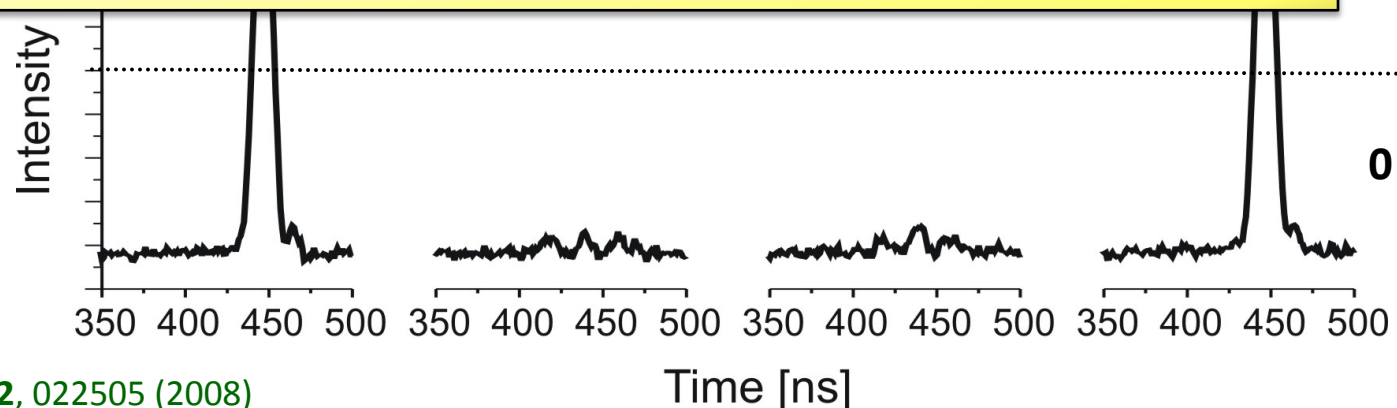
# Mach-Zehnder interferometer based spin-wave logic gate



| Inputs      |               | Output |
|-------------|---------------|--------|
| A ( $I_1$ ) | B ( $I_2$ )   |        |
| 0 (0)       | 0 (0)         | 1      |
| 0 (0)       | 1 ( $I_\pi$ ) | 0      |
| 1           | 0             | 0      |
| 1           | 1             | 1      |

Input: DC pulses  
Output: magnon packets

**How to control one magnon by another?**

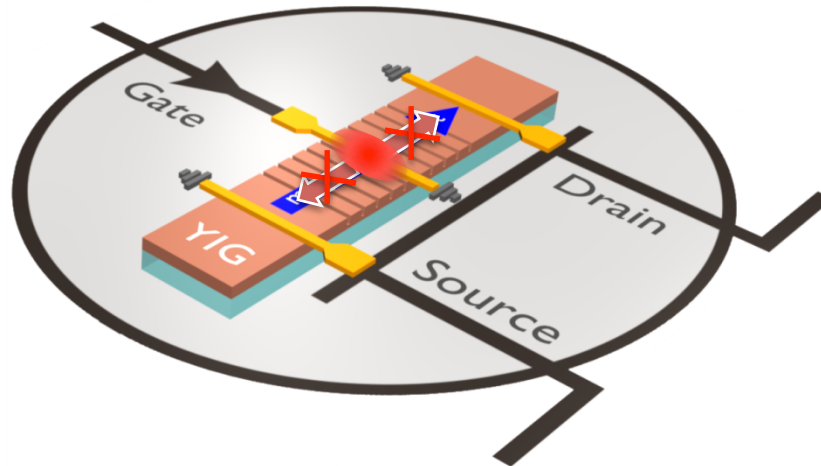


## III. Data processing using magnons

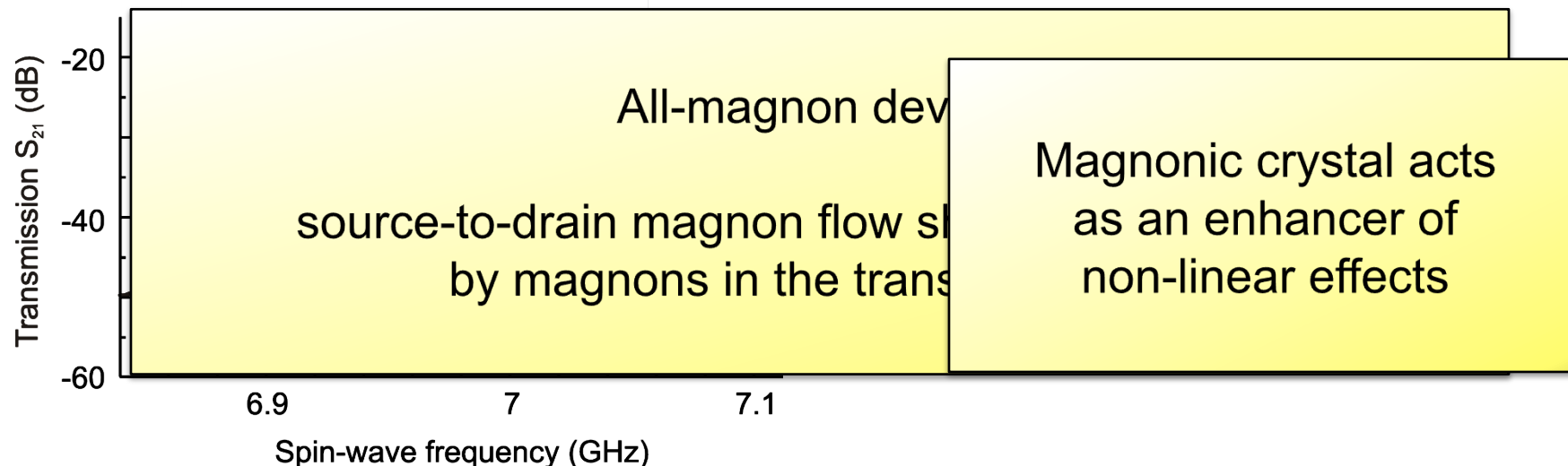
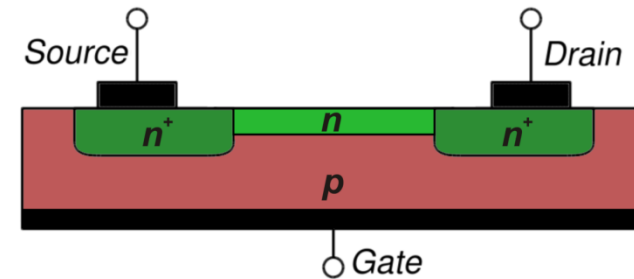
- Spin-wave logic gates



Magnon transistor



Semiconductor field-effect transistor:



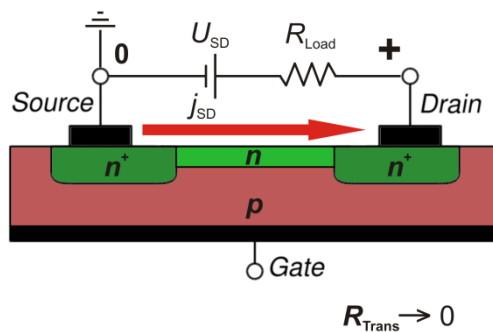
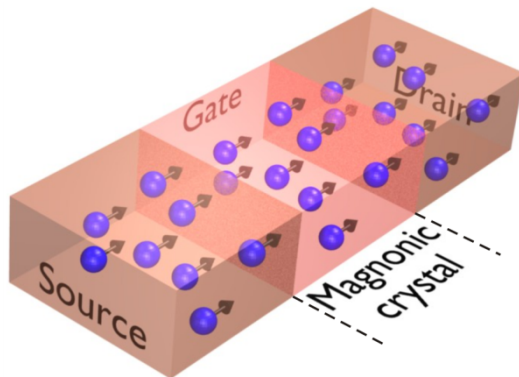
A.V. Chumak et al., *Nature Commun.*, in press (2014)

# Magnon transistor

**Opened:  $R \rightarrow 0$**

Gate magnon density

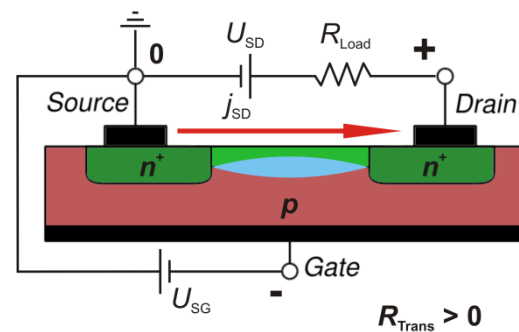
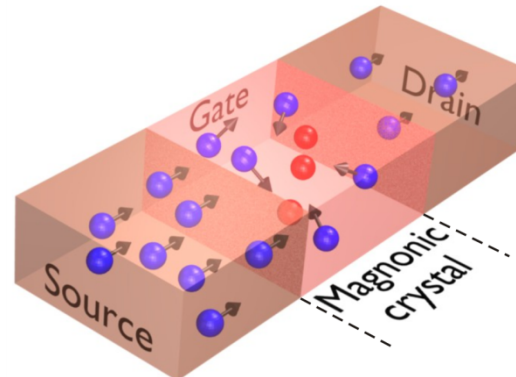
$$n_G = 0$$



**Semi-closed:  $R > 0$**

Gate magnon density

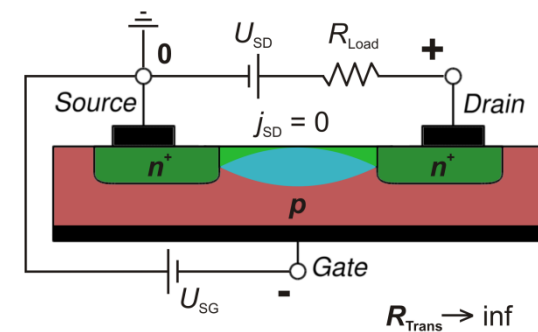
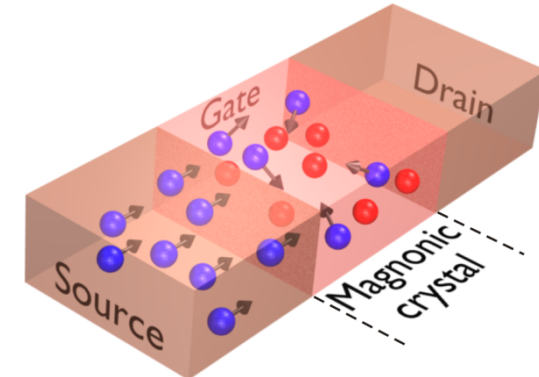
$$n_G > 0$$



**Closed:  $R \rightarrow \infty$**

Gate magnon density

$$n_G \gg 0$$



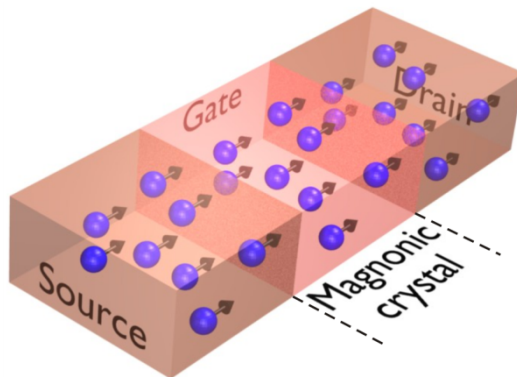
A.V. Chumak et al., Nature Commun., in press (2014)

# Magnon transistor

**Opened:  $R \rightarrow 0$**

Gate magnon density

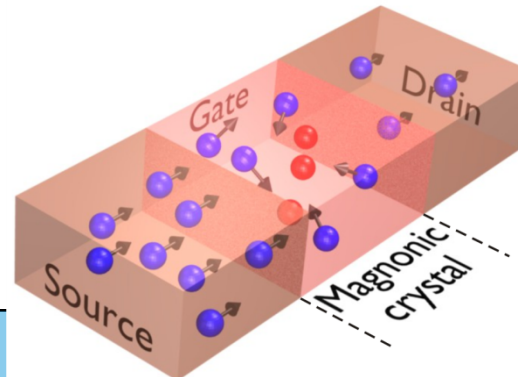
$$n_G = 0$$



**Semi-closed:  $R > 0$**

Gate magnon density

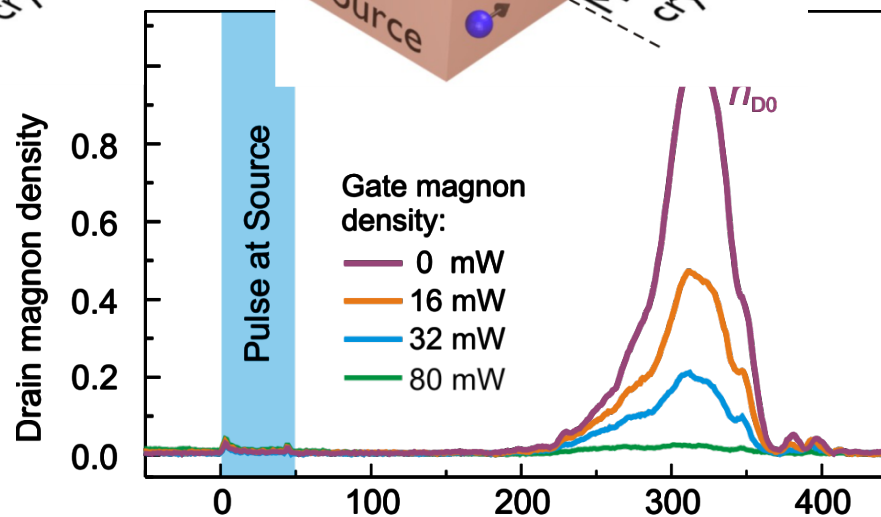
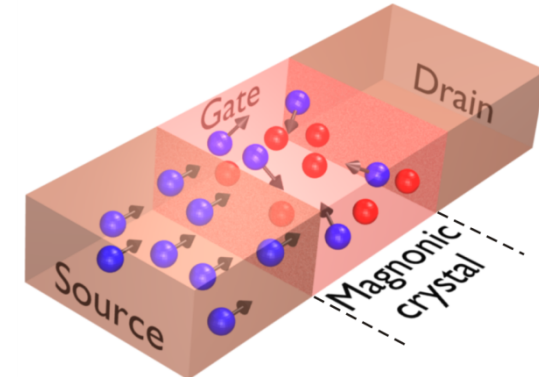
$$n_G > 0$$



**Closed:  $R \rightarrow \infty$**

Gate magnon density

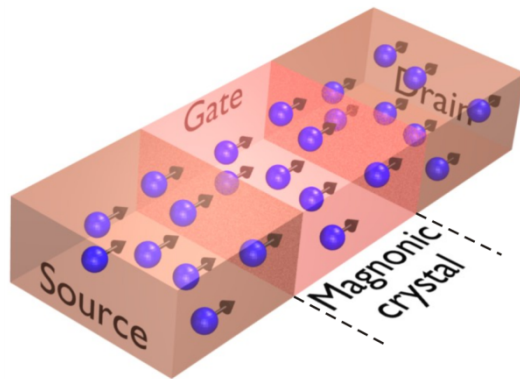
$$n_G \gg 0$$



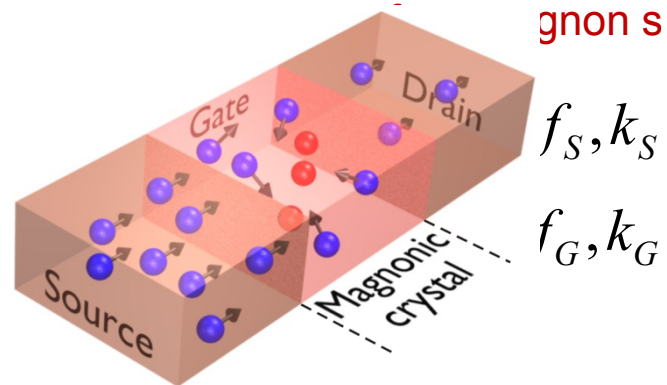
A.V. Chumak et al., Nature Commun., in press (2014)

# Magnon transistor

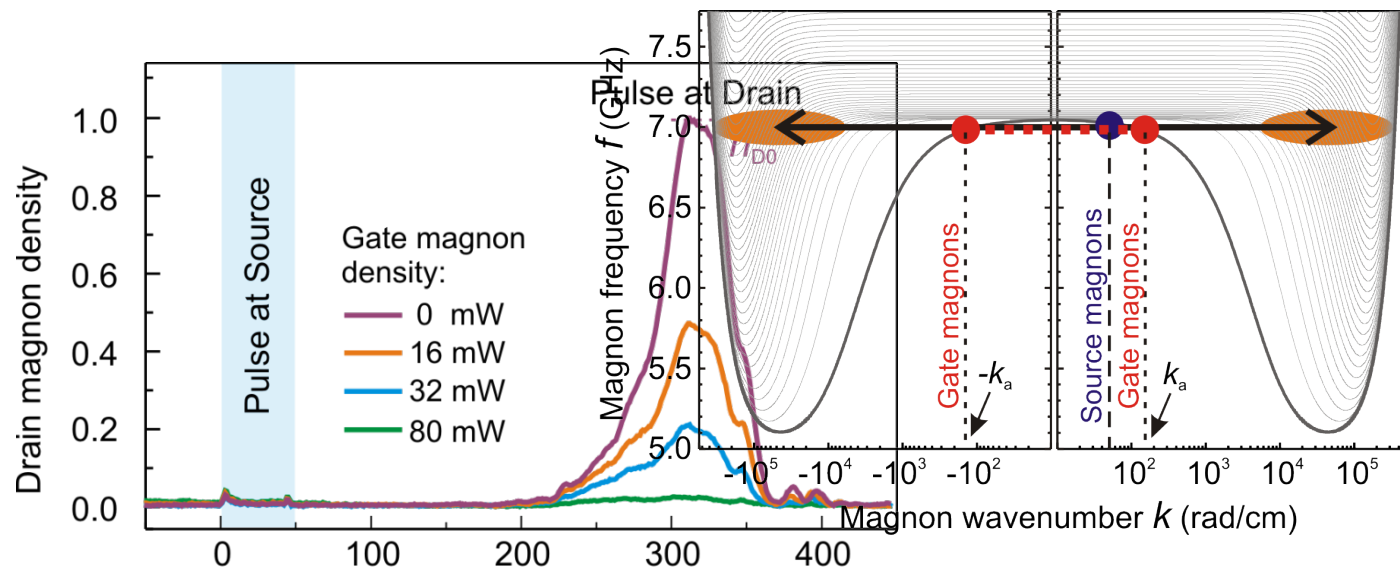
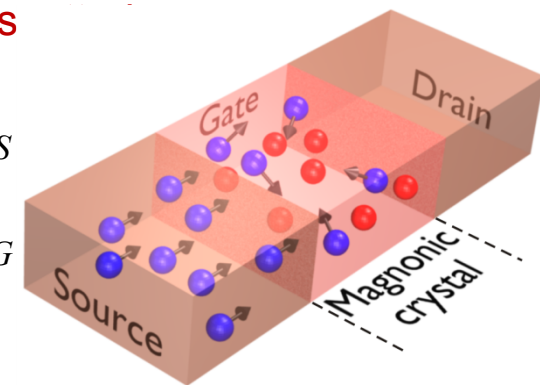
**Opened:  $R \rightarrow 0$**



**Semi-closed:  $R > 0$**

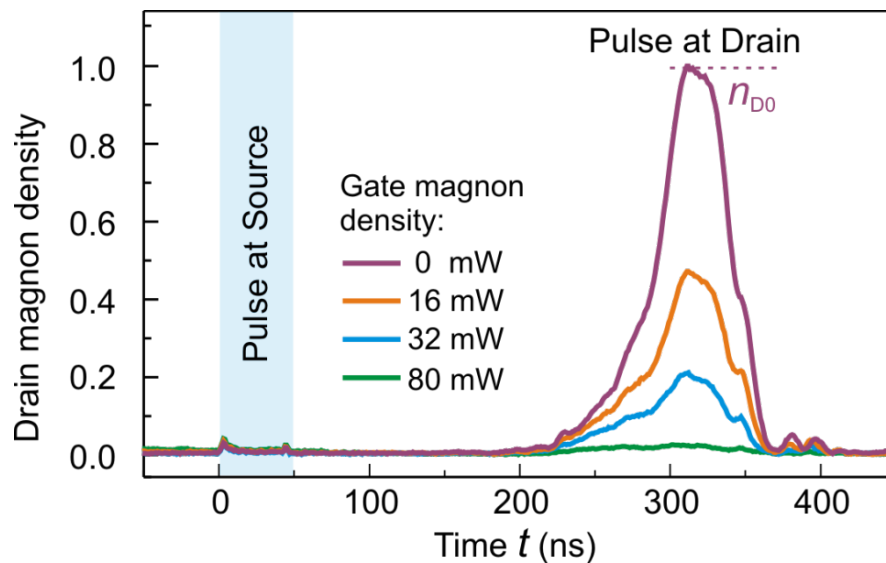
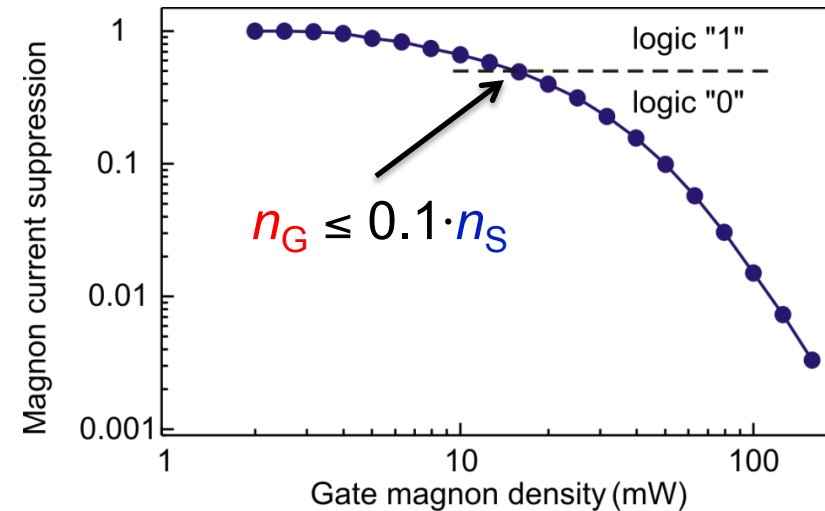
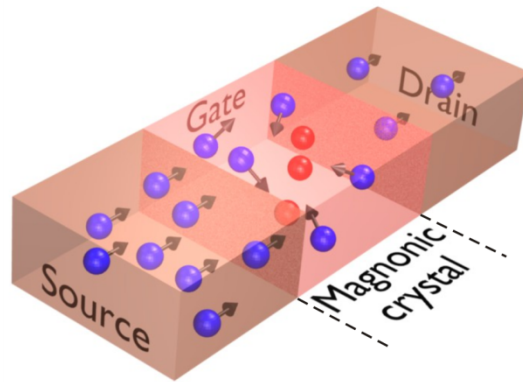


**Closed:  $R \rightarrow \infty$**




A.V. Chumak et al., Nature Commun., in press (2014) Time  $t$  (ns)

# Magnon transistor



“magnon control by magnon”  
 principle was realized:  
 data can be processed on  
 the same magnetic chip

## III. Data processing using magnons

- Spin-wave logic gates
  - Magnon transistor
-  Magnon majority gate

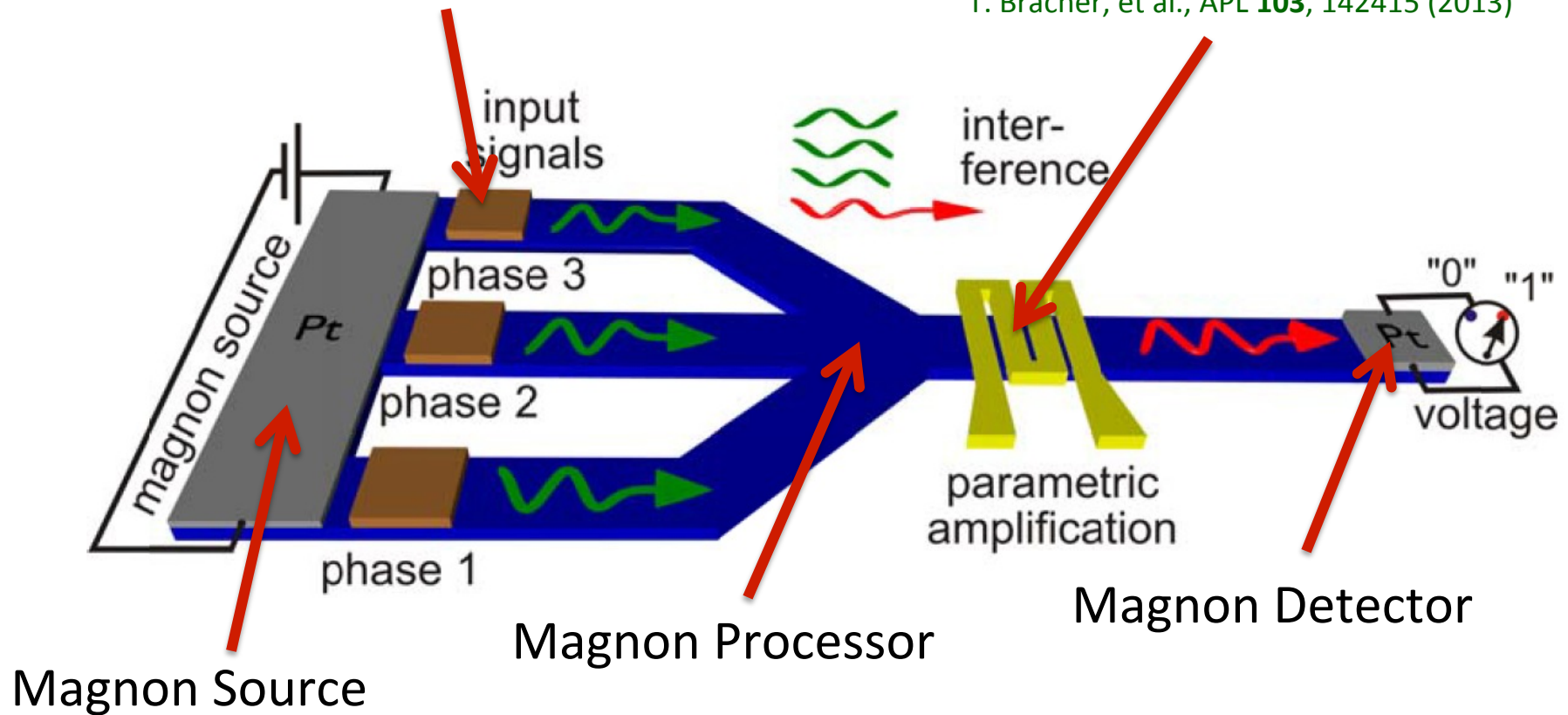


## Phase Shifter

T. Neumann, et al. APL **94**, 042503 (2009)  
 M.P. Kostylev, et al., PRB **76**, 184419 (2007)

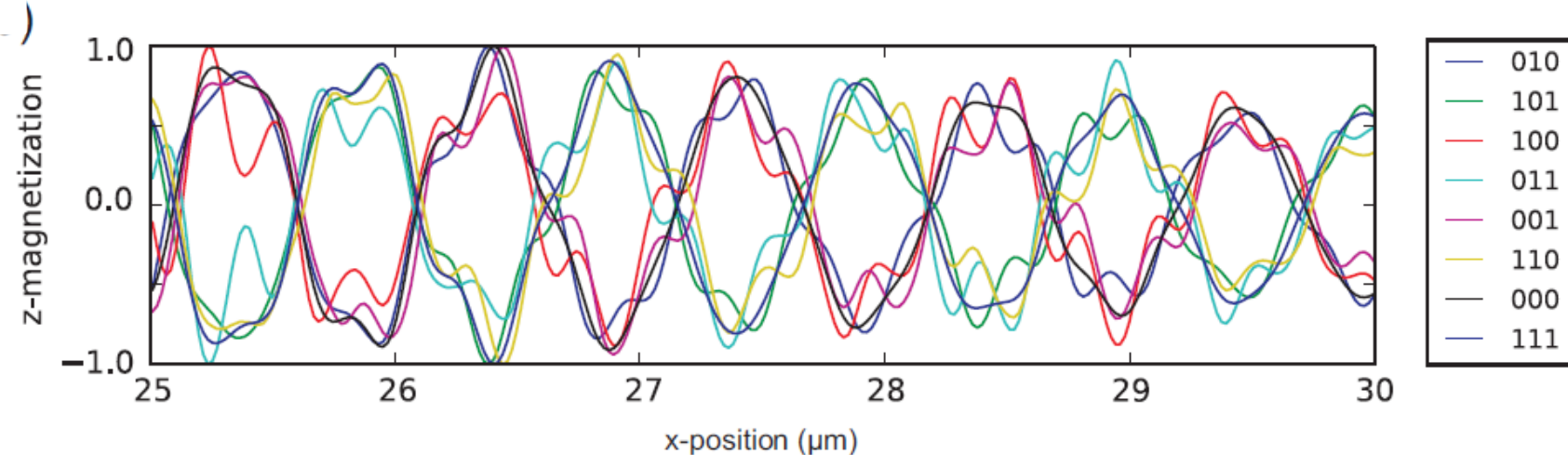
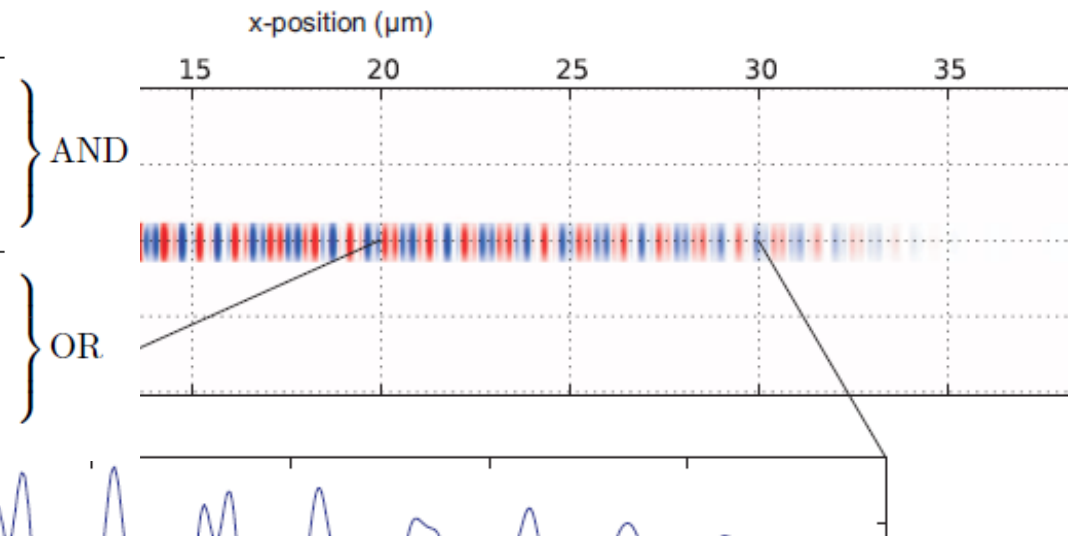
## Parametric Amplifier

T. Brächer, et al. APL **104**, 092418 (2014)  
 T. Brächer, et al., APL **103**, 142415 (2013)



# Majority gates: Simulations

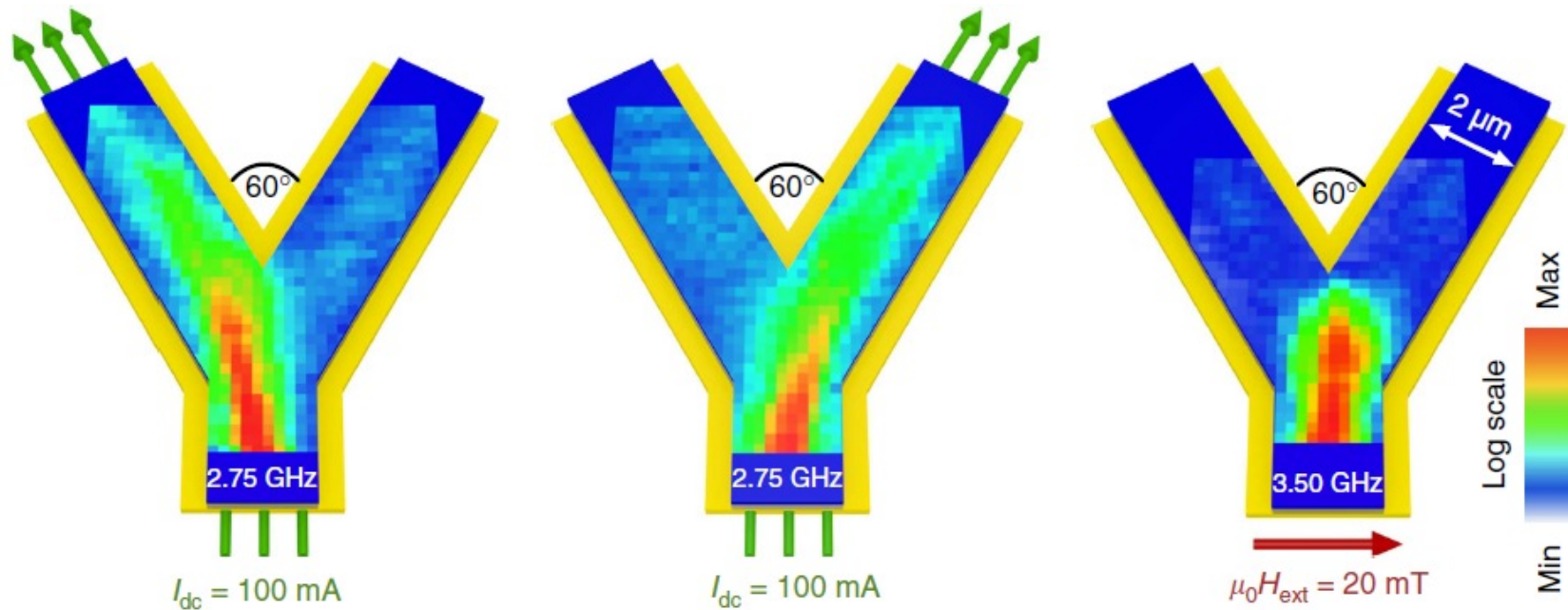
| Input 1 | Input 2 | Input 3 | Output |
|---------|---------|---------|--------|
| Signal  | Signal  | Control |        |
| 0       | 0       | 0       | 0      |
| 1       | 0       | 0       | 0      |
| 0       | 1       | 0       | 0      |
| 1       | 1       | 0       | 1      |
| 0       | 0       | 1       | 0      |
| 1       | 0       | 1       | 1      |
| 0       | 1       | 1       | 1      |
| 1       | 1       | 1       | 1      |



## III. Data processing using magnons

- Spin-wave logic gates
- Magnon transistor
- Magnon majority gate
- ➔ Magnon multiplexer

# Magnon multiplexer



Spin-wave propagation path was controlled by a DC current

- **Classical Computing**
  - Scalar variable
  - Boolean logic
- **Wave Computing**
  - Vector variable
  - Special task data processing
- **Quantum Computing**
  - Vector state variable
  - Entanglement



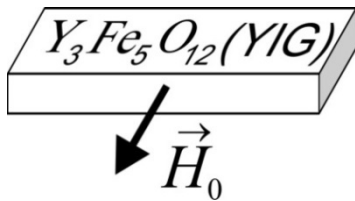
## IV. Magnonic supercurrents

Main idea: find coherent, propagating modes for information transfer, which are free of dissipation (apart from magnon-phonon and magnon-electron coupling)

- No two-magnon, three-magnon, four-magnon scattering etc.
- Bose-Einstein Condensation (BEC) of magnons
- Phonon-coupled BEC of magnons

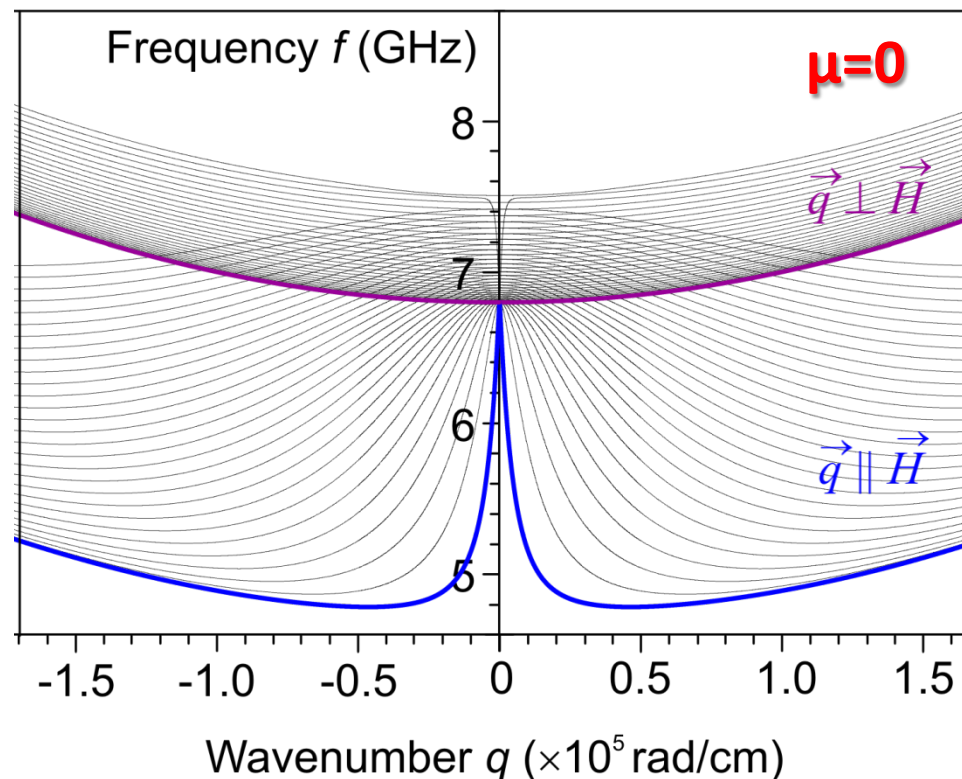
# Magnon distribution

Magnons are **bosons** ( $s=1$ )  
and thus as any quasi-particles  
are described by Bose-Einstein distribution  
with **zero chemical potential**



**Bose-Einstein  
distribution**

$$\rho(f) = \frac{D(f)}{\exp\left(\frac{hf - \mu}{k_B T}\right) - 1}$$

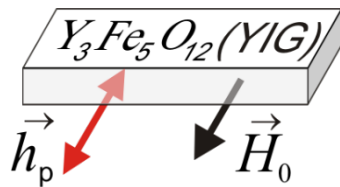


# Control of magnon gas density by parametric pumping

Energy and  
momentum  
conservation laws

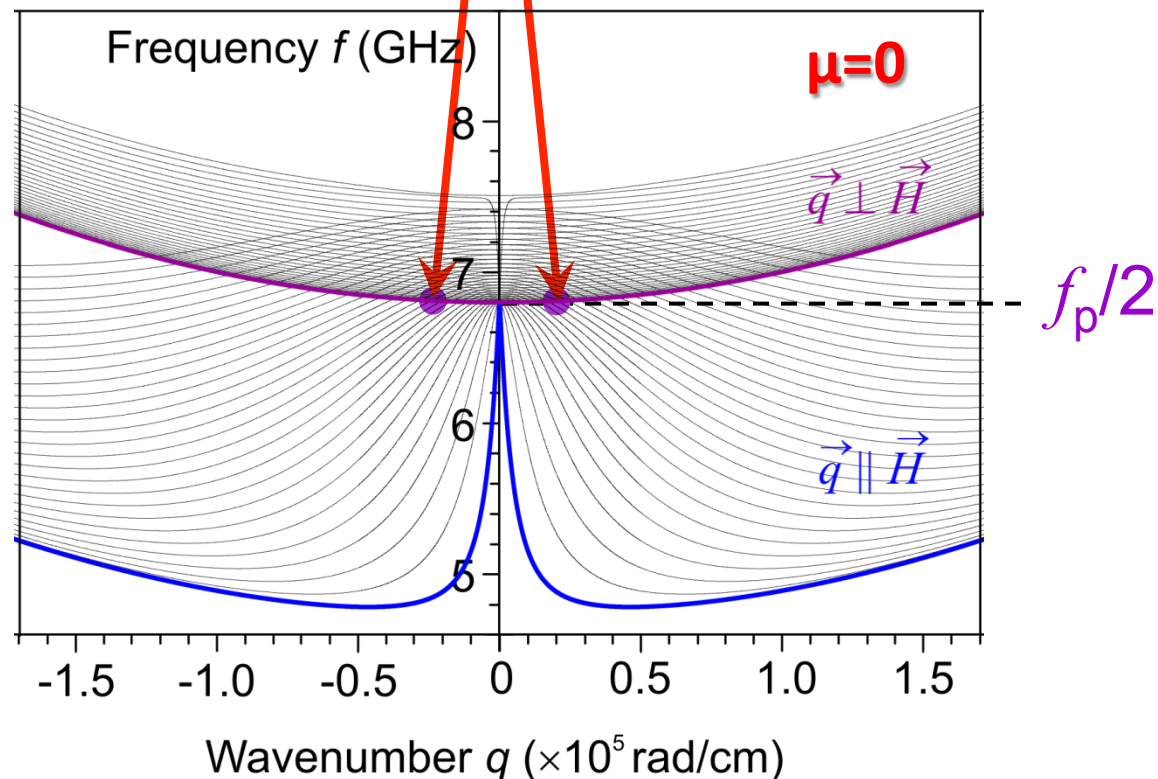
$$\begin{cases} \vec{q}_{sw} + \vec{q}'_{sw} = \vec{q}_p \approx 0 \\ f_{sw} + f'_{sw} = f_p \end{cases}$$

Parametric pumping  
by electromagnetic wave  
at microwave frequency



Bose-Einstein  
distribution

$$\rho(f) = \frac{D(f)}{\exp\left(\frac{hf - \mu}{k_B T}\right) - 1}$$



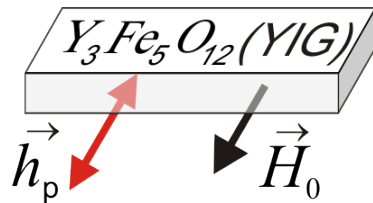


# Control of magnon gas density by parametric pumping

Energy and momentum conservation laws

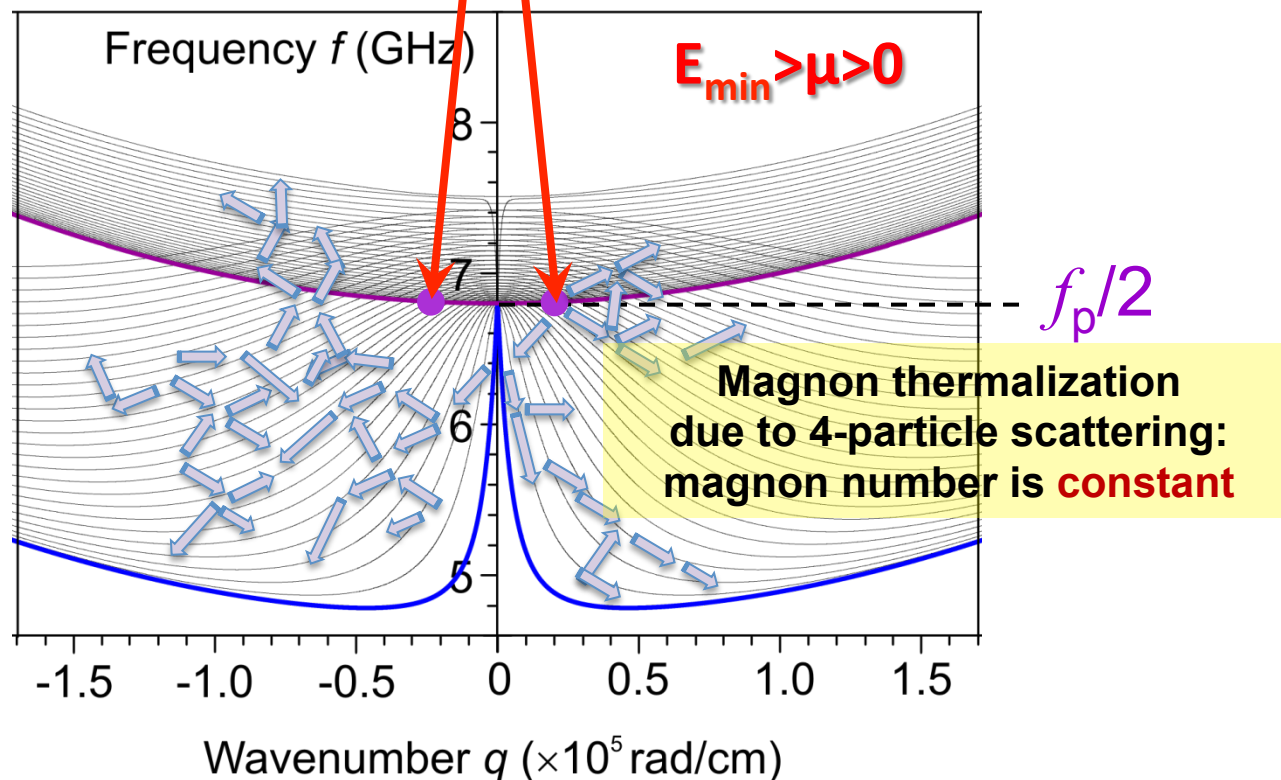
$$\begin{cases} \vec{q}_{sw} + \vec{q}'_{sw} = \vec{q}_p \approx 0 \\ f_{sw} + f'_{sw} = f_p \end{cases}$$

$f_p$  Parametric pumping  
by electromagnetic wave  
at microwave frequency



**Bose-Einstein distribution**

$$\rho(f) = \frac{D(f)}{\exp\left(\frac{hf - \mu}{k_B T}\right) - 1}$$

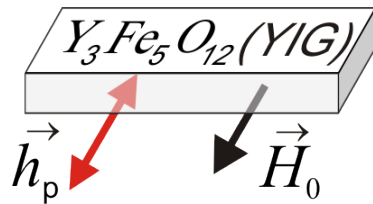


# Bose-Einstein condensate of magnons

Energy and momentum conservation laws

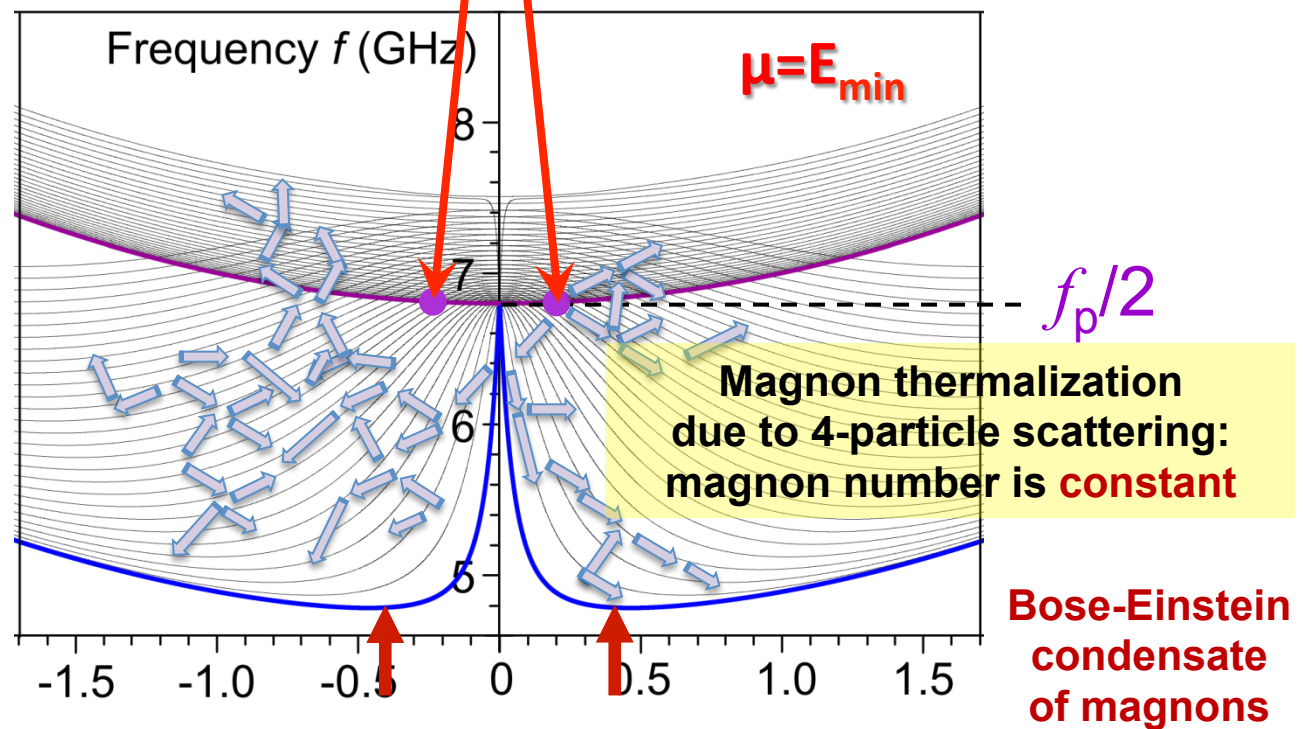
$$\begin{cases} \vec{q}_{sw} + \vec{q}'_{sw} = \vec{q}_p \approx 0 \\ f_{sw} + f'_{sw} = f_p \end{cases}$$

$f_p$  Parametric pumping by electromagnetic wave at microwave frequency



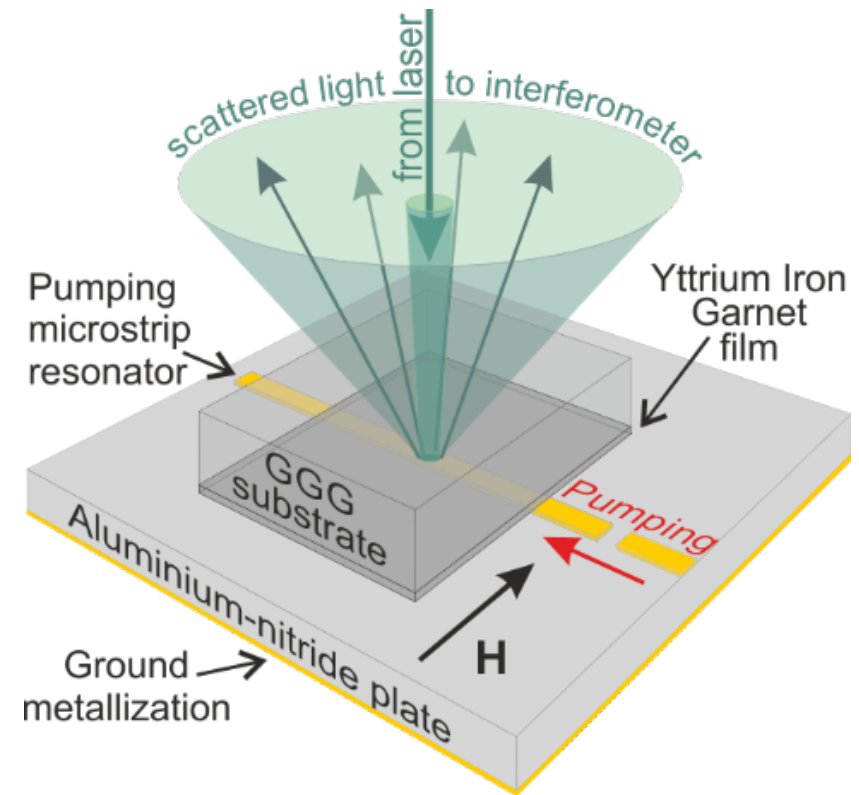
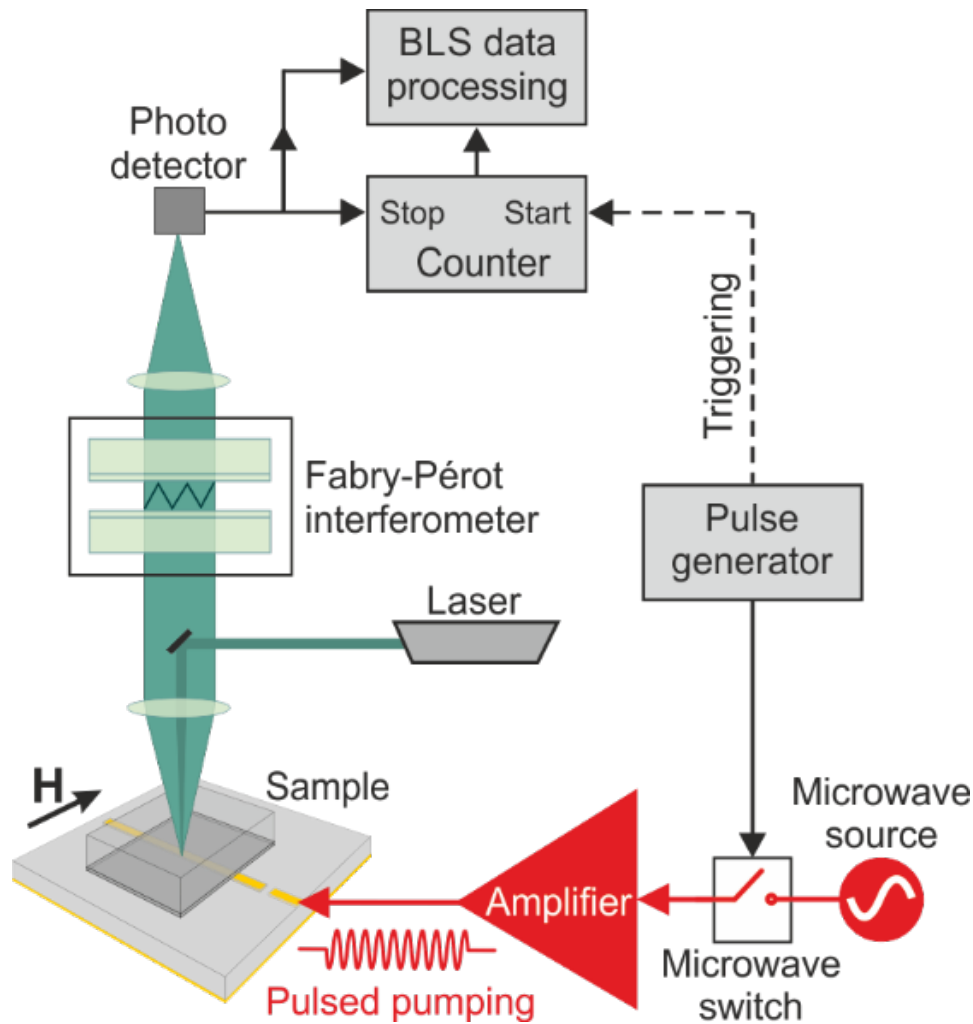
**Bose-Einstein distribution**

$$\rho(f) = \frac{D(f)}{\exp\left(\frac{hf - \mu}{k_B T}\right) - 1}$$

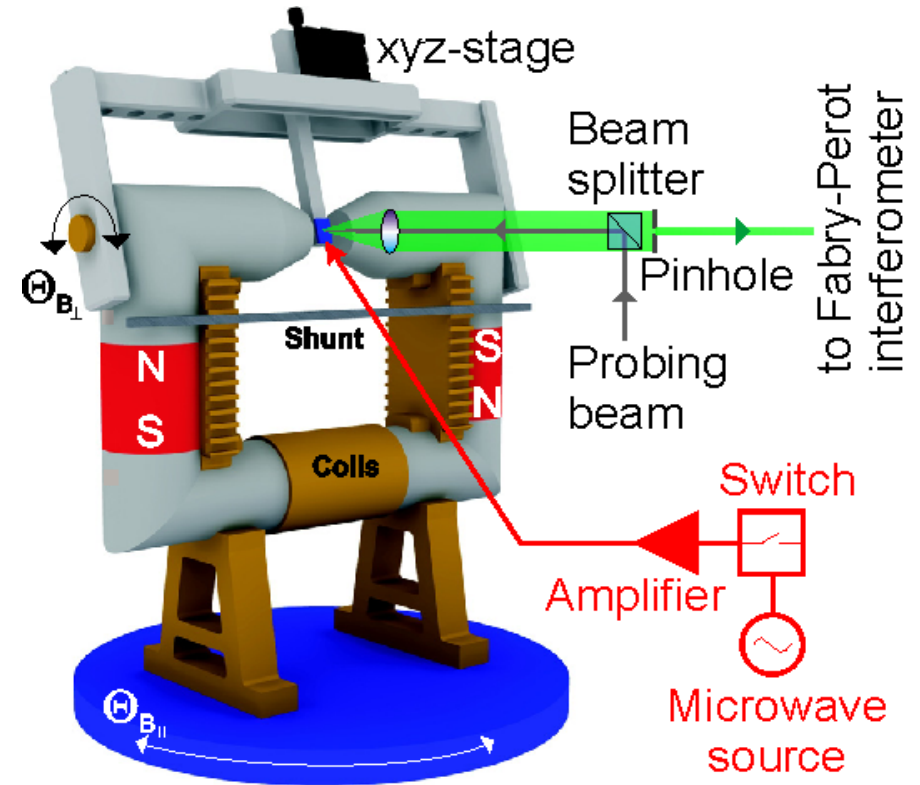
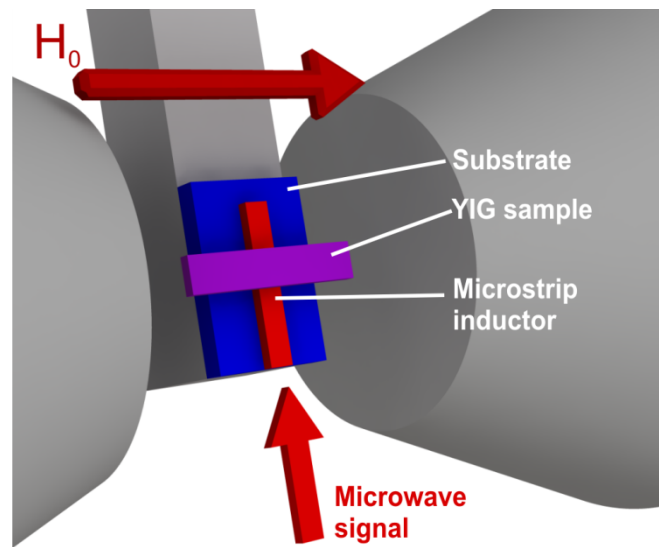


Demokritov et al., Nature **443**, 430 (2006) Wavenumber  $q$  ( $\times 10^5$  rad/cm)

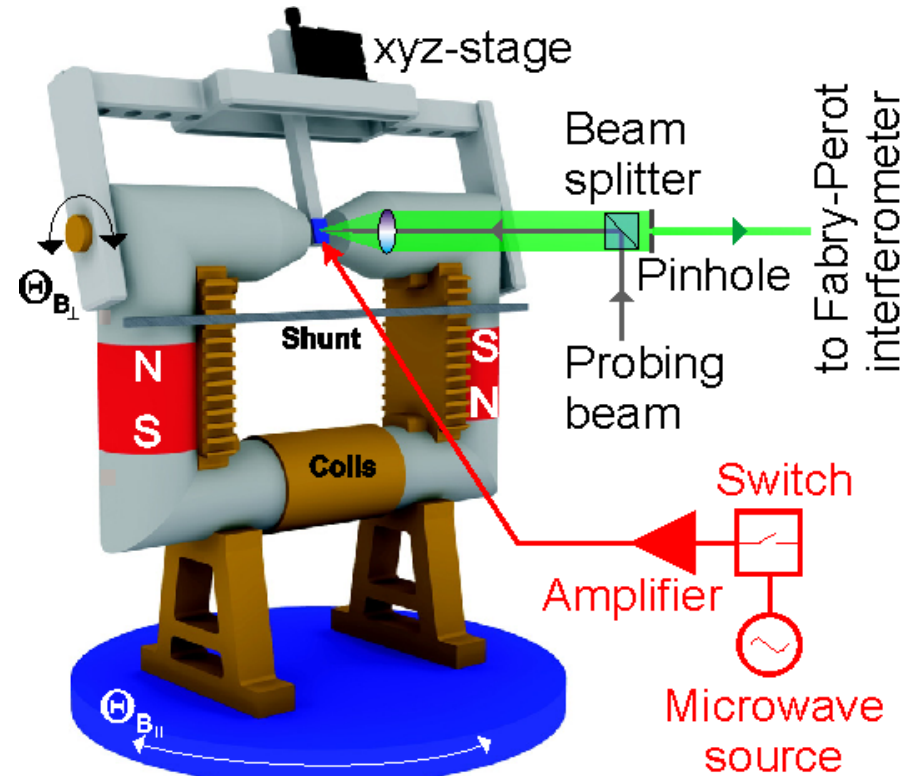
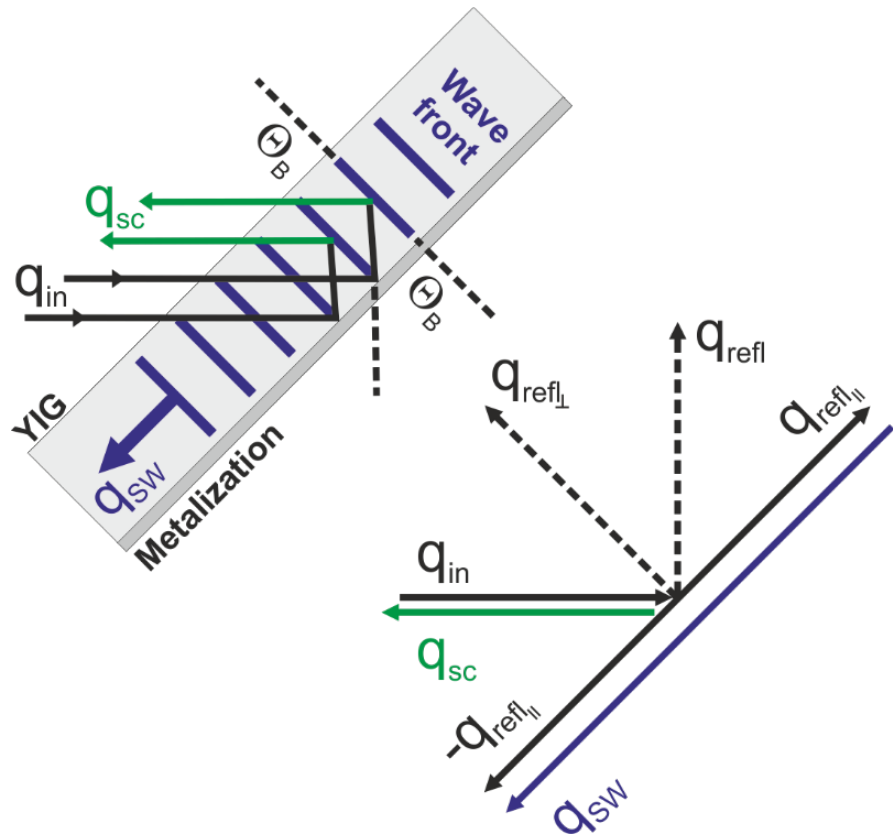
# Time-resolved Brillouin light scattering spectroscopy



# Wave-vector resolved BLS setup

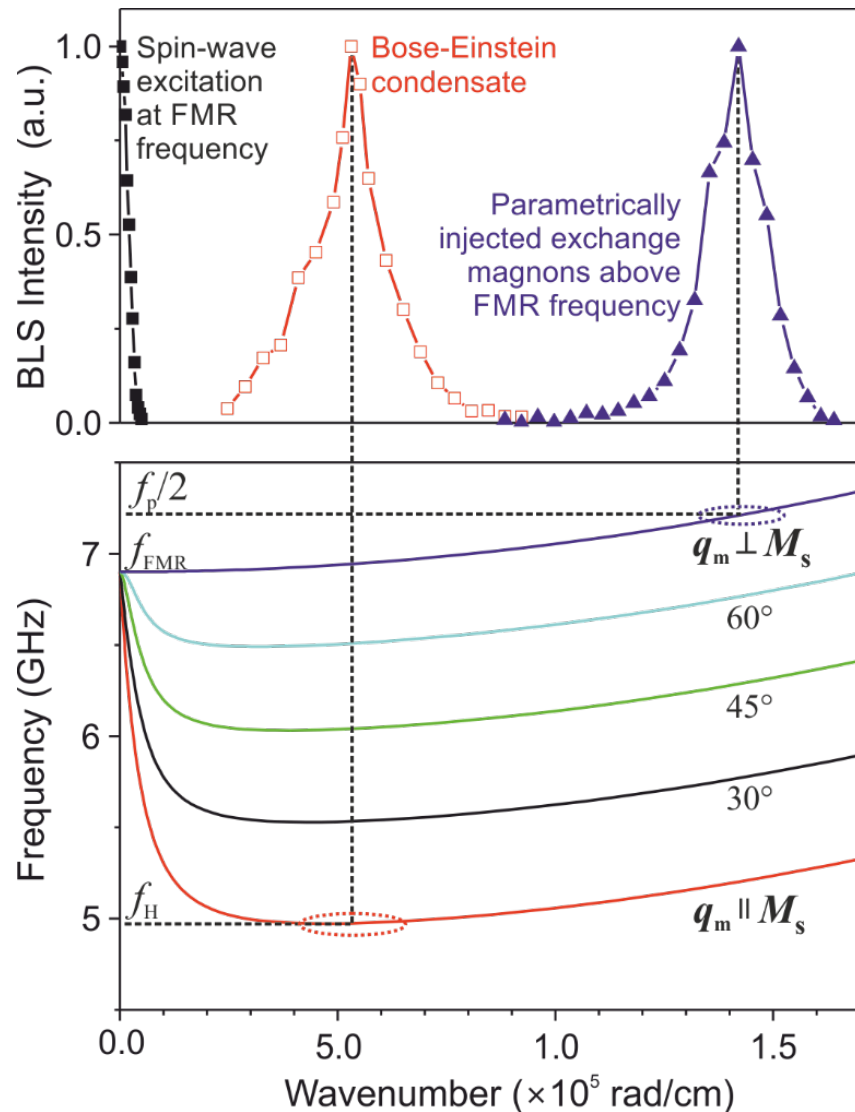


# Wave-vector resolved BLS setup

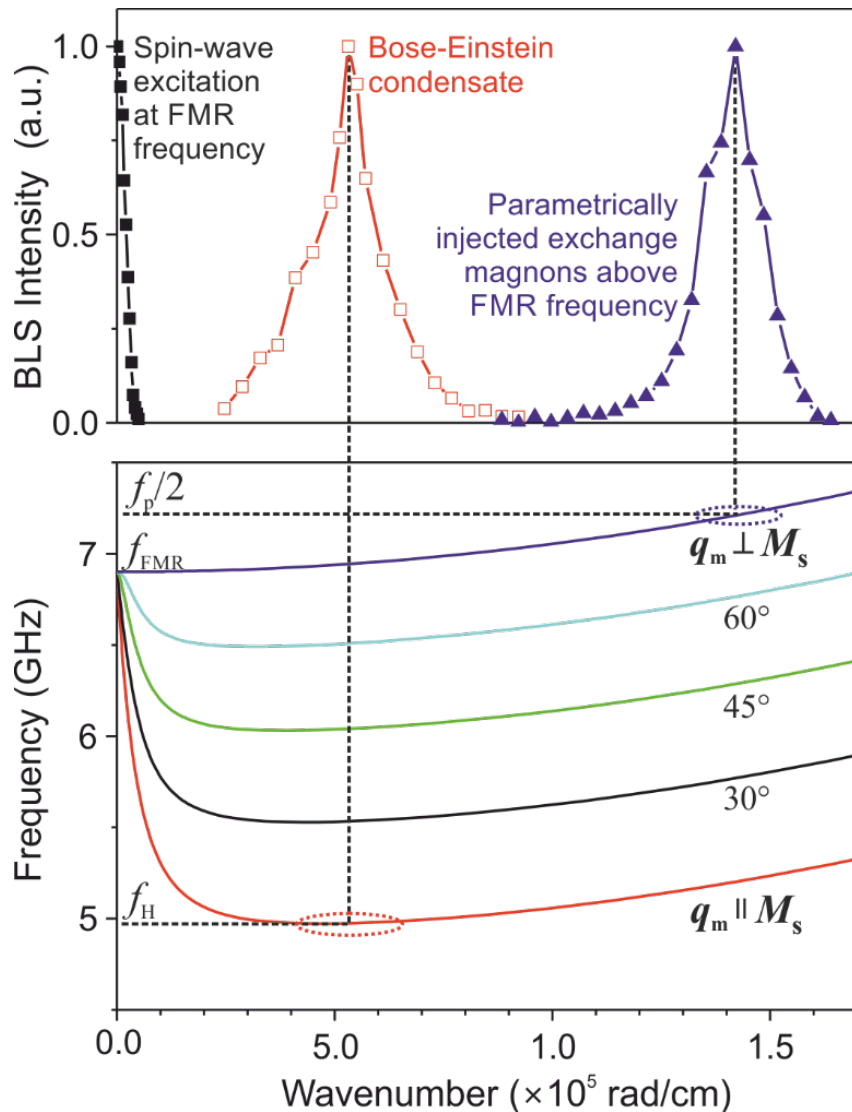


Detection of wave numbers  $\leq 2.36 \times 10^5 \text{ rad/cm}$   
 Wavenumber resolution  $4.1 \times 10^3 \text{ rad/cm}$

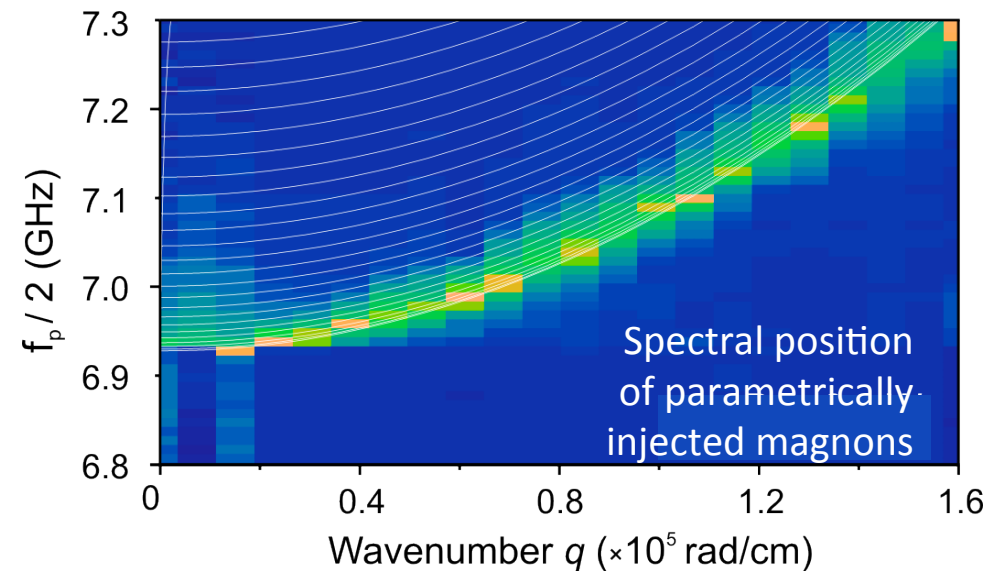
Time resolution 250 ps  
 Frequency resolution 150 MHz  
 Spatial resolution 25  $\mu\text{m}$



Sandweg *et al.*, Rev. Scientific Instr. **81**, 073902 (2010)



Serga *et al.*, Phys. Rev. B **86**, 134403 (2012)

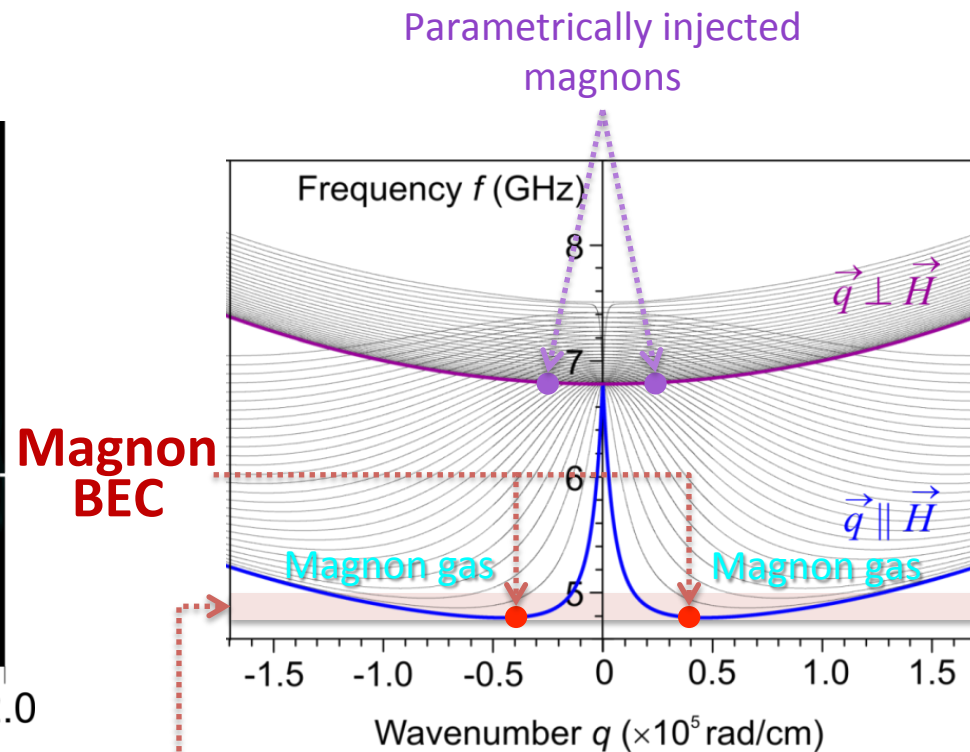
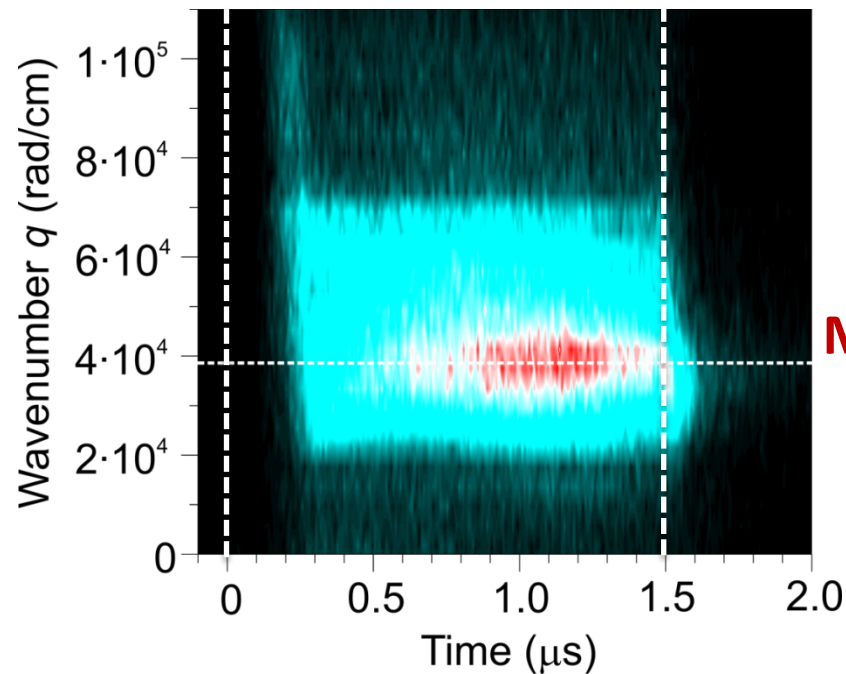


Sandweg *et al.*, Rev. Scientific Instr. **81**, 073902 (2010)

# Gaseous magnons and magnon BEC in a phase space

## Bose-Einstein magnon condensate

Narrow pumping area  
50  $\mu\text{m}$  width



Frequency region of interest

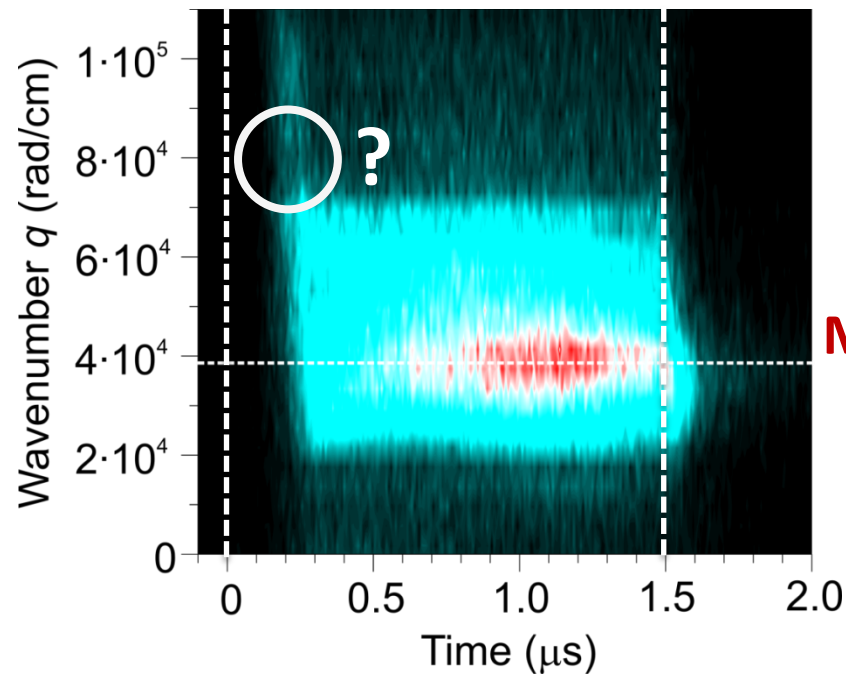
Serga et al., Nat. Commun. **5**, 4452 (2014)




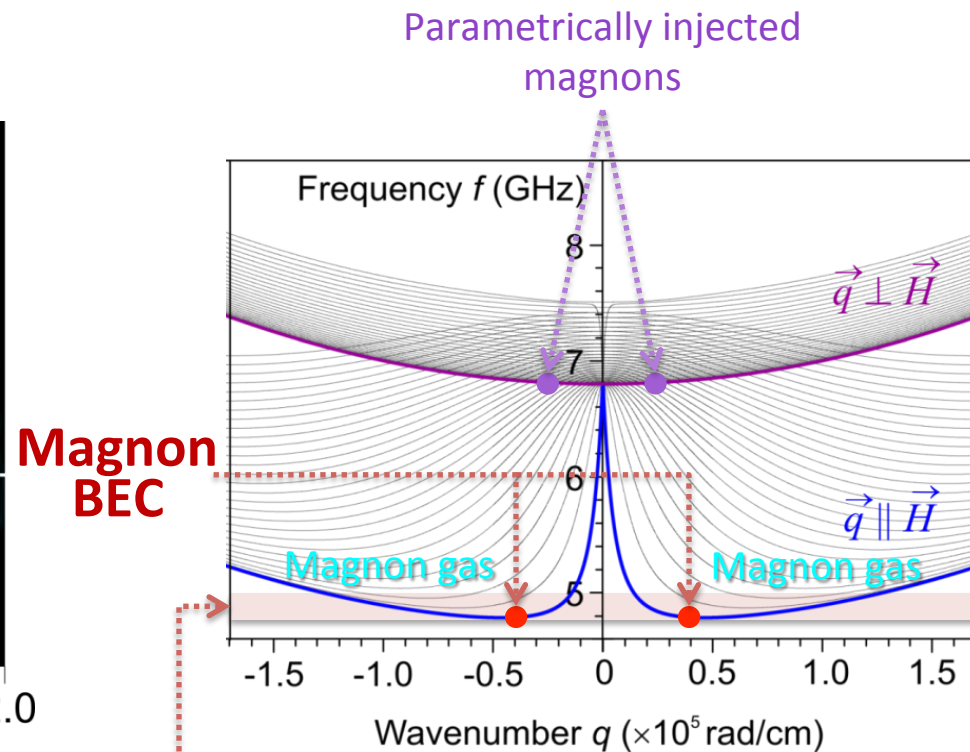
# Gaseous magnons and magnon BEC in a phase space

## Bose-Einstein magnon condensate

Narrow pumping area  
50  $\mu\text{m}$  width



BLS intensity  
(arb. units)  
0  1



Frequency region of interest

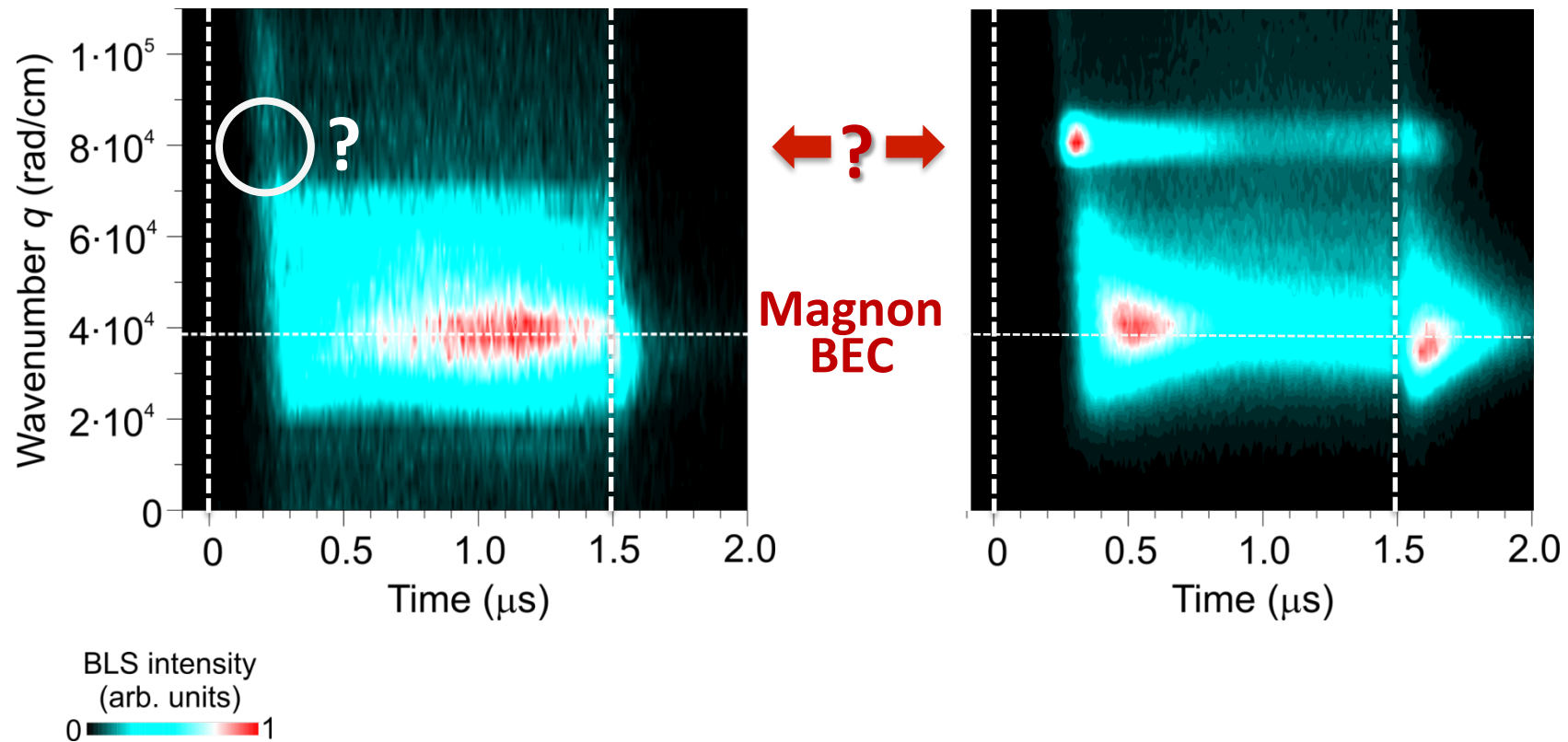
Serga et al., Nat. Commun. **5**, 4452 (2014)

# Gaseous magnons and magnon BEC in a phase space

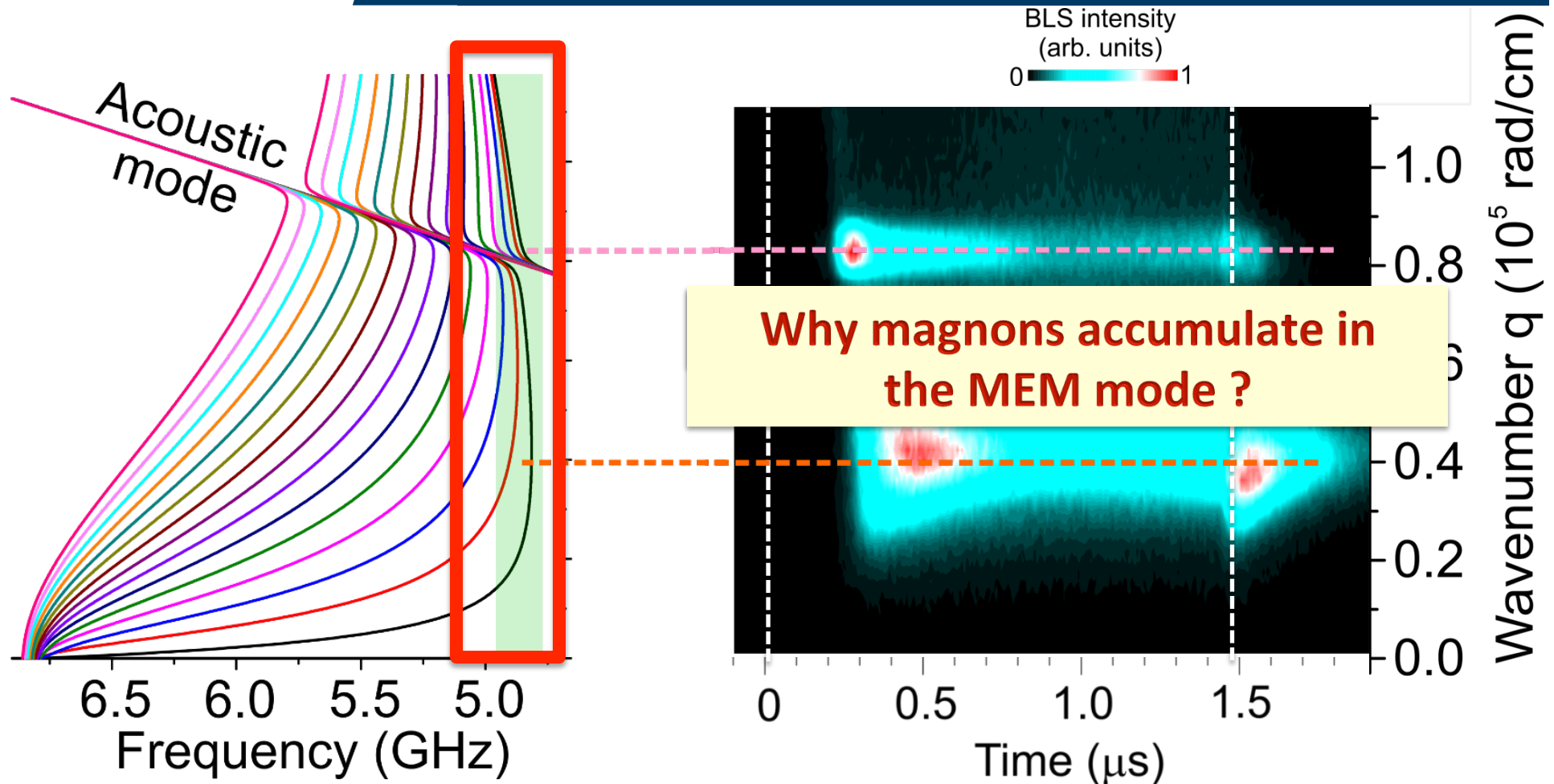
## Bose-Einstein magnon condensate

Narrow pumping area  
50  $\mu\text{m}$  width

Wide pumping area  
500  $\mu\text{m}$  width

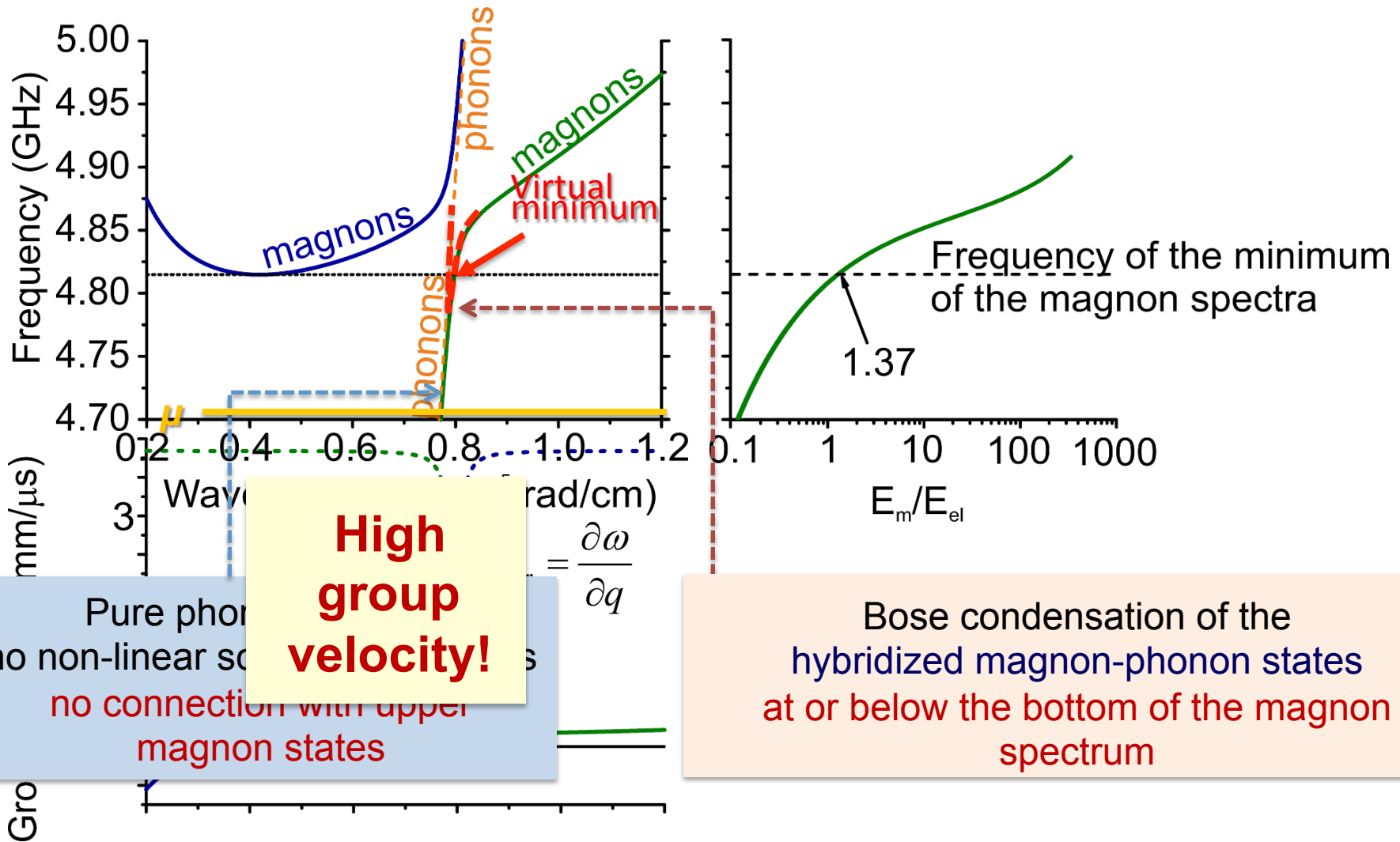


# Gaseous phase and magnon BEC at the bottom of spin-wave spectrum

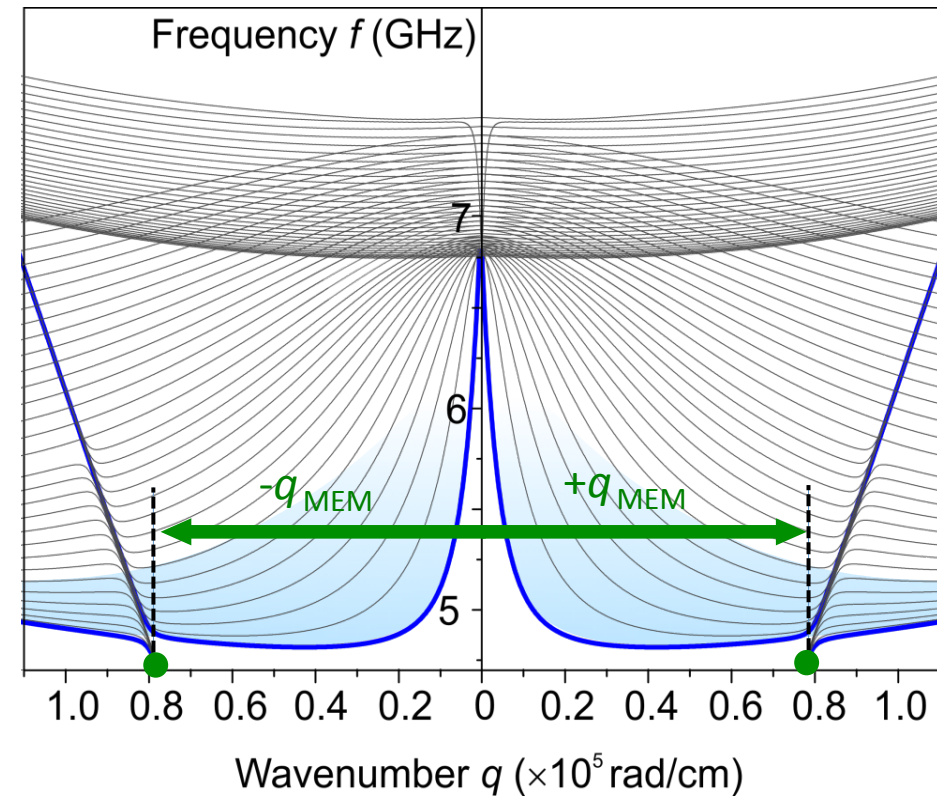
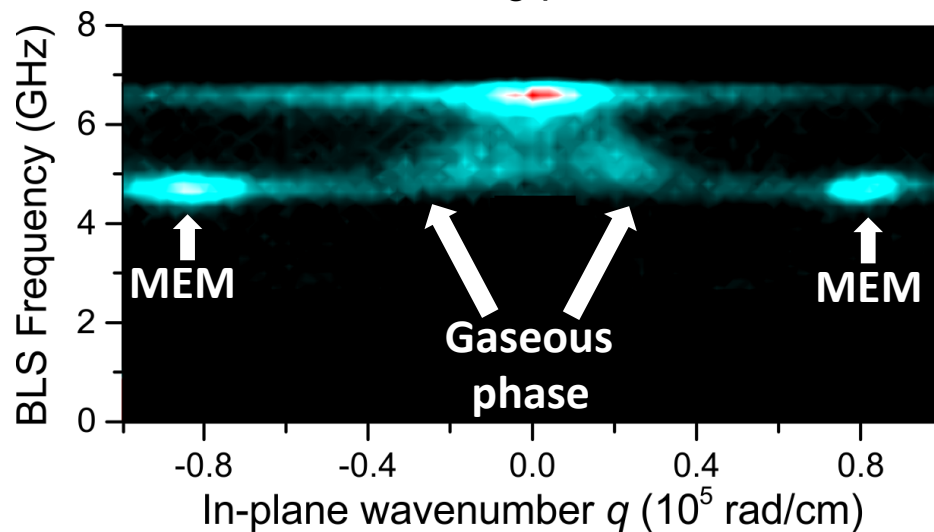
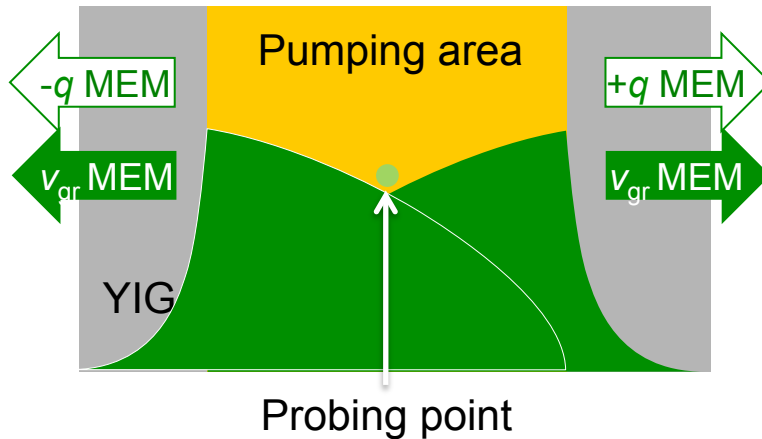


Hybridization between a phonon mode and magnon modes results in  
**magneto-elastic magnon (MEM) mode**

# Condensation of magnon-phonon hybrid particles



## Amplification of the travelling MEM mode



## Amplification of the travelling MEM mode

